



تقدم لجنة EICoM الاكاديمية

دفتر لمادة:

الالكترونيات (2)

من شرح:

د. هادي العيثاوي

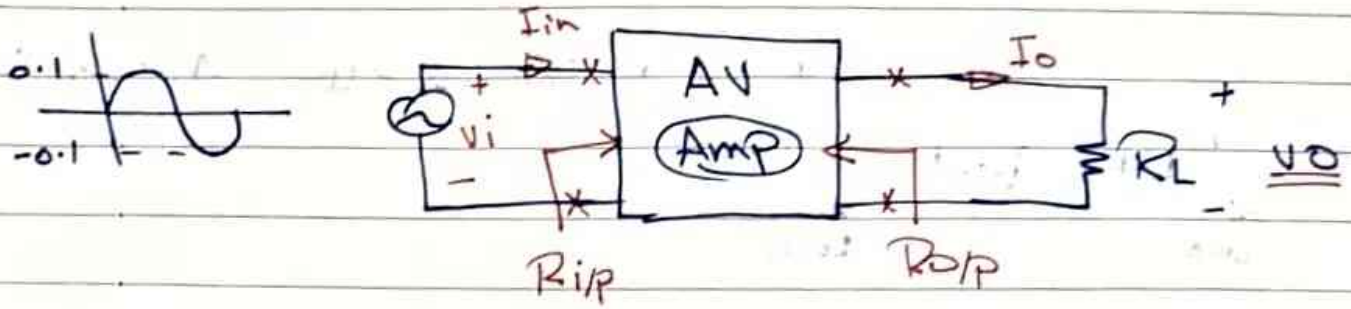
جزيل الشكر للطالب:

محمد مباح



- * non-inverting \Rightarrow Phase shift = 0°
- * inverting \Rightarrow Phase shift = 180°

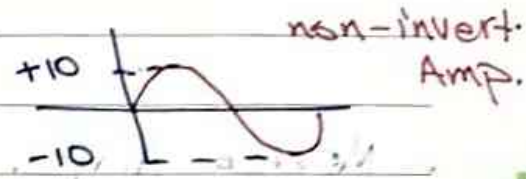
11



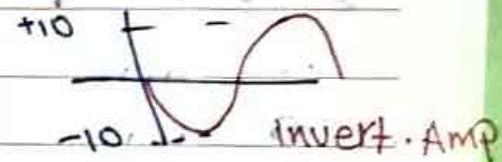
$$v_o = AV \cdot v_i$$

$$AV = \frac{v_o}{v_i} = \frac{10}{0.1} = \underline{\underline{100}}$$

volt: Gain



$$AV = \frac{v_o}{v_i} = \frac{-10}{0.1} = \underline{\underline{-100}}$$



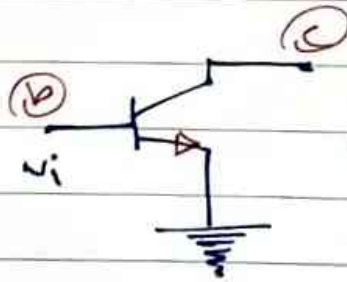
$$(AI = \frac{I_o}{I_{in}})$$

FAM

* BJT Amp :-

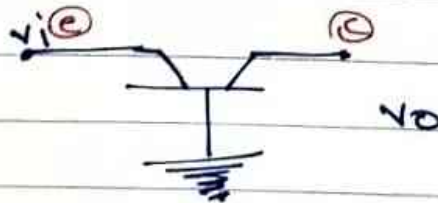
① C.E Amp

المشغل (بيني)
المشغل، المشغل، المشغل



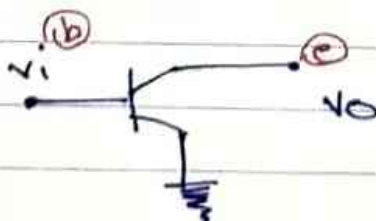
\Rightarrow تكبير التيار والقوة

② C.B Amp



\Rightarrow تكبير القوة ولا تكبير

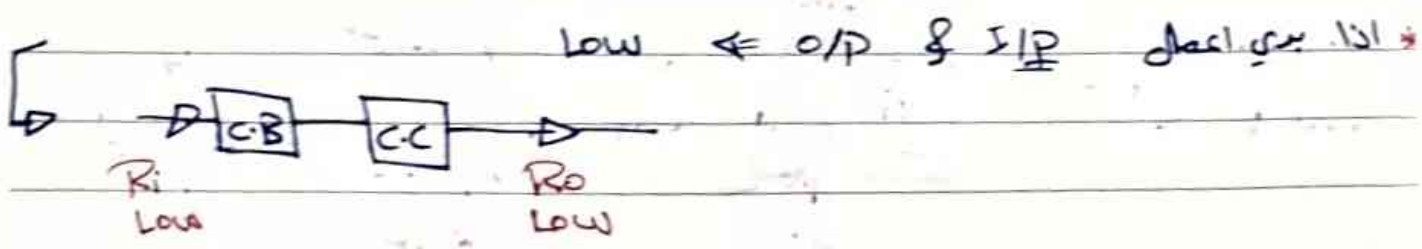
③ C.C Amp



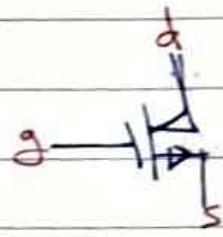
\Rightarrow تكبير التيار ولا تكبير

④ Multistage.

* لكل dc. Anal وجوب شروط اذا انجز بل FAM وانا صفت Ac. Anal



* Mosfet Amp :-



↳ Sat.)i celt dia^

- ① C.S Amp
- ② C.G Amp
- ③ C.D Amp
- ④ cascade

Ac. Analys. \rightarrow sat)i on 3rd & 4th de Analys. i/c Mosfet)i celt dia *

* $\int \frac{d}{dc}$ / Amp & invert / Amp & non-invert. / multipi

Amp)i celt dia

* $I_{BQ} \rightarrow I_{CQ} \rightarrow V_{CEQ} \Rightarrow \underline{DC}$.

* total response = DC Res + AC Res.

ch XI

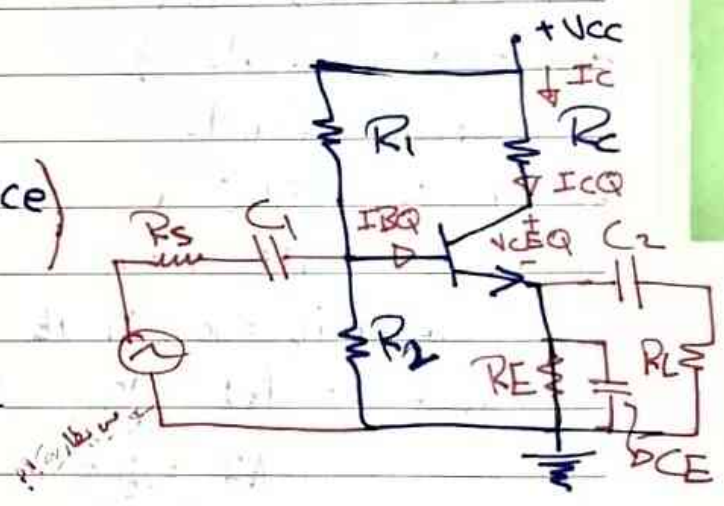
* The BJT must be biased in F.A.M to be used as an Amp.

* The Amp. is a Linear Net: used to Amplify A.C input signal.

* Any Amp. must contain:-

a) D.C source(s)
(to bias the Active device)
in proper mode

b) - Ac. source to supply Ac input signal



c) - capacitors (coupling & blocking)



DC
 $C_1, C_2, C_E \Rightarrow$ open ckt

d) - Resistors

biasing (R_1, R_2, R_E)

To control V_{CE} (R_C)

To stab. Q-pt (R_E)

as a Load (R_L)

AC
 $C_1, C_2, C_E \Rightarrow$ short ckt

AC \Rightarrow $P_{disp} \rightarrow$ source! open ckt \Rightarrow cap bill \Rightarrow \Rightarrow \Rightarrow

* $R_L \Rightarrow$ Load

* $R_C \Rightarrow V_{CE} = V_{CC} - I_C R_C \Rightarrow$ to protect I_C

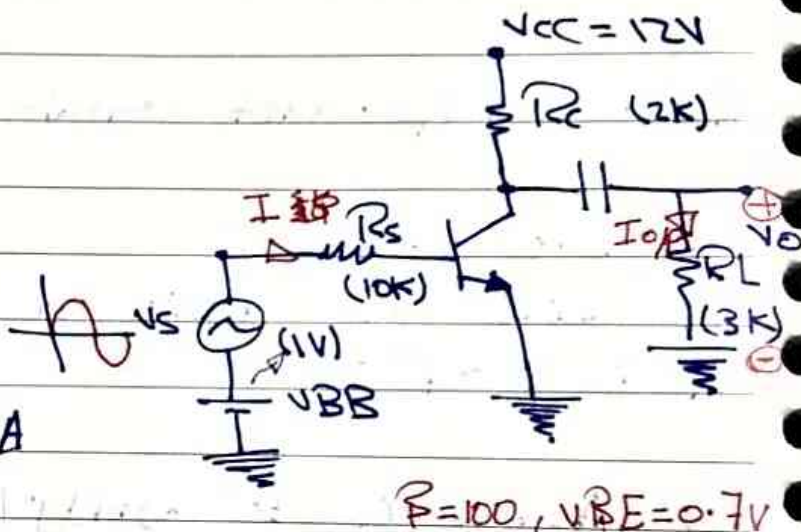
* $R_1, R_2 \Rightarrow$ volt. divid \Rightarrow Biasing Res. \Rightarrow to control I_B

* $R_E \Rightarrow$ stablized Q-point against β variation f_{TC}

AC) voltage cap) bias v. آفوق فلقه AV) اعرف CE) لىه *
 . AV) عافى short cct) عافى

graphical Analysis of basic AMP.

- ① calculate :-
 I_{BQ}, I_{CQ}, V_{CEQ}
- ② Draw D.C.L.L & Located Q-PT
- ③ if V_s drives a base current of the form $i_b = 20 \sin \omega t \mu A$



calculate :- $AV = \frac{V_o}{V_s}$
 $AI = \frac{I_o}{I_s}$

- ④ write expressions for :-
 I_B, I_C, V_{CE}

Sol :-

since the Amp is Linear cct so superposition is used.

- ① D.C source effect ($V_s = 0$)

for D.C Anal. \Rightarrow A.C \rightarrow Short cct.
 cap \rightarrow O. cct.

\Rightarrow

* FAM \Rightarrow NPN $\rightarrow V_C > V_B \rightarrow$ Reverse
 \rightarrow Forward.

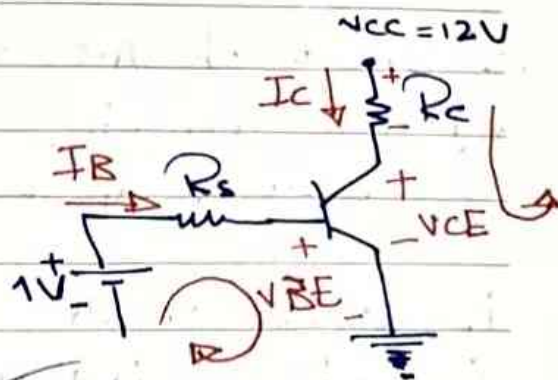
5

* Assume BJT in FAM.

$$-1 + I_B R_B + V_{BE} = 0$$

$$I_B = \frac{(1 - 0.7) V}{10K} = 0.03 mA$$

$$= \boxed{30 \mu A = I_{BQ}}$$



$$I_C = \beta I_B = 100 * 0.03 = \boxed{3 mA = I_{CQ}}$$

$$-V_{CC} + I_C R_C + V_{CE} = 0$$

$$V_{CE} = 12 - 3 * 2 = \boxed{6 V = V_{CEQ}}$$

② D.C.L.L

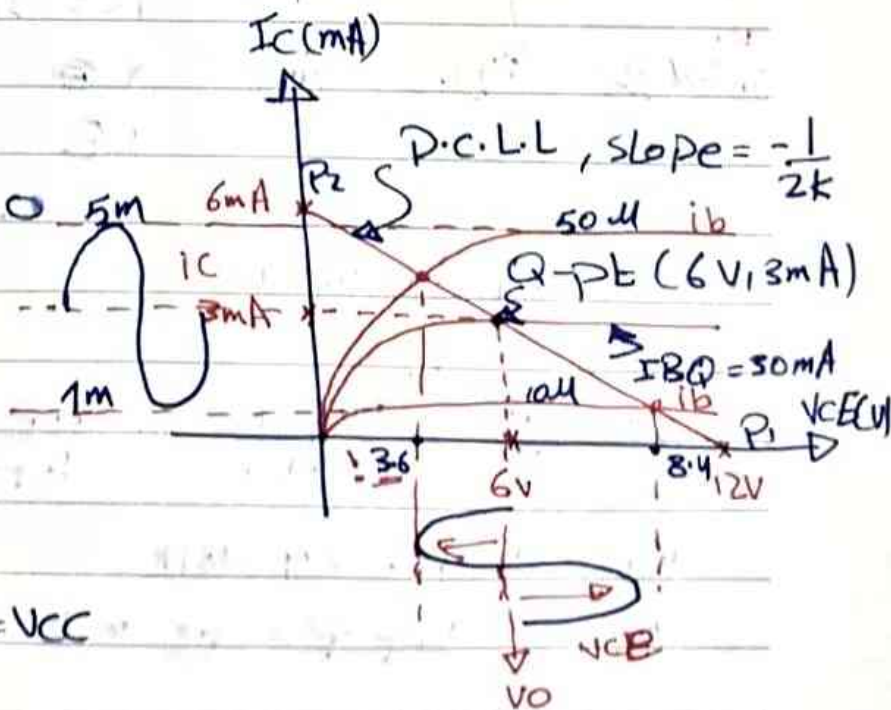
KVL for C-E Loop

$$\Rightarrow -V_{CC} + I_C R_C + V_{CE} = 0$$

$$V_{CE} = V_{CC} - I_C R_C$$

D.C.L.L. eq.

$$\text{slope} = -\frac{1}{R_C}$$



$V_{CE}(V)$

Ⓐ for $I_C = 0$, $V_{CE} = V_{CC}$

$P_1 (12V, 0)$

Ⓑ for $V_{CE} = 0$, $I_C = \frac{V_{CC}}{R_C} = 6mA$

$P_2 (0, 6mA)$

2, 10

$2 + 5 \sin 10 + \sin$

?

کے لیے 3.6, 8.4 کے لیے ??

* اذا ما مضى R_L في R_C و R_L و R_C و R_L و R_C و R_L و R_C و R_L و R_C

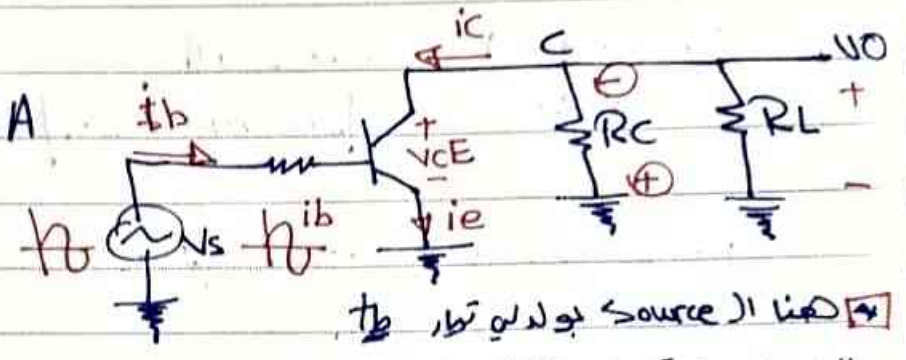
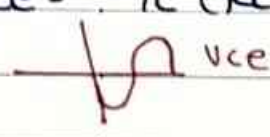
6

② Effect of A.C source (DC → D.S.C)

* For Ac Analysis

D.C → D.S.C, Cap → D.S.C

$i_b = 20 \sin \omega t \text{ mA}$
 $i_c = \beta i_b = 2 \sin \omega t \text{ mA}$
 $V_{ce} = -i_c (R_C // R_L)$



هنا ال source بولونو تار، i_b
 والي بولونو خرونه بولونو صغارو V_{ce}
 والي بولونو عس اعلى، i_c

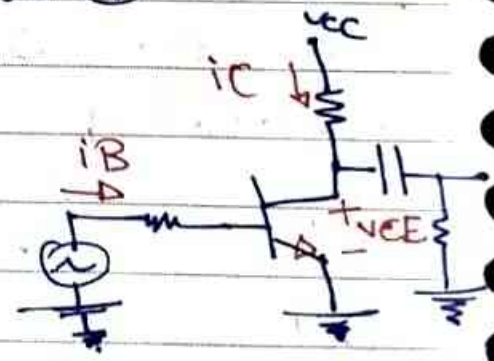
* According to superposition

$I_B = I_{BQ} + i_b \Rightarrow i_B = (30 + 20 \sin \omega t) \text{ mA}$
 $i_c = I_{CQ} + i_c = (3 + 2 \sin \omega t) \text{ mA}$
 $V_{CE} = V_{CEQ} + V_{CE}$
 $V_{CE} = -i_c (R_C // R_L) = -2 \sin \omega t (3 // 2)$
 $= -2.4 \sin \omega t \text{ (V)}$

$V_{ce} = 6 - 2.4 \sin \omega t \text{ V}$

③ $A_V = \frac{V_O}{V_S} = \frac{V_{OP-P}}{V_{SP-P}} = \frac{V_{OP}}{V_{SP}}$

$V_{OP} = V_{CEP} = 2.4 \text{ Volt}$
 $V_{OP-P} = V_{CEP-P} = 4.8 \text{ Volt}$



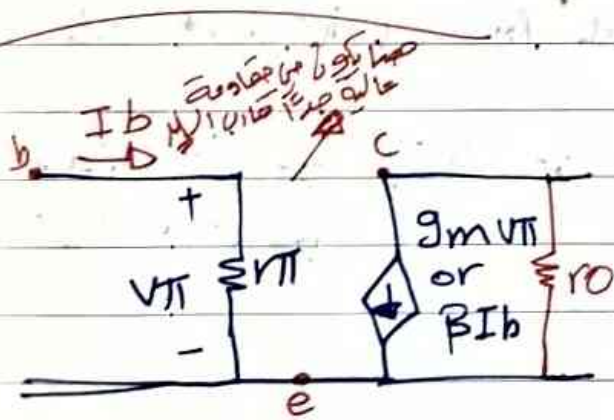
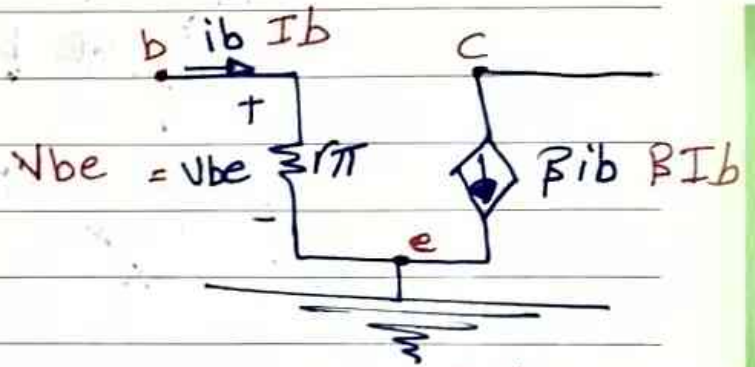
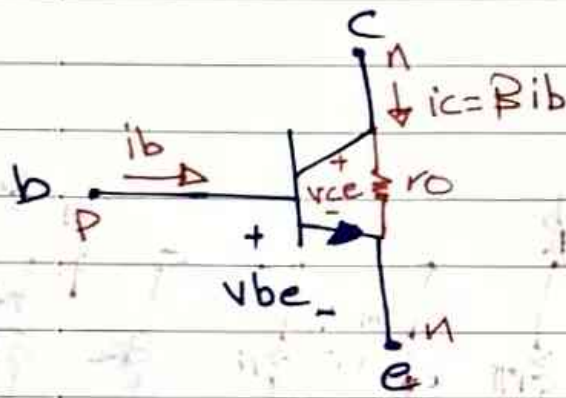
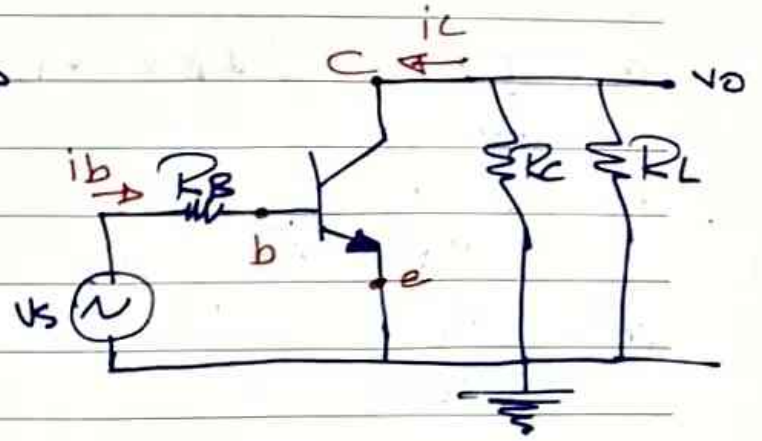
for this ccb $I_S = I_B$

$A_I = \frac{I_O}{I_S} = \frac{V_O}{R_L} = \frac{-0.8 \sin \omega t}{0.02 \sin \omega t} = -40 \text{ mA}$

* $i_c \text{ max} \rightarrow V_{ce} \text{ min}$
 $i_c \text{ min} \rightarrow V_{ce} \text{ max}$
 * $V_{ce} = D??$ Ic N projection i_c
 D.C.L.L. i_c

BJT in FAM Reverse biased PN Junc \leftarrow open ckt \leftarrow $\epsilon_0 \epsilon_r \frac{Q}{d}$

* To perform AC Analysis the BJT is replaced by its hybrid- π model



* currents in Real represents phase current.

r_{π} :- Diffusion resistance (B-E resistance)
 $r_{\pi} = \frac{\beta V_T}{I_{CQ}}$

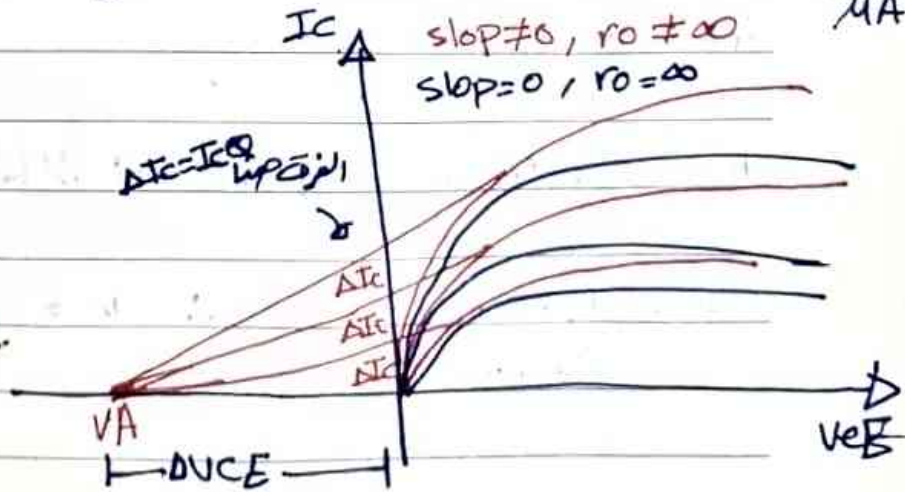
g_m :- Transconductance (A/V), mA/VA

hybrid- π model

$$g_m = \frac{I_{CQ}}{V_T} \quad (\text{mA/V})$$

$$r_o = \frac{V_A}{I_{CQ}} \quad \text{---} \quad \text{D.C Anal.}$$

- V_A :- Early voltage
 (90 < V_A < 300) V



$r_o \rightarrow$ ∞ \rightarrow $V_A \rightarrow \infty$ \rightarrow Small \rightarrow $r_o = \infty$ \rightarrow $V_A \rightarrow \infty$

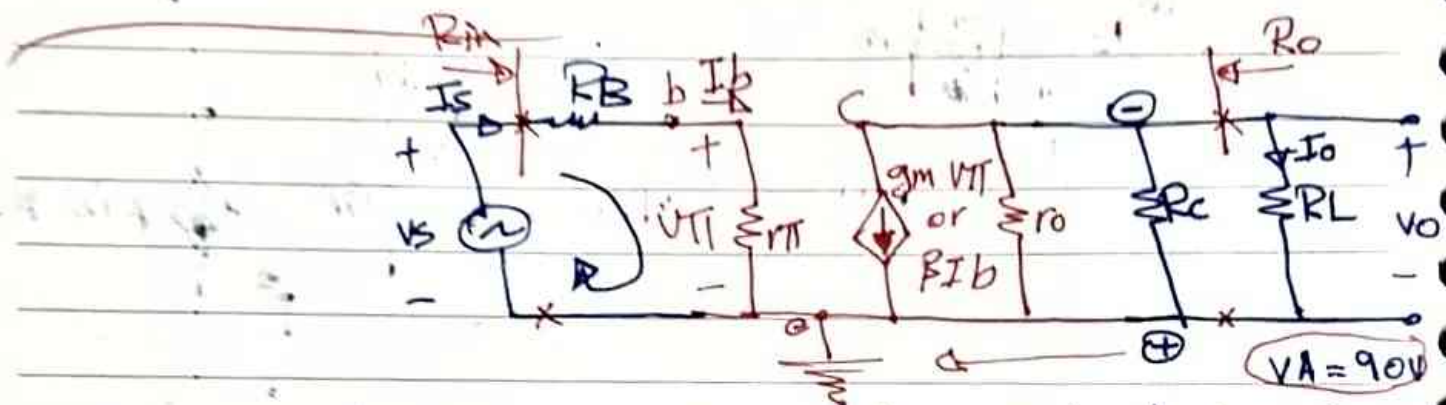
* Small signal \Rightarrow Linear linearity لا تنطبق على
 \hookrightarrow Input signal \rightarrow small \rightarrow Q-pt لا تنطبق على

181

$$r_o = \frac{\Delta V_{CE}}{\Delta I_C} \quad (I_B = \text{constant})$$

$$r_o = \frac{1}{\text{slope of } I_C \text{ lines}}$$

$$r_o = \frac{V_A}{I_{CQ}}$$



Small-signal A.C equivalent ckt

* calculate :- A_V, A_I
 Input Res. (R_{in})
 output Res. (R_o)

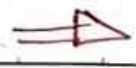
* اذا R_L ماضى R_L في I_o
 في R_C على R_o

Sol:-

$$A_V = \frac{V_o}{V_S}$$

$$V_o = -g_m v_{\pi} \bar{R}_L \quad , \quad \bar{R}_L = r_o \parallel R_C \parallel R_L$$

$$v_{\pi} = \frac{V_S \cdot r_{\pi}}{r_{\pi} + R_B} \quad \therefore V_o = -g_m \bar{R}_L \frac{V_S \cdot r_{\pi}}{r_{\pi} + R_B}$$



including R_L في R_o نظرًا لأن R_L في I_o *
 في R_C نظرًا لأن R_C في I_o *

(in this ex.)

* لوان اعطانيه تقدر انا v_o تقدر انا v_s

$$\frac{v_o}{v_s} = A_V = -g_m \bar{R}_L \frac{r_{\pi}}{r_{\pi} + R_B}$$

⊖ means 180° phase shift between v_o & v_s (only in CE)

$$A_V = \frac{v_o}{v_s} = \frac{v_o}{v_{\pi}} \cdot \frac{v_{\pi}}{v_s}$$

$$= -g_m \bar{R}_L \frac{r_{\pi}}{r_{\pi} + R_B}$$

$$\underline{I_{CQ} = 3mA}$$

$$g_m = \frac{I_{CQ}}{V_T} = \frac{3mA}{26mV} \quad (A/V) \rightarrow \underline{mA/V} \text{ or } (mV/V)$$

$$g_m = \frac{3000}{26} mA/V \approx 115 mA/V$$

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}} = \frac{100 * 26mV}{3mA} = 860 \Omega$$

$$\Rightarrow \bar{R}_L = r_o \parallel R_C \parallel R_L$$

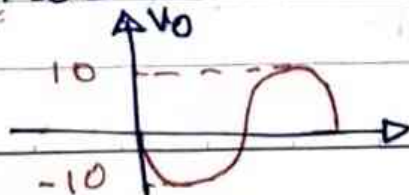
$$r_o = \frac{V_A}{I_{CQ}} = \frac{90V}{3mA} = 30 K\Omega$$

$$\bar{R}_L = 30K \parallel 2 \parallel 3K \Rightarrow \bar{R}_L = 1.1 K\Omega$$

$$A_V = 115 * 1.1 \frac{0.86}{10 + 0.86} = -126 * 0.08 = \underline{\underline{-10}}$$

$$A_V = \frac{v_o}{v_s} = -10 \Rightarrow v_o = -10 v_s$$

$$\text{for } v_s = 0.1 \sin \omega t \text{ V} \Rightarrow v_o = -1 \sin \omega t$$



→ 1 (for this ckt)

current dev. $AI = \frac{I_o}{I_s} = \frac{I_o}{I_b} \cdot \frac{I_b}{I_s}$

منه ايل الس
التيه الس

$$I_o = -\beta I_b \cdot \frac{\bar{R}_c}{\bar{R}_c + R_L} \Rightarrow \frac{I_o}{I_b} = \frac{-\beta \bar{R}_c}{\bar{R}_c + R_L}$$

$$\bar{R}_c = r_o \parallel R_c$$

$$\frac{I_b}{I_s} = 1 \Rightarrow \therefore AI = \frac{-\beta \bar{R}_c}{\bar{R}_c + R_L}$$

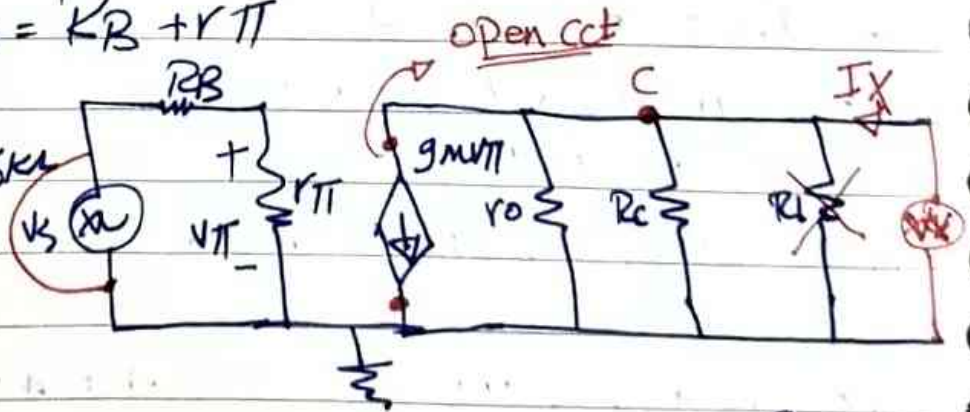
$$\bar{R}_c = 30K \parallel 2K = 1.8K$$

$$\Rightarrow AI = \frac{-100 \times 1.8}{1.8 + 3} = \frac{-180}{4.8} = \underline{\underline{-37.5}}$$

$R_{in} ?? \Rightarrow R_{in} = R_B + r_{\pi}$

$$R_{in} = 10 + 0.86 = 10.86K\Omega$$

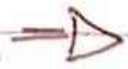
$$\Rightarrow R_o = \frac{V_x}{I_x} \Big|_{V_s=0}$$



KVL at node C

Since $V_s = 0 \Rightarrow v_{\pi} = \frac{V_s R_{\pi}}{R_{\pi} + R_B} = 0$

$$\Rightarrow I_x = \frac{V_x}{R_c} + \frac{V_x}{r_o} + g_m v_{\pi}$$



$$\frac{I_X}{V_X} = \frac{1}{R_C} + \frac{1}{r_o} = \frac{1}{R_o}$$

$$\therefore R_o = R_C \parallel r_o$$

When $V_S = 0 \Rightarrow V_{IT} = 0 \Rightarrow \therefore g_{mVT} = 0$

Dependent c.s is 0

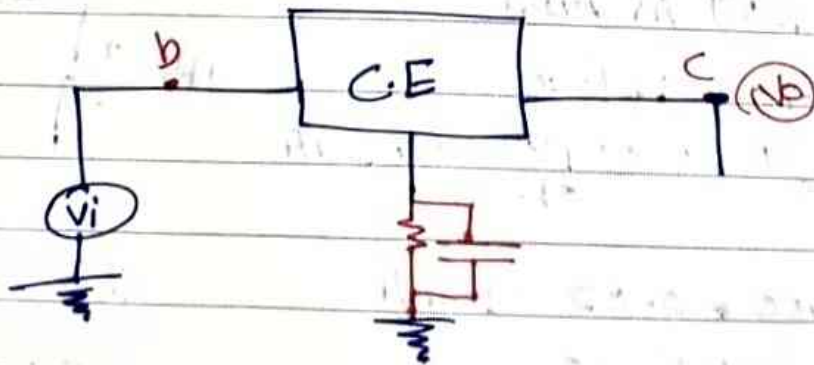
$$\therefore R_o = R_C \parallel r_o = 2 \parallel 30k \Rightarrow R_o = 1.98k\Omega$$

Single Stage BJT Amp

① common Emitter Amp (CE)

$v_i \rightarrow$ base, v_o from C

e \rightarrow common Terminal



Basic C.E

C.E with R_E

C.E with R_E & C.E

* إذا كان الـ BJT في FAM لا يقدر، الصيغة هي Amp

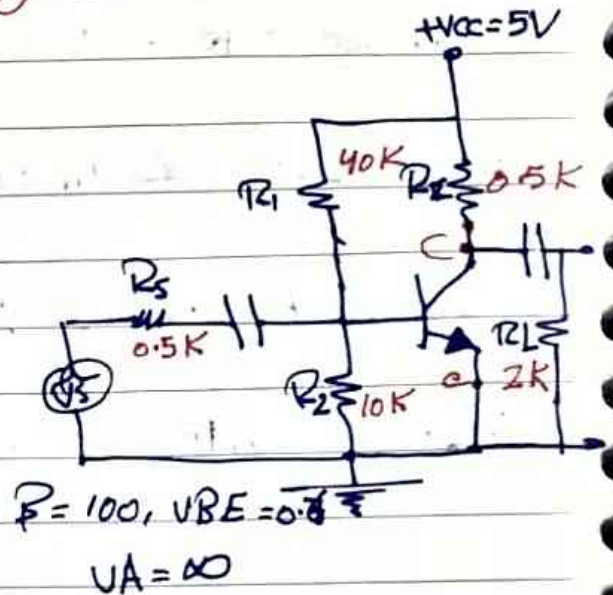
12

① Basic C.E Amp.

E-D is directly connected to ground

Ex:-

- ① calculate I_{CQ} , V_{CEQ}
- ② Draw s.s. AC equivalent ckt & find:- A_V , A_I
 R_i , R_o
- ③ Draw D.C & A.C.L.L & find their slope



Sol:-

① D.C. Analysis.

cap \rightarrow O.C, AC \rightarrow S.C

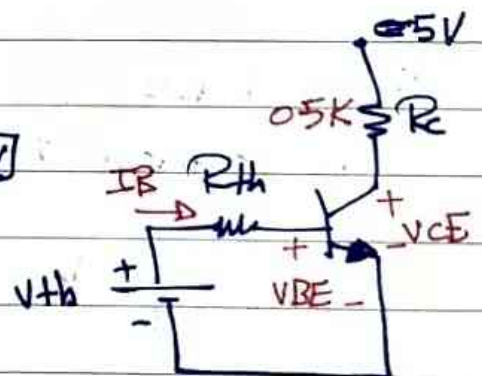
$R_{th} = R_1 || R_2 = 10 || 40 = 8K$

$V_{th} = 5 \cdot \frac{R_2}{R_1 + R_2} \Rightarrow V_{th} = \frac{5 \cdot 10}{40 + 10} = 1V$

Assume the BJT in FAM

$-V_{th} + I_B R_{th} + V_{BE} = 0$

$I_B = \frac{(1 - 0.6)V}{8K} = \frac{0.4V}{8K} = 0.05mA$



$I_C = \beta I_B = 100 \cdot 0.05 = 5mA$

$-5 + I_C R_C + V_{CE} = 0$

$V_{CE} = 5 - 5 \cdot 0.5 = 2.5V$

$I_B = + \checkmark$

$V_{CE} > V_{BE} \checkmark$

BJT FAM conditions

\Rightarrow

* إذا كان الـ BJT في FAM لا يقدر، الصيغة هي Amp
 $R_{in} = (R_L || \beta R_E)$ Find R_{in} seen by the volt. source

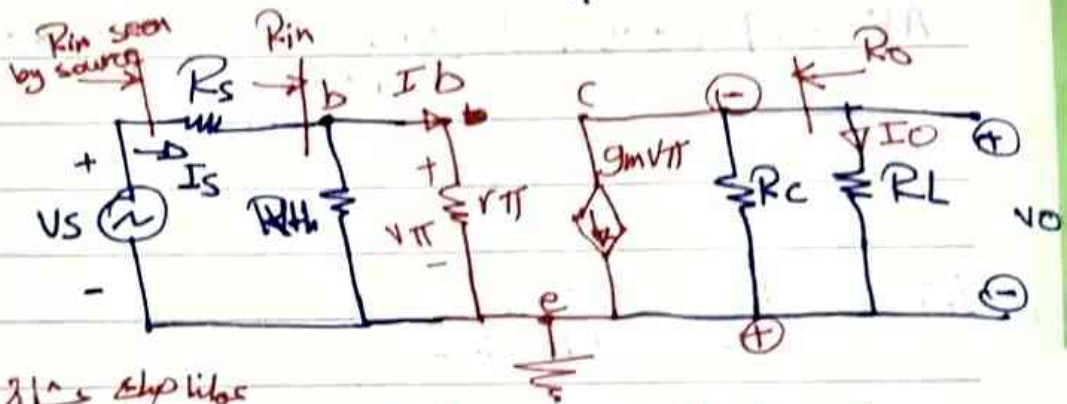
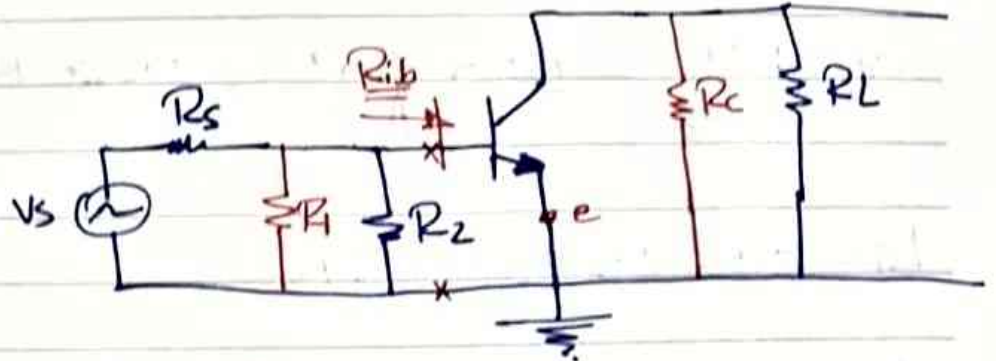
* $R_{in} \Rightarrow R_{input}$ seen by the base (b)

\hookrightarrow $\frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$

R_{in}

zcc sig amplifier, R_{in} & R_{out}

② A.C. Analysis



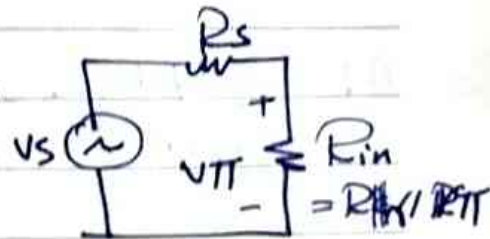
V_{Th}, V_{Th} \rightarrow $\frac{V_{Th}}{R_{Th}}$ \rightarrow $\frac{V_{Th}}{R_{Th}}$

s.s. A.C equivalent cct.

$$\Rightarrow AV = \frac{V_O}{V_S} = \frac{V_O}{V_{Th}} \cdot \frac{V_{Th}}{V_S}$$

$$V_O = -g_m V_{Th} (R_C \parallel R_L) \Rightarrow \frac{V_O}{V_{Th}} = -g_m (R_C \parallel R_L)$$

$$\frac{V_{Th}}{V_S} = \frac{R_{in}}{R_{in} + R_S} \quad (\text{V.D})$$



$$\therefore AV = -g_m (R_C \parallel R_L) \frac{R_{in}}{R_{in} + R_S}$$

$$g_m = \frac{I_{CQ}}{V_T} = \frac{5\text{mA}}{26\text{mV}} = 192 \text{ A/V}$$

$$R_{in} = R_{Th} \parallel R_{Th}$$

\Rightarrow

* C.E \Rightarrow $V \parallel$ $I \parallel$

14

$$R_{in} = R_{th} \parallel r_{\pi}$$

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}} = \frac{100 \times 26 \text{ mV}}{5 \text{ mA}} \approx 0.520 \text{ k}\Omega$$

$$R_{in} = 8 \parallel 0.52 \approx 0.5 \text{ k}\Omega$$

$$A_V = -192 (0.5 \parallel 2) \frac{0.5}{0.5 + 0.5} = -192 \times 0.4 \times 0.5$$

$$A_V = -38$$

$$\Rightarrow A_I = \frac{I_o}{I_s} = \frac{I_o}{I_b} \cdot \frac{I_b}{I_s}$$

$$\text{Current Dev. } I_o = -\beta I_b \frac{R_c}{R_c + R_L} \Rightarrow \frac{I_o}{I_b} = \frac{-\beta R_c}{R_c + R_L}$$

$$I_b = I_s \frac{R_{th}}{R_{th} + r_{\pi}} \Rightarrow \frac{I_b}{I_s} = \frac{R_{th}}{R_{th} + r_{\pi}}$$

$$A_I = \frac{-\beta R_c}{R_c + R_L} \cdot \frac{R_{th}}{R_{th} + r_{\pi}}$$

$$= \frac{-100 \times 0.5}{0.5 + 2} \cdot \frac{8}{8 + 0.52} = -18$$

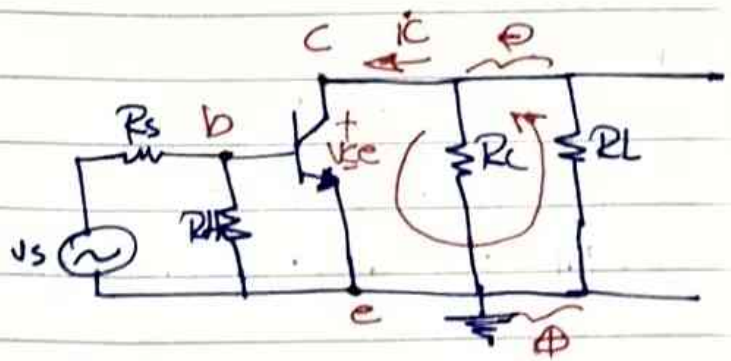
$$R_o = \frac{V_x}{I_x} \Big|_{V_s = 0}$$

* the interception between A.C.L.L of x-axis \Rightarrow the max peak output signal without distortion

[6]

A.C.L.L

Draw A.C cct
- KVL for c-e loop



$v_{ce} + i_c (R_C || R_L)$

A.C.L.L eqn

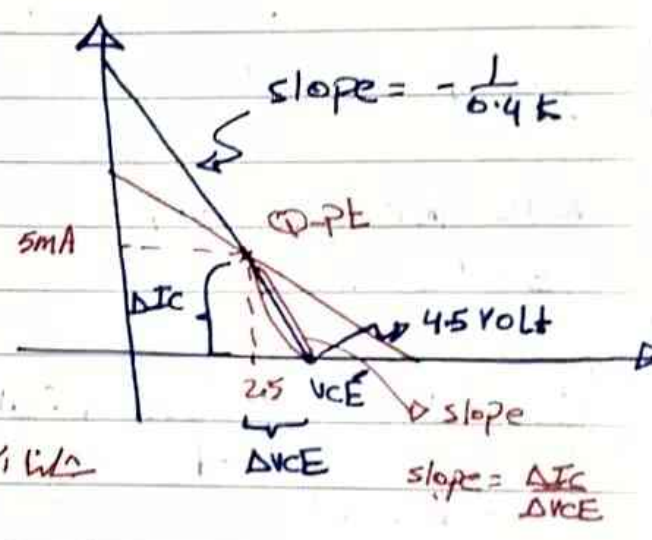
$v_{ce} = -i_c (R_C || R_L)$

slope = $-\frac{1}{(R_C || R_L)}$

slope = $-\frac{1}{0.4}$

* slope for $A_c > D_c$

slope of A.c = $\frac{\Delta I_C}{\Delta V_{CE}}$



$\frac{1}{(R_C || R_L)} = \frac{5-0}{V_{CE}-25}$

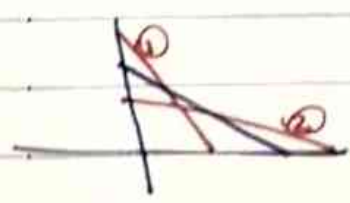
$\therefore V_{CE} = 2 + 25 = 4.5$

* Max. Peak symmetrical o/p voltage

$V_o(\text{max})_{\text{Peak}} = I_{CQ} (R_C || R_L)$

* max peak to peak symmetrical o/p voltage

$V_o(\text{max})_{pp} = 2 I_{CQ} (R_C || R_L)$



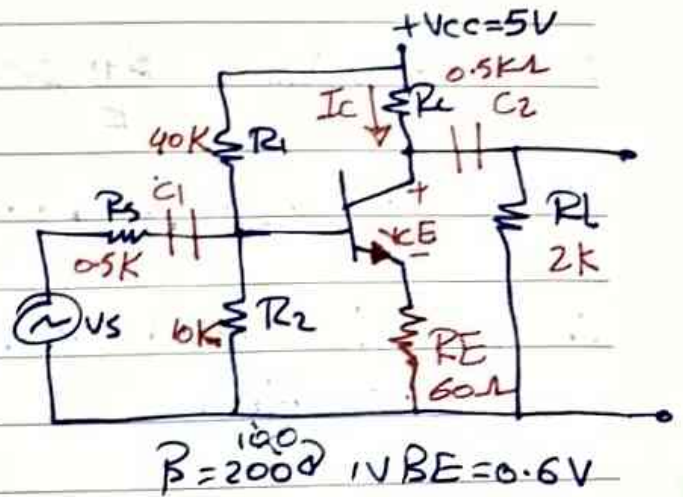
slope ① > slope ②

Handwritten notes at the bottom of the page, including Arabic text and mathematical relationships: slope AC < slope DC

(β) ما يتغير لانوسن ا) DC R_{th} I_B V_{CE} V_{CE} KVL K β FAM 0.770
 the transistor in sat mode $\beta = 200$

II CE with RE

* without RE the BJT transistor in sat mode because the both junction in ~~FAM~~ forward



* if we add RE \Rightarrow FAM \rightarrow stabilized Q-pt (function) against β variation

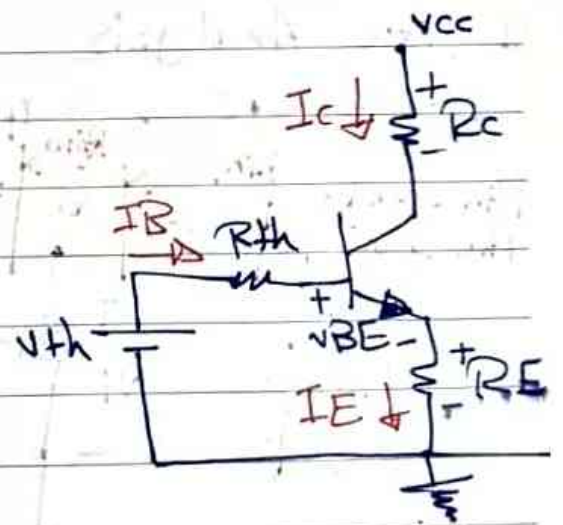
1 DC Analysis:-

AC \rightarrow S.C, CAP \rightarrow D.C

$$V_{th} = \frac{5 \cdot 10}{50} = 1V$$

$$R_{th} = 10 \parallel 40 = 8K = \cancel{276V}$$

$$-V_{th} + I_B R_{th} + V_{BE} + I_E R_E = 0$$



$$I_B = \frac{V_{th} - V_{BE}}{R_{th} + (\beta + 1)R_E} = \frac{1 - 0.6}{[8 + (201) \cdot 60]} = \frac{0.4V}{20K}$$

$$I_B \approx 0.02mA, I_{CQ} \approx \beta I_B = 4mA$$

$$V_{CE} = V_{CC} - I_C R_C - I_E R_E$$

$$I_E = (\beta + 1) I_B = \frac{\beta + 1}{\beta} I_C = 4.02 \text{ mA}$$

$$V_{CE} = 5 - 4 \times 0.5 - 4.0 \times 0.06 = 2.76 \text{ Volt}$$

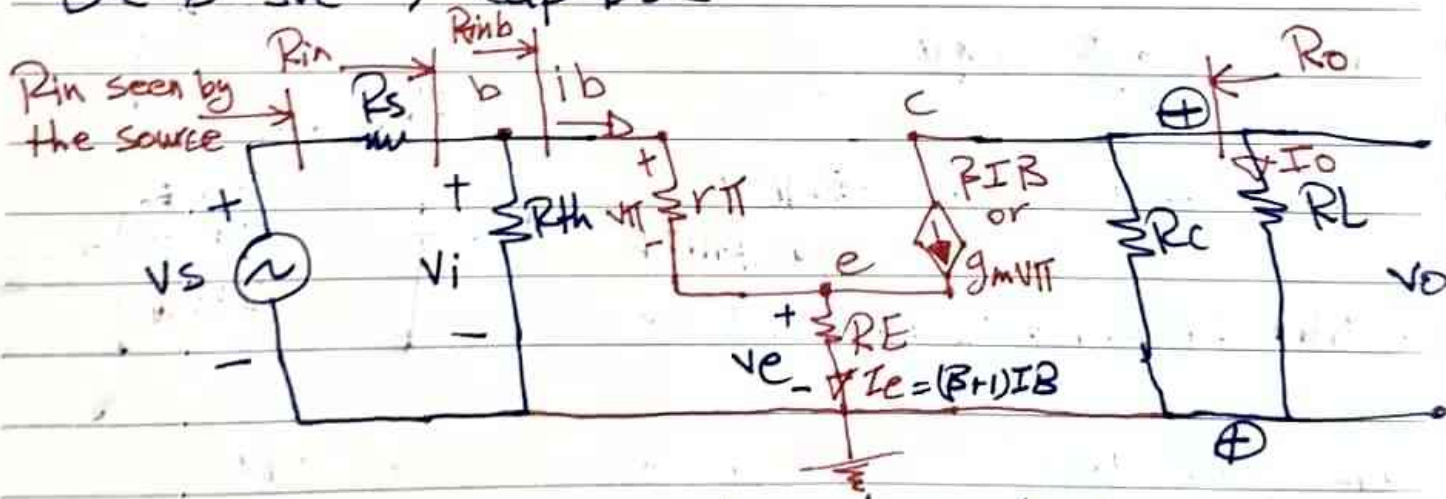
$\therefore R_E$ is used to stabilize Q-Point against β variation

* for bias-stable design \Rightarrow choose $R_{th} = 0.1(\beta + 1)R_E$

* to check bias-stable condition $\Rightarrow R_{th} \leq 0.1(\beta + 1)R_E$

② A.C Analysis

D.C \rightarrow S.C, cap \rightarrow D.S.C



s.s. AC equivalent cct.

$$A_V = \frac{V_o}{V_s} = \frac{V_o}{V_i} \times \frac{V_i}{V_s}$$

$$V_o = -\beta I_B (R_C \parallel R_L) \Rightarrow$$

Advantage.
increase R_{in} & increase R_b & reduce A_V $\Leftarrow R_E$) 1 2 3 4 *

* $A_V = 1$ unitless \rightarrow because \square its a ratio.

$$-v_i + v_{\pi} + v_e = 0$$

$$v_i = v_{\pi} + v_e = I_b r_{\pi} + (\beta + 1) I_b R_E$$

$$= I_b (r_{\pi} + (\beta + 1) R_E)$$

$$\frac{v_o}{v_i} = -\frac{\beta (R_C \parallel R_L)}{r_{\pi} + (\beta + 1) R_E}$$

$$R_{in} = R_{th} \parallel R_{ib}$$

$$R_{ib} = \frac{v_i}{I_b} = \frac{I_b (r_{\pi} + (\beta + 1) R_E)}{I_b}$$

$$= r_{\pi} + (\beta + 1) R_E$$

$$\frac{v_i}{v_s} = \frac{R_{in}}{R_{in} + R_s}$$

$$\therefore A_V = -\frac{\beta (R_C \parallel R_L)}{r_{\pi} + (\beta + 1) R_E} \cdot \frac{R_{in}}{R_{in} + R_s} \quad \therefore R_E \text{ reduces } A_V$$

$$I_{CQ} = 4 \text{ mA}$$

$$r_{\pi} = \frac{\beta V_T}{I_{CQ}} = \frac{200 \times 26 \text{ mV}}{4 \text{ mA}} = 1.3 \text{ k}\Omega$$

$$R_{ib} = 1.3 \text{ k}\Omega + (201) \times 60 = 13 \text{ k}\Omega$$



* Resistance Reflection Rule * important *

* RE stabilized the gain AV against β variation
(Independent)

20

$$R_{in} = 8K // 13 = 4.9 K\Omega \quad \therefore RE \text{ increases } R_{in}$$

$$A_V = \frac{-200(0.5 // 2)}{(1.3 + 12) K} \cdot \frac{4.9}{4.9 + 0.5}$$

$$A_V = \frac{-80}{13} \cdot \frac{4.9}{5.4} \Rightarrow \underline{A_V = -5.9}$$

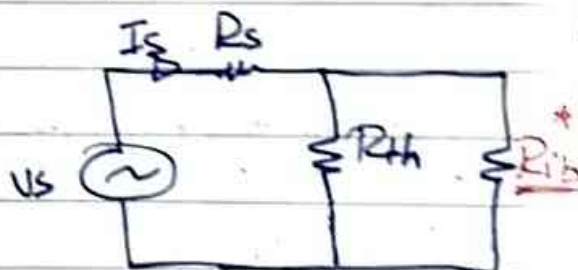
$$- AI = \frac{I_o}{I_s} \Rightarrow \frac{I_o}{I_b} \cdot \frac{I_b}{I_s}$$

$$I_o = -\beta I_b \frac{R_c}{R_c + R_L} \quad (\text{curr. dev. Rule})$$

$$\frac{I_o}{I_b} = -\frac{\beta R_c}{R_c + R_L}$$

$$I_b = I_s \cdot \frac{R_{Th}}{R_{Th} + R_{ib}}$$

$$\frac{I_b}{I_s} = \frac{R_{Th}}{R_{Th} + R_{ib}}$$



$$R_{ib} = r_{\pi} + (\beta + 1)R_E$$

$$\therefore AI = -\frac{\beta R_c}{R_c + R_L} \cdot \frac{R_{Th}}{R_{Th} + R_{ib}} = -\frac{200 \times 0.5}{2.5} \cdot \frac{8}{8 + 13} = \underline{-16}$$

$\therefore RE$ reduces AI

$$\Rightarrow R_o = \left. \frac{V_x}{I_x} \right|_{V_s=0}$$

When $V_s = 0$, $V_{\pi} = 0$, $I_b = 0$

βI_b or $g_m V_{\pi} = 0 \Rightarrow O.C$

$$\underline{R_o = R_c = 0.5K}$$

\Rightarrow

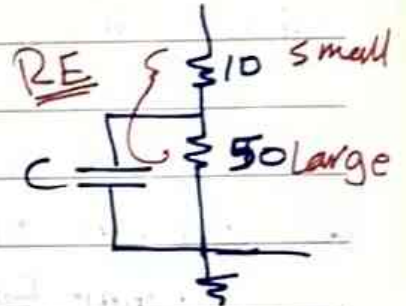
$$\therefore A_v = -\beta (R_c \parallel R_L) \cdot \frac{R_{in}}{r_{\pi} + (\beta + 1)R_E R_{in} + R_s}$$

If $(\beta + 1) \gg r_{\pi}$ & $\beta \gg 1$, $R_{in} \gg R_s$

\hookrightarrow
 $\Rightarrow A_v \approx \frac{R_c \parallel R_L}{R_E}$

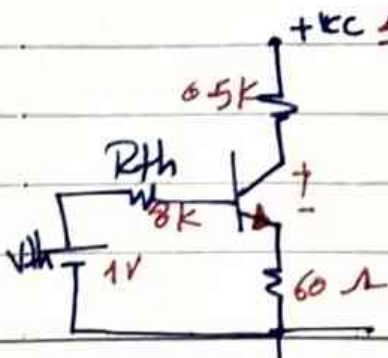
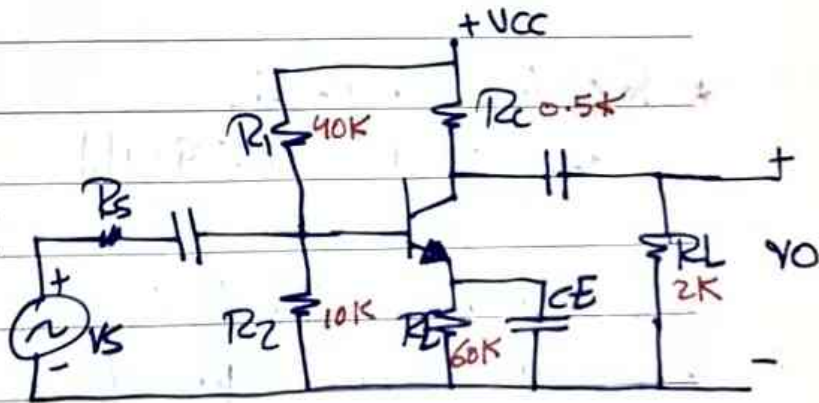
Ac

or (disadvantages) $\beta \downarrow$
 \rightarrow r_{π} is not small \rightarrow



III CE with bypass cap. CE:-

① for Dc Analysis
 CE is o.c & the ccb is
 analyzed as CE with RE



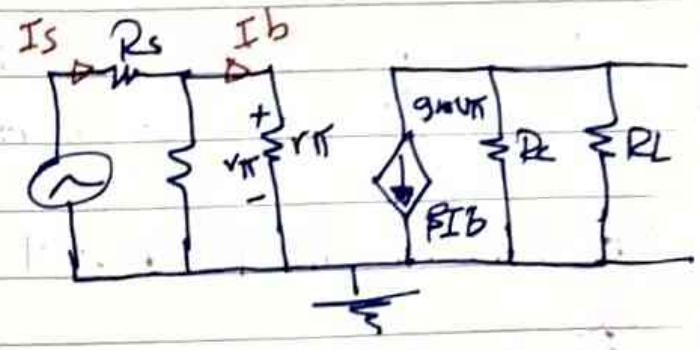
$I_{CQ} = 4 \text{ mA}$
 $V_{CEQ} = 2.76 \text{ V}$

$\beta = 200, V_{BE} = 0.6 \text{ V}$



(RE کی انگریزی) Dependent ہے β کے لئے $2, AV$) Lip*
 جو $2, R_{in}$) Lip*
 [22]

② for AC Analysis
 CE-DC → Cancels RE effect. the ckt behaves as Basic C.E Amp.



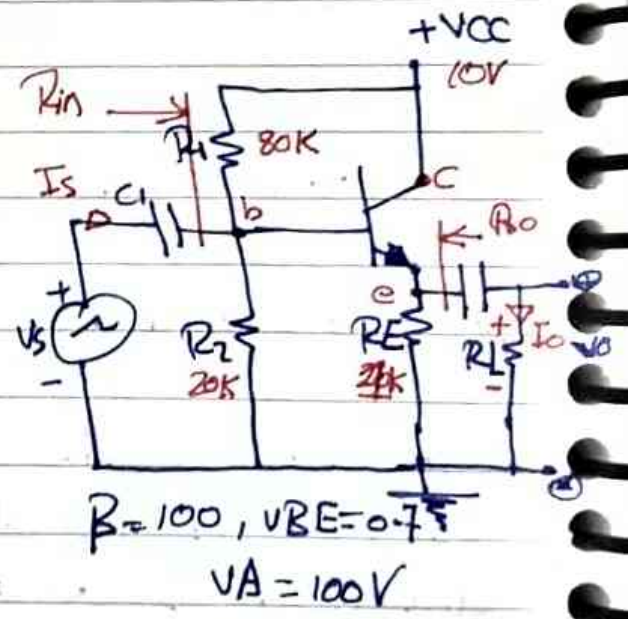
$\Rightarrow AV = -\beta \frac{(Rc // RL) \cdot Rin}{r\pi (Rin + Rs)} \approx -45$

$Rin = r\pi // Rth$

② common-collector Amp
 c.c. Amp Emitter follower.

$Vi \rightarrow$ to base
 Vo from Emitter
 common Terminal is \ominus

* For A.C Analysis
 C \rightarrow ground (C-Terminal)



- ① Determine I_{CQ}, V_{CEQ}
- ② Draw S.S.A.C eq. ckt & find AV, AI, Rin, Ro

\Rightarrow

β & β dependent source of current βI_B

23

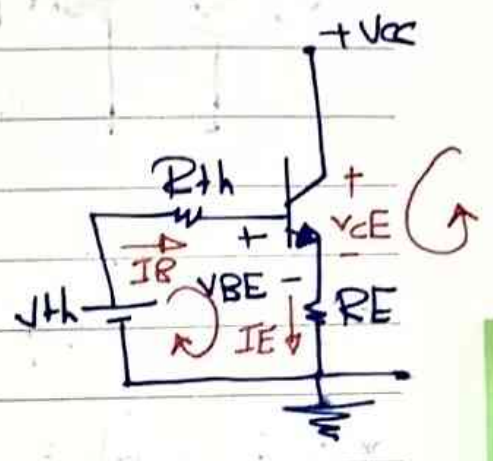
Sol:-

① D.C Analysis

C → D.C, AC → D.S.C

$R_{th} = 80 // 20 = 16k$

$V_{th} = \frac{10 * 20}{100} = 2V$



$-V_{th} + I_B R_{th} + V_{BE} + (\beta + 1) I_B R_E = 0$

$I_B = \frac{(2 - 0.7)V}{16 + 101 * 1} = \frac{1.3V}{117k\Omega} = 0.011 mA \checkmark \oplus$

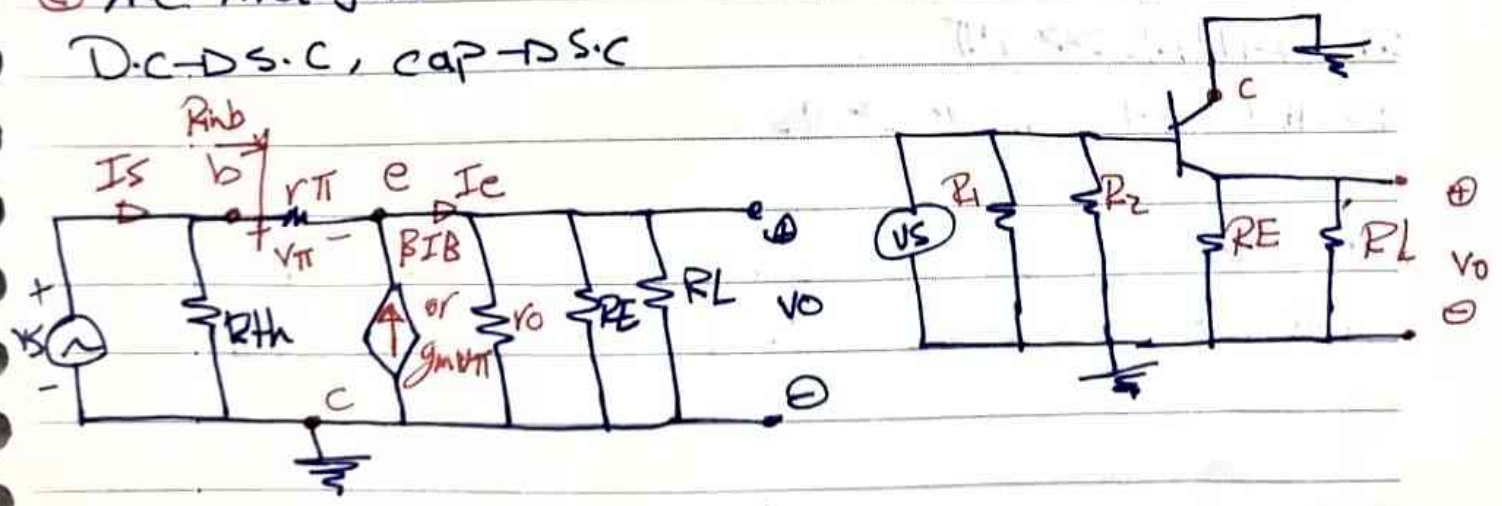
$I_C = \beta I_B = 1.1 mA, I_E = \frac{\beta + 1}{\beta} I_C$

$V_{CE} = V_{CC} - I_E R_E = 10 - 1.1 * 1 = 8.9 Volt \checkmark > V_{BE}$

∴ BJT in FAM

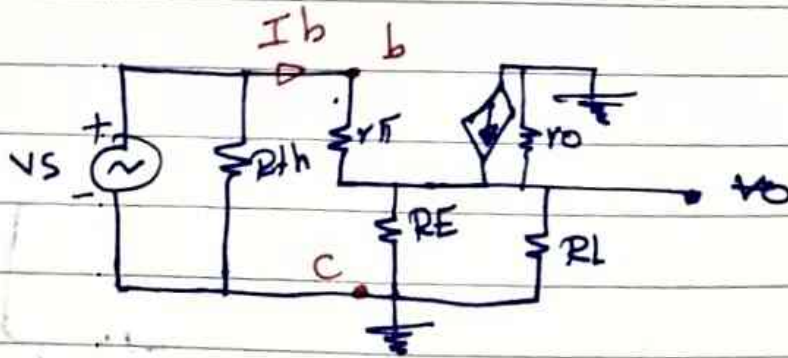
② A.C. Analysis

D.C → D.S.C, cap → D.S.C



Small signal A.C. eq. ckt.





$$A_V = \frac{V_O}{V_S} = \frac{V_O}{V_i}$$

$$V_O = I_e \cdot \bar{R}_L = (\beta + 1) I_b \bar{R}_L$$

$$\bar{R}_L = r_o \parallel R_E \parallel R_L$$

$$-V_i + V_{T\pi} + V_O = 0$$

$$V_i = V_{T\pi} + V_O$$

$$= I_b r_{\pi} + (\beta + 1) I_b \bar{R}_L$$

$$\frac{V_O}{V_i} = \frac{(\beta + 1) \bar{R}_L}{r_{\pi} + (\beta + 1) \bar{R}_L}$$

\Rightarrow ① $A_V < 1$ -> لا تكبر الفولتية

② $\phi = 0^\circ$, no phase

$$\text{IF } (\beta + 1) \bar{R}_L \gg r_{\pi}$$

$$\Rightarrow A_V \approx 1 \Rightarrow V_O \approx V_S$$

* v_o follows v_s in mag. & sign and it is taken from emitter so it is called Emitter follower

\Rightarrow

* Power Amp = AV · AI
 ? this ckt is consider as a power Amp.

25

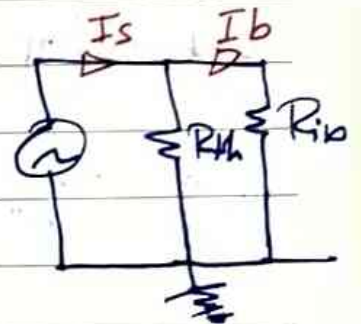
$$AI = \frac{I_o}{I_s} = \frac{I_o}{I_b} \cdot \frac{I_b}{I_s}$$

$$I_o = \frac{I_e \cdot \bar{R}_E}{\bar{R}_E + R_L} = \frac{(\beta + 1) I_b \bar{R}_E}{\bar{R}_E + R_L}$$

∴ by eq. \bar{R}_E + R_L is in parallel (c.d) I_o

$$\therefore \frac{I_o}{I_b} = \frac{(\beta + 1) \bar{R}_E}{\bar{R}_E + R_L}, \text{ where } \bar{R}_E = V_o // R_E$$

$$R_{ib} = \frac{V_i}{I_b} = \frac{I_b (r_{\pi} + (\beta + 1) R_L)}{I_b}$$



$$R_{ib} = r_{\pi} + (\beta + 1) \bar{R}_E$$

$$I_b = \frac{I_s R_{th}}{R_{th} + R_{ib}}$$

$$\frac{I_b}{I_s} = \frac{R_{th}}{R_{th} + R_{ib}}$$

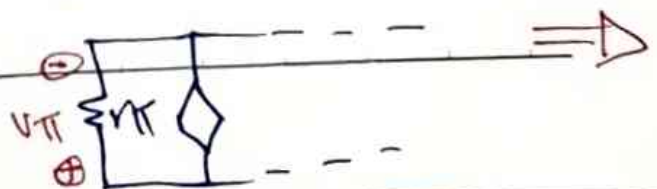
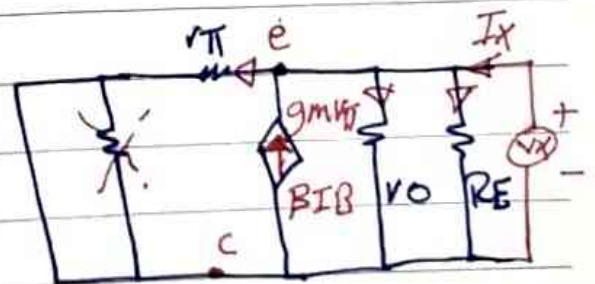
$$AI = \frac{(\beta + 1) \bar{R}_E}{\bar{R}_E + R_L} \cdot \frac{R_{th}}{R_{th} + R_{ib}} \Rightarrow * (3) AI > 1 \text{ (Current Amp)}$$

$$* R_{in} = R_{th} // R_{ib} \Rightarrow * (4) \text{ high } R_{in}$$

$$* R_o = \frac{V_x}{I_x} \Big|_{V_s=0}$$

kcl at node e

$$I_x + g_m V_{\pi} = \frac{V_x}{R_o} + \frac{V_x}{R_E} + \frac{V_x}{r_{\pi}}$$



but when $V_S = 0$

$$V_{\pi} = -V_X$$

$$I_X = V_X \left(g_m + \frac{1}{r_o} + \frac{1}{R_E} + \frac{1}{r_{\pi}} \right)$$

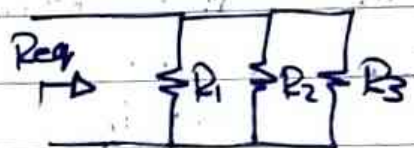
$$= V_X \left(\frac{g_m r_{\pi} + 1}{r_{\pi}} + \frac{1}{r_o} + \frac{1}{R_E} \right)$$

$$\text{but } g_m r_{\pi} = \frac{I_{CQ}}{V_T} \frac{\beta V_T}{I_{CQ}} = \beta$$

$$\frac{I_X}{V_X} = \frac{1}{R_o} = \frac{\beta + 1}{r_{\pi}} + \frac{1}{r_o} + \frac{1}{R_E}$$

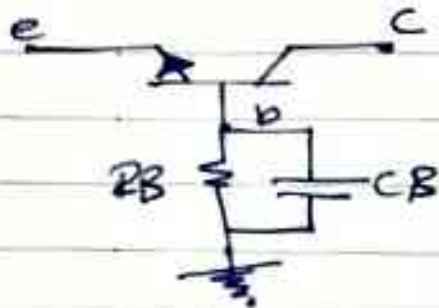
$$\therefore R_o = \frac{r_{\pi}}{\beta + 1} \parallel r_o \parallel R_E$$

⇒ Low R_o



$$R_{eq} = R_1 \parallel R_2 \parallel R_3$$

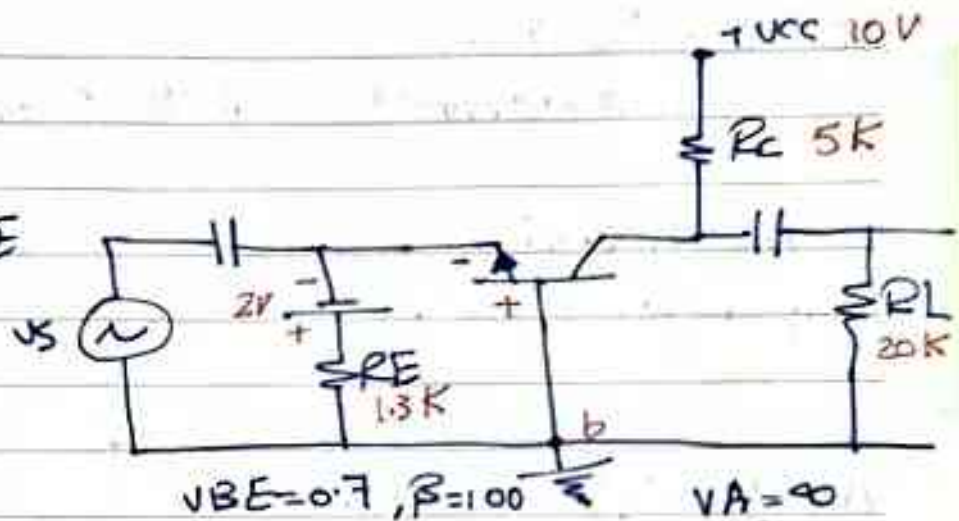
③ common - Base Amp. C.B.Amp



v_i to emitter
 v_o taken from collector
 base is common terminal

① Find I_{CQ} , V_{CEQ} , V_E

② Draw s.s.A.c eq. c.c.t & find A_V , A_I , R_{in} , R_o



SOL:-

① D.C. Analysis
 C-DO.C, A.C-DS.C

$$V_{BE} - 2 + I_E R_E = 0$$

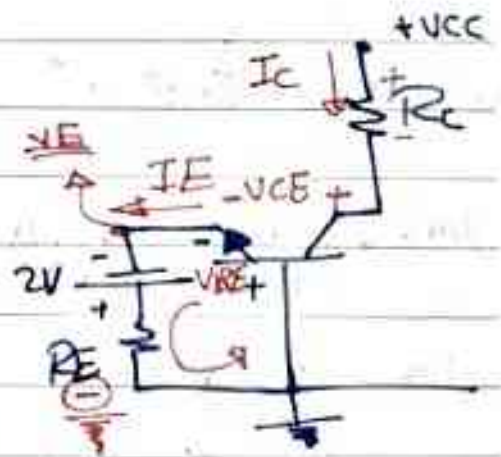
$$I_E = \frac{(2 - 0.7)V}{1.3K} = \frac{1.3V}{1.3K} = 1mA$$

$$I_C = \alpha I_E = \frac{100}{100+1} \cdot 1 = 0.99mA$$

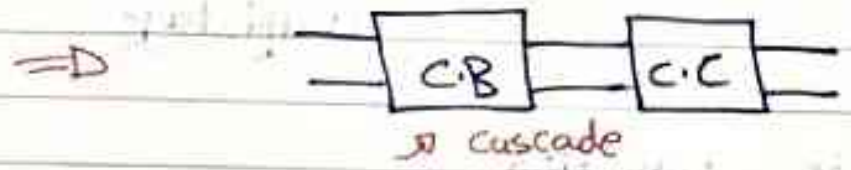
$$-V_{CC} + I_C R_C + V_{CE} - 2 + I_E R_E = 0$$

$$V_{CE} = 10 + 2 - (0.99 \times 5) - (1.3 \times 1) \Rightarrow V_{CE} = 5.8 \checkmark$$

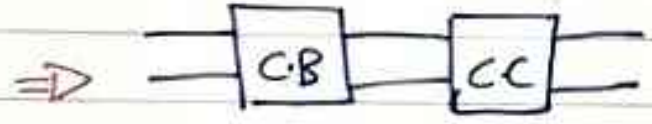
\therefore Trans in FAM




* Low R_i & R_o

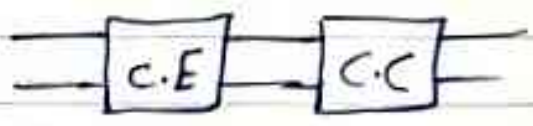


* $A_V > 1$, Low R_o , $\phi = 0^\circ$

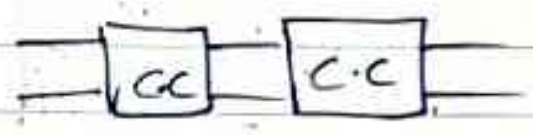



cascode \rightarrow الاضربة stage 1 R_o stage 2 R_{in} 

* $\phi = 180^\circ$

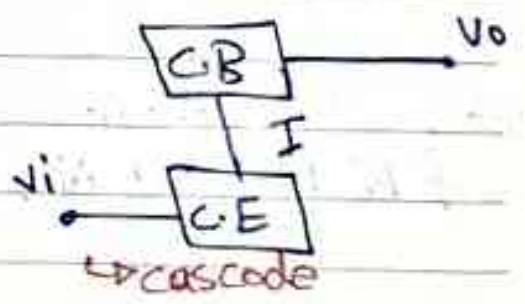


* $A_I = (\beta + 1)^2$ \rightarrow كبير جداً \Rightarrow



① stage 1 Load R_o \rightarrow stage 2 R_{in} 

* تنظيم لتأثير الكاسكود !



* Multistage BJT Amps *

Amps. contain more than ONE Transistor (At Least Two). They are used to achieve certain combined specifications which can't be achieved using single stage such as :-

- very high A_V or A_I
- Low R_o & $A_V > 1$
- Low R_o & Low R_i

* $V_{B2} = V_{C1} \Rightarrow$ $V_{B2} = V_{C1}$ \Rightarrow $V_{B2} = V_{C1}$
 نوع التوصل (C.E) \Rightarrow $V_{B2} = V_{C1}$
 توصيل مباشر

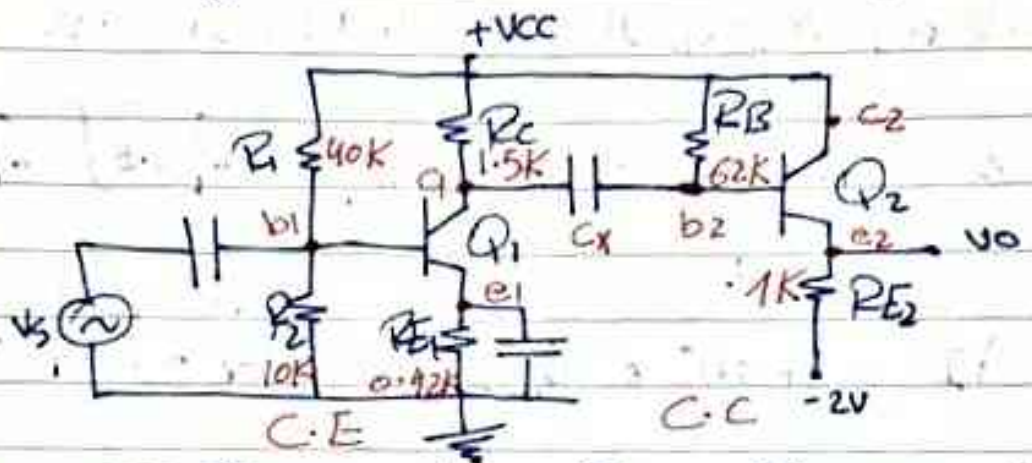
32

Multistage

Cascade connection

Cascade connection

① Cascade Multistage



① Find $I_{CQ1}, V_{CEQ1}, I_{CQ2}, V_{CEQ2}$

$\beta_1 = 100, \beta_2 = 50$
 $V_{BE1} = V_{BE2} = 0.7V$
 $V_{A1} = V_{A2} = 100V$

② Draw s.s.A.C eq. ccb
 & Find A_V, A_I, R_{in}, R_o

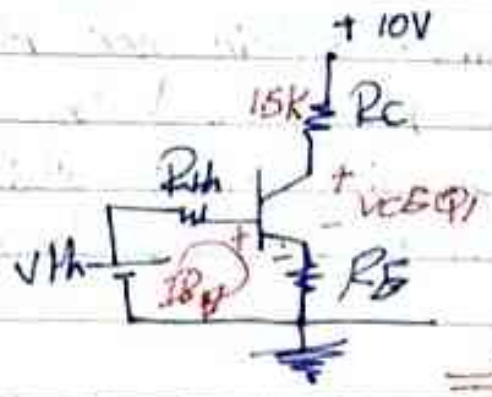
Sol:

① D.C Analysis

* Q1 (C.E)

$R_{Th} = 40 || 10 = 8K$

$V_{Th} = \frac{10 \times 10}{50} = 2V$



Q1 Pt1
 Q1 Pt2

* $V_{B2} = V_{C1} \Rightarrow$ $V_{B2} = V_{C1}$ \Rightarrow $V_{B2} = V_{C1}$
 نوع التوصل (C.E) \Rightarrow $V_{B2} = V_{C1}$
 توصيل مباشر

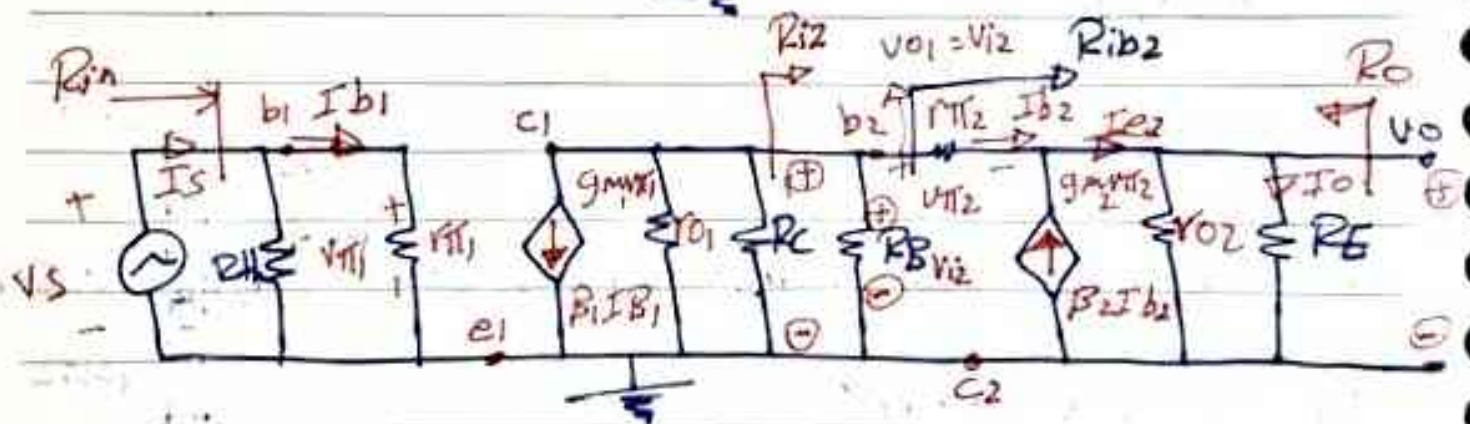
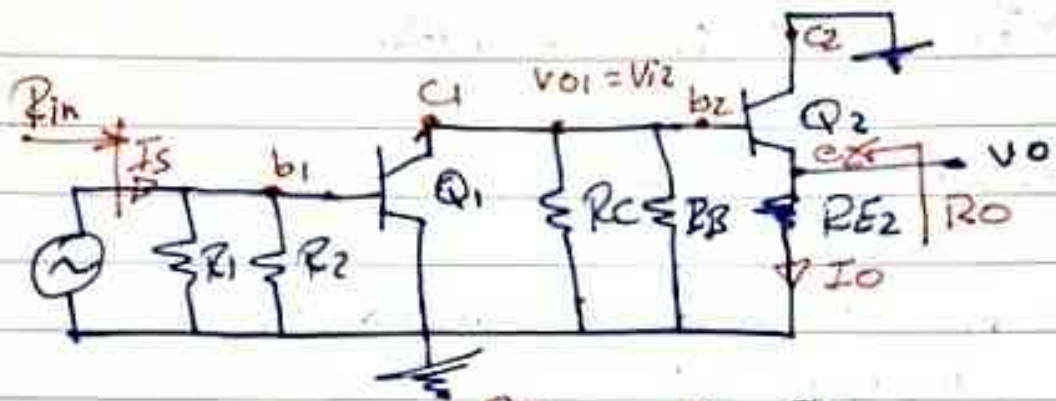
$$-10 + V_{CE2} + I_{E2} R_{E2} - 2 = 0$$

$$V_{CE2} = 12 - 5 \cdot 1 \cdot 1$$

$$V_{CE2} = \underline{6.9V}$$

② AC Analysis

Cap → D.C., D.C → A.C



S.S. A.C eq. ckt

$$* AV = \frac{V_O}{V_S} = \frac{V_O}{V_{O1}} * \frac{V_{O1}}{V_S}$$

$$V_O = I_{E2} \cdot r_{O2} \parallel R_E = (\beta_2 + 1) I_{B2} (R_{E2} \parallel r_{O2})$$

$$-V_{I2} + V_{\pi 2} + V_O = 0$$

$$V_{I2} = I_{B2} V_{\pi 2} + (\beta_2 + 1) I_{B2} (R_E \parallel r_{O2})$$



$$\frac{V_o}{V_{i2}} = \frac{V_o}{V_{o1}} = \frac{(\beta_2 + 1)(R_E \parallel r_{o2})}{r_{\pi 2} + (\beta_2 + 1)(R_E \parallel r_{o2})}$$

$$A_{V2} < 1 \text{ (c.c.)}$$

$$\Rightarrow V_{o1} = -g_{m1} V_{\pi 1} (r_{o1} \parallel R_C \parallel R_{i2})$$

$$R_{i2} = R_B \parallel R_{ib2}$$

$$R_{ib2} = (R_E \parallel r_{o2})(\beta_2 + 1) + r_{\pi 2}$$

$$V_s = V_{\pi 1}$$

$$A_{V1} = \frac{V_{o1}}{V_s} = -g_{m1} \bar{R}_L$$

$$\bar{R}_L = R_C \parallel r_{o1} \parallel R_{in2}$$

$$\Rightarrow V_A = \frac{V_o}{V_s} = \underbrace{-g_{m1} \bar{R}_L}_{A_{V1}} \underbrace{\frac{(\beta_2 + 1)(R_E \parallel r_{o2})}{r_{\pi 2} + (\beta_2 + 1)(R_E \parallel r_{o2})}}_{A_{V2}}$$

$$\therefore A_{V1} > 1 \Rightarrow A_V > 1, \phi = 180^\circ$$

$$\approx -150$$

$$* A_I = \frac{I_o}{I_s}$$

$$A_I = \frac{\frac{V_o}{R_E}}{\frac{V_s}{R_{in}}} \Rightarrow A_I = \frac{V_o}{V_s} \cdot \frac{R_{in}}{R_E} \quad \overset{A_V}{\approx}$$



$$* A_I = \frac{I_o}{I_s} = \frac{I_o}{I_{b2}} \cdot \frac{I_{b2}}{I_{b1}} \cdot \frac{I_{b1}}{I_s} \rightarrow X \quad \text{قادر، قابل}$$

$$A_i = A_v \frac{R_{in}}{R_E}, \quad R_{in} = r_{\pi 1} \parallel R_{th} = 1.118 = 0.9k$$

$$A_i = \frac{-150 \cdot 0.9}{1k} = -135$$

* AV & AI Relations.

① AI in terms of AV

$$A_i = \frac{I_o}{I_s} = \frac{\frac{V_o}{R_L}}{V_s} = A_v \cdot \frac{R_{in}}{R_L}$$

$\frac{V_s}{R_{in} + R_s}$ is source current I_s \rightarrow $\frac{V_o}{R_L}$ is load current I_o

② AV in terms

$$A_v = \frac{V_o}{V_s} = \frac{I_o}{I_s} \cdot \frac{R_L}{R_{in} + R_s}$$

\rightarrow $\frac{I_o}{I_s}$ is current gain A_i \rightarrow $\frac{R_L}{R_{in} + R_s}$ is voltage division factor

* $R_o = \frac{V_x}{I_x} \Big|_{V_s=0}$

$$R_o = (r_{o1} \parallel R_C \parallel R_B) + r_{\pi 2} \parallel r_{o2} \parallel R_{E2}$$

$\frac{R_{E2}}{\beta + 1}$ is thevenin resistance \rightarrow Invt. P.R

* $g_m r_{\pi 1} = 0 \Rightarrow V_{\pi 1} = 0$ \rightarrow $V_{\pi 1} = 0$ \rightarrow $400 \cdot C$

load \rightarrow $\frac{R_{E2}}{\beta + 1}$ is thevenin resistance

is thevenin resistance of the circuit

Very high current Gain ckt.



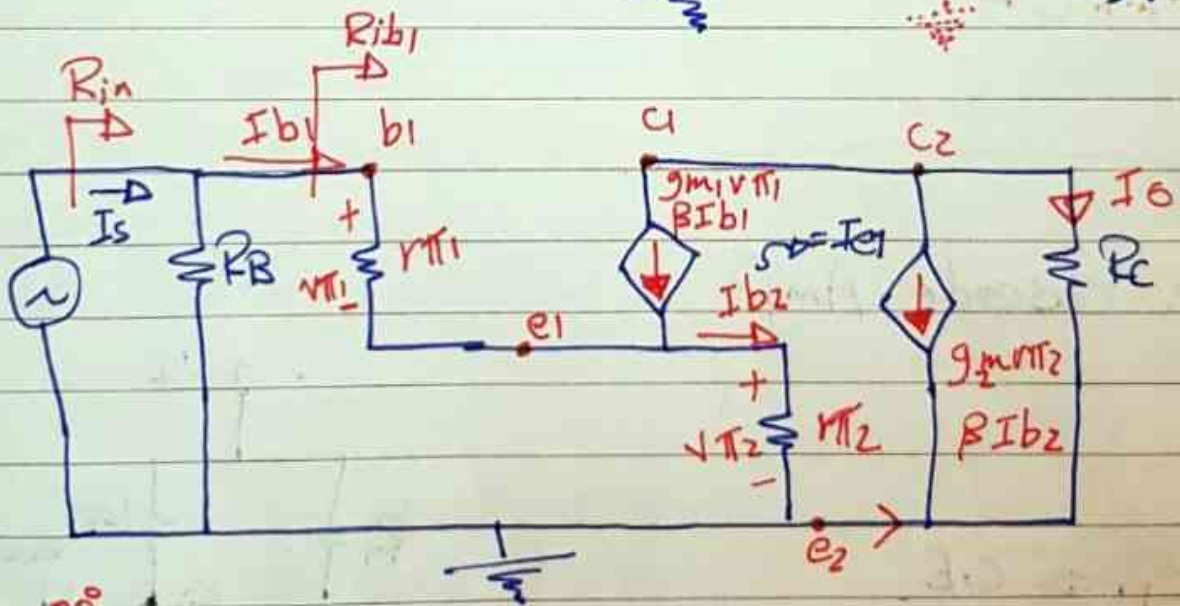
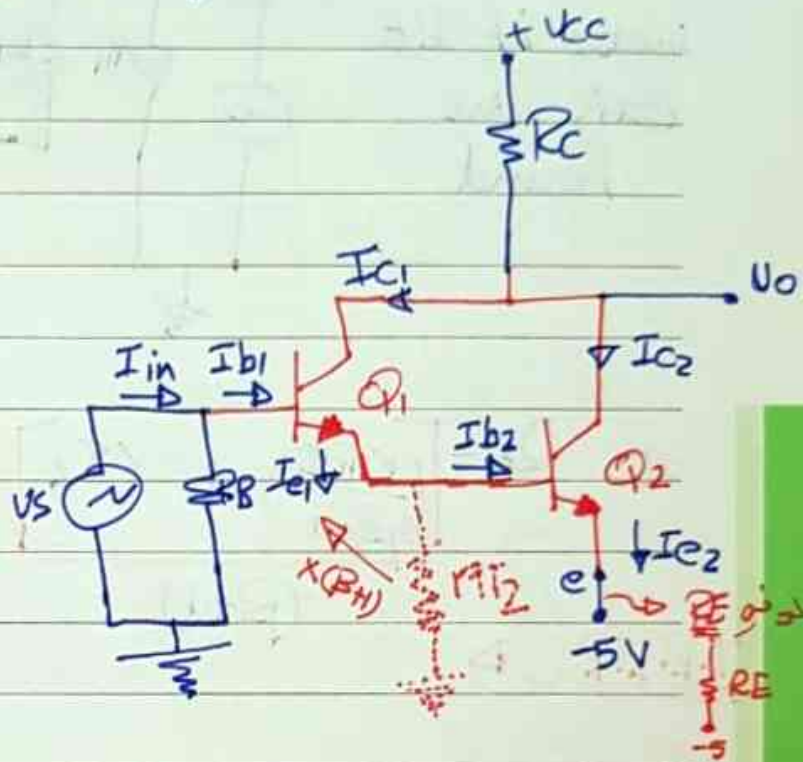
37

Cascade :- Darlington Pair configuration.

$$I_{b1} \approx I_{in}$$

$R_B \Rightarrow$ very big.

$$AI = \frac{I_o}{I_i} \approx \frac{I_o}{I_{b1}}$$



$$\Rightarrow I_o = \ominus \beta I_{b2} = \beta I_{e1} = \beta (\beta + 1) I_{b1} = (\beta^2 + \beta) I_{b1}$$

$$\therefore AI \approx \frac{I_o}{I_{b1}} \approx \beta^2 + \beta \approx \ominus \beta^2$$

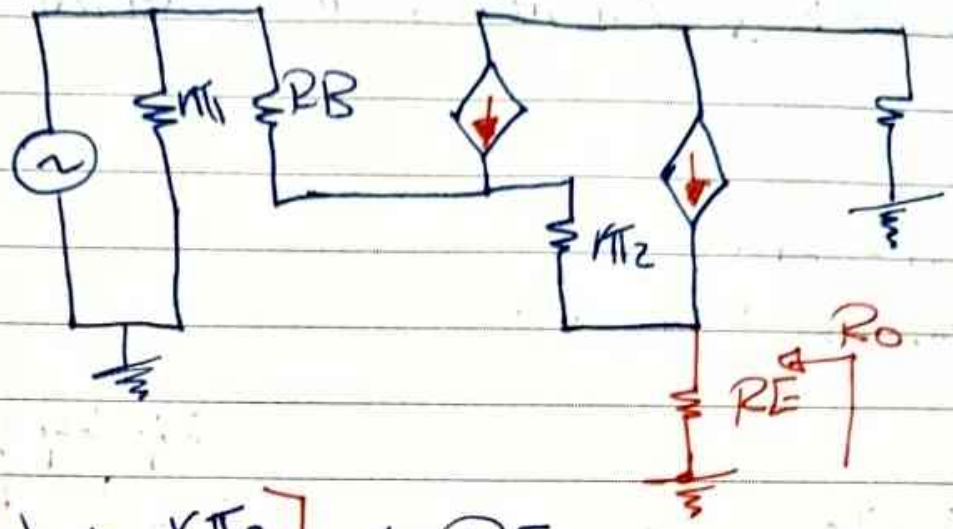
$$\Rightarrow R_{in} = R_B \parallel R_{ib1}$$

$$R_{ib1} = r_{\pi 2} (\beta + 1) + r_{\pi 1}$$

$\sim \sim \sim$ $\sim \sim \sim$

* $R_o = ?? \Rightarrow R_o = R_c$

incase if R_E
~~etc~~ was
 found



$$\Rightarrow R_o = \left[\frac{r_{\pi 1}}{\beta + 1} + r_{\pi 2} \right] \parallel R_E$$

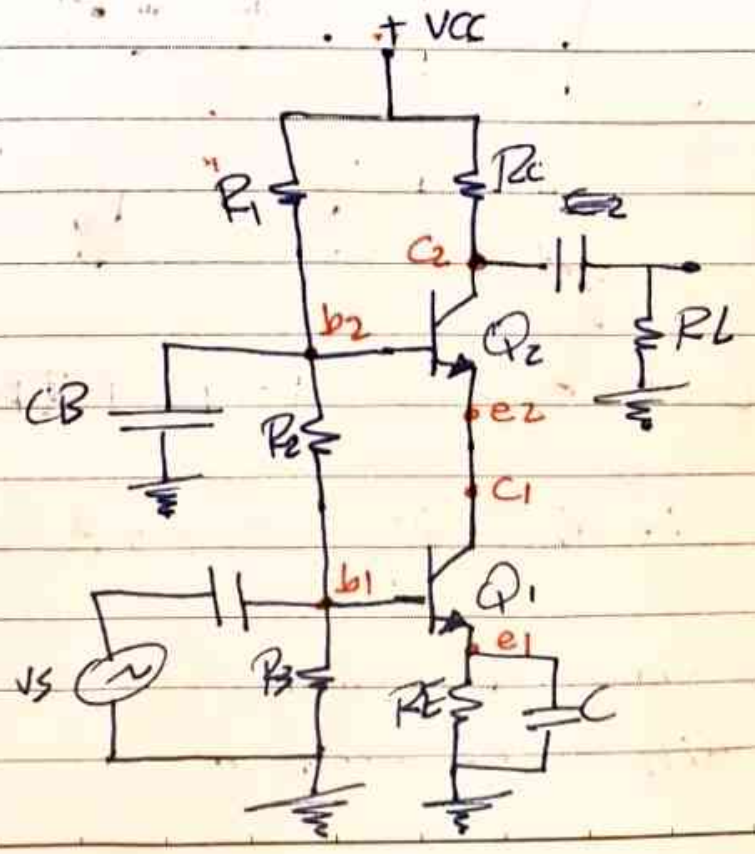
I.R.R.R

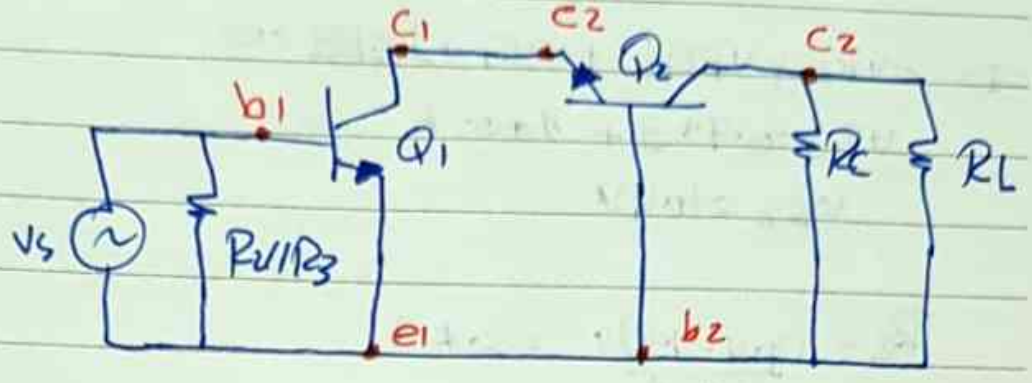
② Cascode Amp

$Q_1 \Rightarrow C.E$

$Q_2 \Rightarrow D.C.B$

* $R_f \Rightarrow D.S.C$ in A.C





Ex: ① Design the cascode ckt shown in Fig :- to have $I_{CQ} = 1\text{mA}$, $V_{CE1} = V_{CE2} = 3\text{V}$

Assume $I_C \approx I_E \rightarrow I_{B \approx I_E} \rightarrow$ *ما بقدر انا Analysis/design انا ما بقدر انا*
السرف واننا ما انا انا انا انا انا انا

choose the biasing current
 $I = 10\%$ of I_C

The BJT has $V_{BE} = 0.7\text{V}$

② Draw s.s.A.C eqn't ckt & find A_V, A_I, R_{in}, R_o

Sol:-

R_C ?

$$-10 + I_C R_C + V_{CE2} + V_{CE1} + I_C R_E = 0$$

$$I_C R_C = 10 - 3 - 3 - 1 * 0.7 = 3.3\text{V}$$

$$R_C = \frac{3.3\text{V}}{1\text{mA}} = 3.3\text{K}\Omega$$

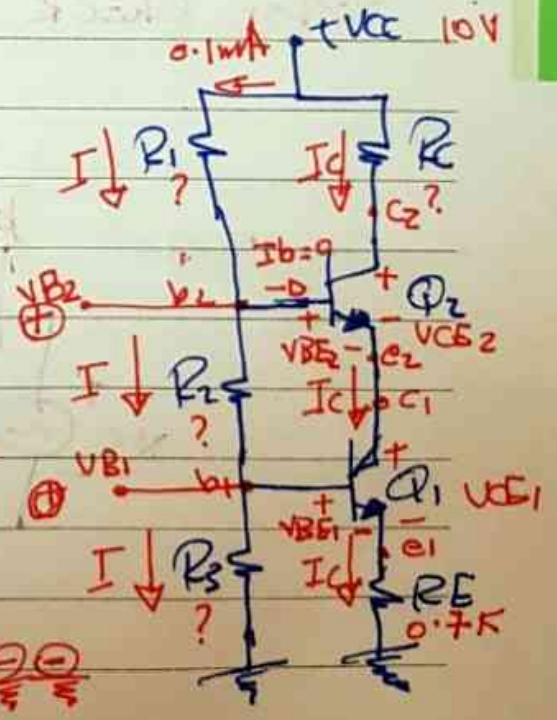
R_1, R_2, R_3 ?

$$R_3 = \frac{V_{B1}}{I}, \quad R_2 = \frac{V_{B2} - V_{B1}}{I}, \quad R_1 = \frac{V_{CC} - V_{B2}}{I}$$

$$-V_{B1} + V_{BE1} + I E R_E = 0$$

$$V_{B1} = 0.7 + 1 * 0.7 = 1.4\text{V}$$

$$R_3 = \frac{1.4\text{V}}{0.1\text{mA}} = 14\text{K}\Omega$$



K_1, K_2, K_3 في المقادير $R_T = \dots$ (بعض ما يرتبط اول والا اذا طرقت التيارات او اذا طرقت التيارات) 40

$$\Rightarrow -V_{B2} + V_{BE2} + V_{CE1} + I_E R_E = 0$$

$$V_{B2} = 0.7 + 3 + 1 * 0.7$$

$$V_{B2} = 4.4V$$

$$R_2 = \frac{(4.4 - 1.4)V}{0.1mA} = 30k\Omega$$

$$R_1 = \frac{10 - 4.4}{0.1} = 56k\Omega$$

$$R_T = 14 + 30 + 56 = 100k$$

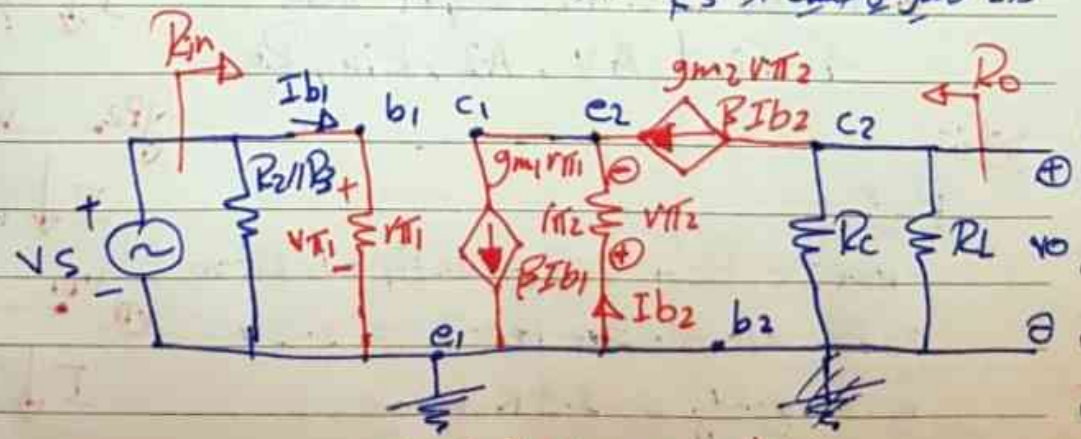
$$R_T = \frac{V_{CC}}{I} = \frac{10V}{0.1} = 100k$$

For check

تغير V_{B1} في R_1 و R_2 تغير R_T

تغير I_E في R_E و $I_E = \frac{V_{CC} + 2}{R_T}$

تغير R_T في R_1 و R_2



S.S. A.C eq. cct.

$$A_V = \frac{V_o}{V_s} = \frac{V_o}{V_{T2}} \cdot \frac{V_{T2}}{V_{T1}} \cdot \frac{V_{T1}}{V_s}$$

$$V_o = -g_{m2} V_{T2} (R_C || R_L)$$

$$\frac{V_o}{V_{T2}} = -g_{m2} (R_C || R_L)$$

→

* KCL at node Q₁

$$g_{m2} v_{\pi 2} + \frac{v_{\pi 2}}{r_{\pi 2}} = g_{m1} v_{\pi 1}$$

$$v_{\pi 2} \left(g_{m2} + \frac{1}{r_{\pi 2}} \right) = g_{m1} v_{\pi 1}$$

$$v_{\pi 2} \left(\frac{\beta_2 + 1}{r_{\pi 2}} \right) = g_{m1} v_{\pi 1}$$

$$\frac{v_{\pi 2}}{v_{\pi 1}} = \frac{r_{\pi 2}}{\beta_2 + 1} g_{m1} \Rightarrow \frac{v_{\pi 1}}{v_s} = 1$$

$$\therefore A_v = -g_{m2} (R_C \parallel R_L) \left(\frac{r_{\pi 2}}{\beta_2 + 1} \right) g_{m1}$$

$$= -g_{m1} (R_C \parallel R_L) \frac{\beta_2}{\beta_2 + 1} = \boxed{-g_{m1} (R_C \parallel R_L)}$$

* A_v of cascode \approx A_v for CE Amp because Q₂ is c.B which Does Not Amplify the current.

$$* AI = \frac{I_o}{I_s} = \frac{\frac{v_o}{R_L}}{\frac{v_s}{R_{in}}} = A_v \frac{R_{in}}{R_L}$$

* $R_{in} = r_{\pi 1} \parallel R_2 \parallel R_3$

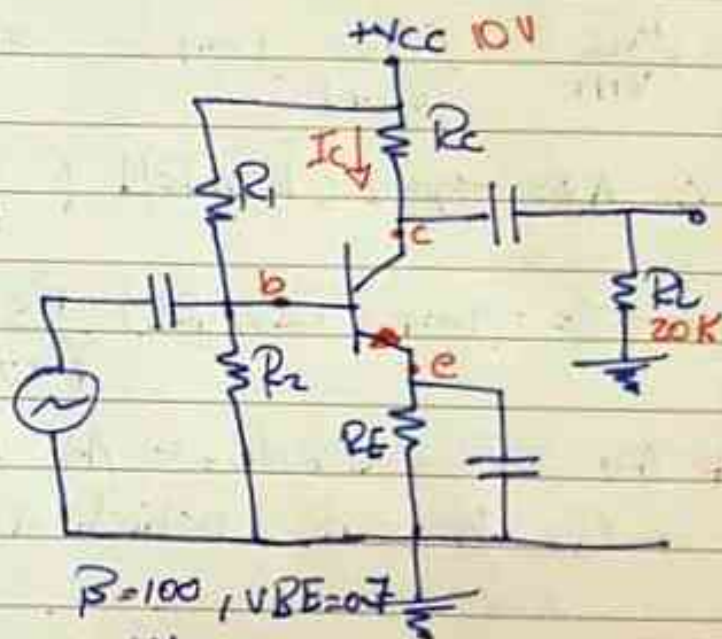
* $R_o = R_c$

$\rightarrow V_S = 0 \rightarrow V_{T1} = 0 \rightarrow V_{T2} = 0 \rightarrow g_{m2} = 0$

Ex:- Design the cct shown to have $I_{CQ} = 1\text{mA}$
 $V_{CEQ} = 4\text{V}$, $A_V = -155$
 & its biase-stable

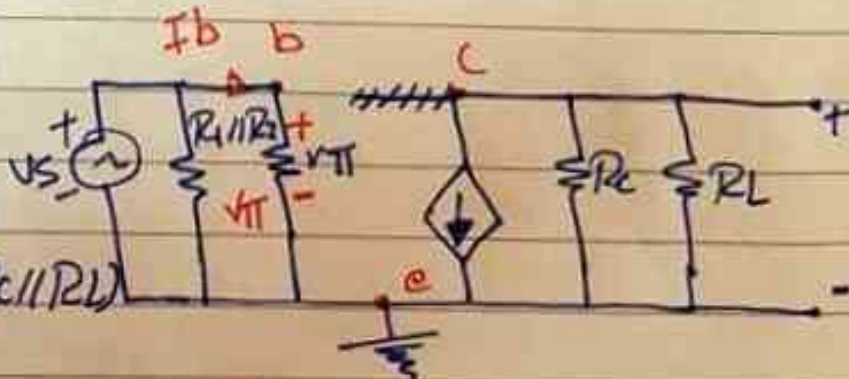
Determine:-

- 1) * R_c, R_E, R_1, R_2
- 2) Draw s.s. & a.c eq ckt & find A_V, R_{in}, R_o .
- 3) write D.C & A.C.L.L & find their slopes.



Soln:-

$V_o = -g_m V_{T1} (R_c \parallel R_L)$



$V_T = V_S \Rightarrow \frac{V_o}{V_S} = -g_m (R_c \parallel R_L)$

$g_m = \frac{I_{CQ}}{V_T} = \frac{1}{26\text{mV}} = 38.5 \frac{\text{mA}}{\text{V}}$

$-155 = -38.5 (R_c \parallel R_L)$

RL Given

R_c) A_V) g_m)
 R_E) $D.C$) g_m)

$$(R_C // R_L) = \frac{155}{38.5} = 4 \text{ k}\Omega$$

$$4 \text{ k}\Omega = R_C // 20 \text{ k}\Omega$$

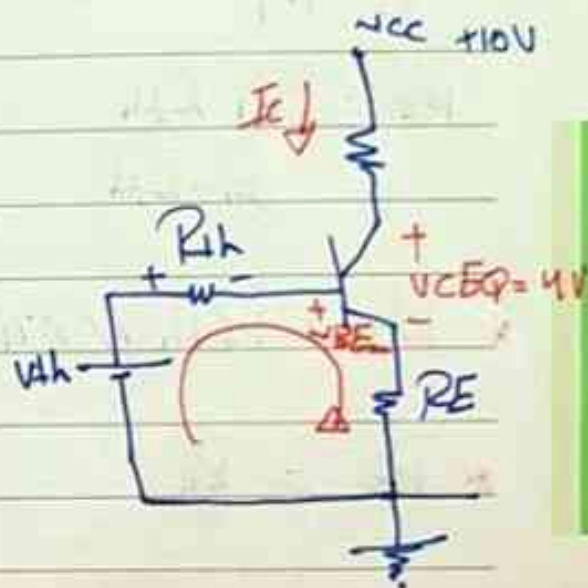
$$R_C = 5 \text{ k}\Omega$$

* From DC *

$$-10 + I_C R_C + V_{CE} + I_E R_E = 0$$

$$R_E = \frac{10 - 5 \times 1 - 4}{I_E} \approx 1 \text{ k}\Omega$$

(for $I_E \approx I_C$)



* for bias-stable design

$$R_{th} = 0.1 (\beta + 1) R_E$$

$$= 0.1 * 101 * 1 = 10.1 \text{ k}\Omega$$

$$R_{th} = R_1 // R_2$$

$$R_1 V_{th} = V_{cc} \frac{R_2 \cdot R_1}{R_1 + R_2}$$

(multiply both sides by R_1)

$$R_1 V_{th} = V_{cc} \cdot R_{th}$$

$$R_1 = \frac{V_{cc}}{V_{th}} \cdot R_{th}$$

$$\Rightarrow -V_{th} + I_B R_{th} + V_{BE} + I_E R_E = 0$$



$$V_{th} = \frac{I_{CQ}}{\beta} (10.1) + 0.7 + \frac{\beta+1}{\beta} I_{CQ} * 1$$

$$= 0.01 * 10.1 + 0.7 + 1.1 = 1.9V$$

$$R_1 = \frac{10}{1.9} * 10.1 = 52 k\Omega$$

$$R_2 = \frac{R_1 R_{th}}{R_1 - R_{th}} = \frac{52 * 10.1}{52 - 10.1} = \frac{520 k}{42} = 125 k\Omega$$

* $R_{in} = R_{th} // r_{\pi}$

* $R_o = R_c$

* $A_V = A_{V_{mid}} \cdot \frac{R_{in}}{R_L}$

* D.C.L.L

$$-V_{CC} + I_C R_c + V_{CE} + I_E R_E = 0$$

$$\frac{\beta+1}{\beta} I_C$$

$$V_{CE} = V_{CC} - I_C \left(R_c + \frac{\beta R_E}{\beta+1} \right)$$

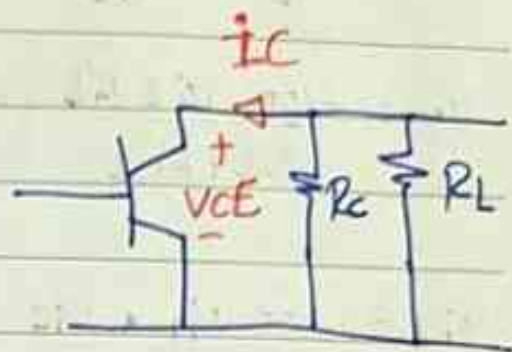
||
 $= \Rightarrow I_C \approx I_E$

$$V_{CE} = V_{CC} - I_C (R_c + R_E)$$

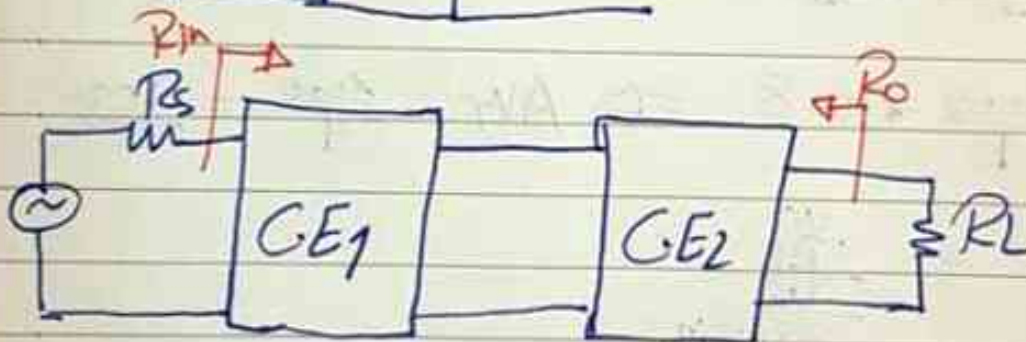
* Ac.LL

$$v_{ce} + i_c (R_c // R_L) = 0$$

$$v_{ce} = -i_c (R_c // R_L)$$

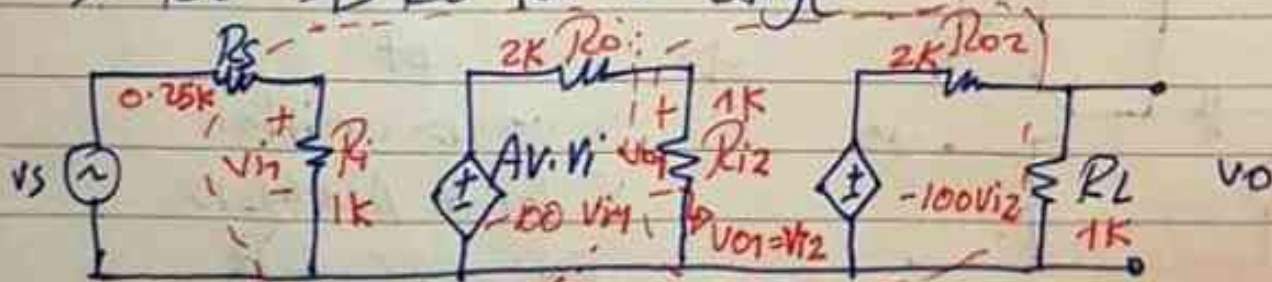


* Any voltage Amp can be represented by



* Find overall AV, over ALL A_I, over all R_i
overall R_o

overall R_{in} ⇒ R_{in} for 1st stage
 ⇒ R_o ⇒ R_o for 2nd stage



$R_i = 1k\Omega, R_o = 2k, AV = 100$



Ideal (قريب من المثالي) R_s (مقاومة المصدر)

$R_{i1} \uparrow, R_{o1} \downarrow \Rightarrow$ Ideal (قريب من المثالي) \rightarrow Trans (نقل) $\left\{ \begin{array}{l} \text{Ideal??} \\ \rightarrow AV_T = AV_1 \cdot AV_2 \end{array} \right.$
Direct

* $AV_T = \frac{V_o}{V_s} = \frac{V_{o2}}{V_{i2}} * \frac{V_{i2}}{V_{i1}} * \frac{V_{i1}}{V_s}$

$V_{o2} = \frac{-100 V_{i2} R_L}{R_L + R_{o2}} \Rightarrow \frac{V_{o2}}{V_{i2}} = \frac{-100 * 1}{1+2} = \frac{-100}{3}$ ✓

$V_{i2} = \frac{100 V_{i1} * R_{i2}}{R_{i2} + R_{o1}} \Rightarrow \frac{V_{i2}}{V_{i1}} = \frac{-100 * 1}{2+1} = \frac{100}{3}$ ✓

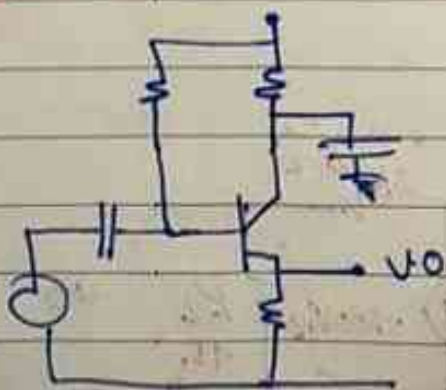
$V_{i1} = \frac{V_s * R_{i1}}{R_{i1} + R_s} = \frac{V_{i1}}{1+0.25} = 0.8$

$AV_T = \left(\frac{-100}{3}\right) * \left(\frac{100}{3}\right) * 0.8$

$= \frac{10000}{9} * 0.8 \Rightarrow AV_T = \frac{8000}{9} = \underline{900}$

* $AI = \frac{I_o}{I_s} = \frac{\frac{V_o}{R_L}}{\frac{V_s}{R_s + R_{i1}}}$

$= AV * \frac{R_s + R_{i1}}{R_L} = 1125$



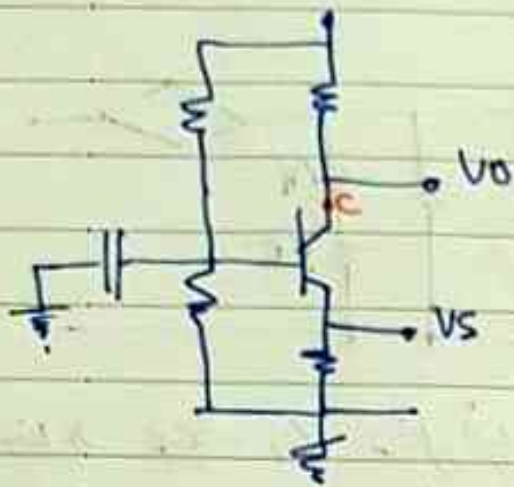
\Rightarrow C.E. cct

① $V_o \Rightarrow$ emitter

② for AC Analysis

cap \Rightarrow D.C. \Rightarrow ∞

47

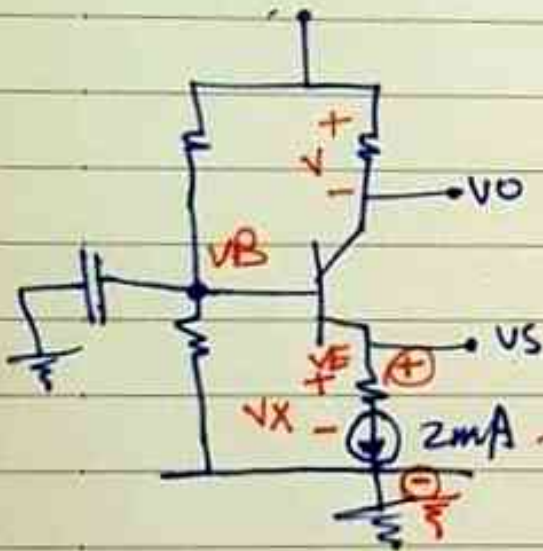


\Rightarrow C.B cct

① $V_O \Rightarrow$ collector

② for AC Analysis

cap = DS.C \Rightarrow B \Rightarrow Gnd

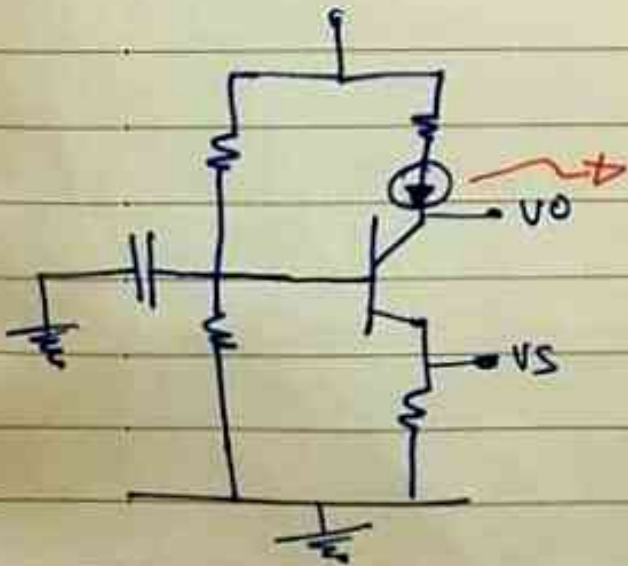


~~VX~~ C.B

* $V_E = V_B - V_{BE}$

for $V_X = -V_{CC} + I_C R_C + V_{CE} + V_X - 5 =$

$2mA \Rightarrow I_E = 2mA$



I_C

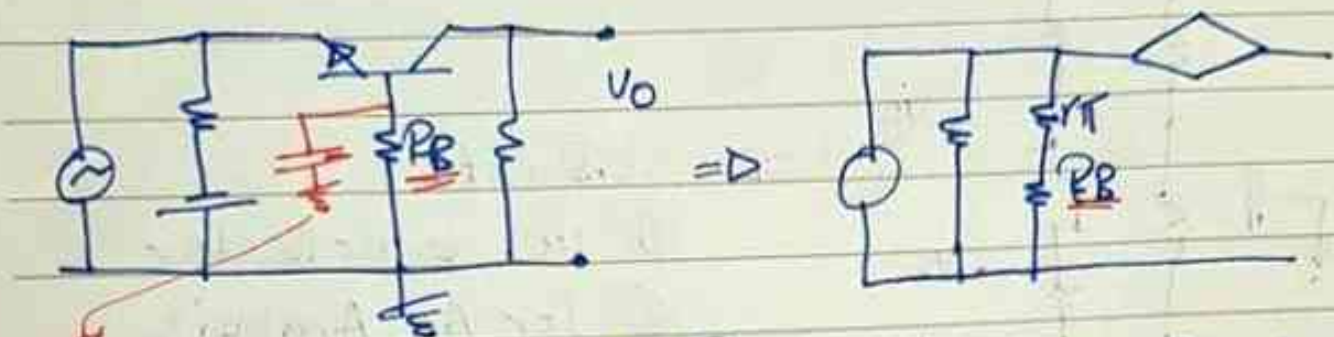
C.B

- Q₁ => design for single stage
 - Q₂ => multistage
 - Q₃ => multiple choice
- 5 concept 15 calculation

* write Dc & Ac & their slopes

48

لو هوز ايشه ايه تا ايه
ب اكتب ايشه تا ايه



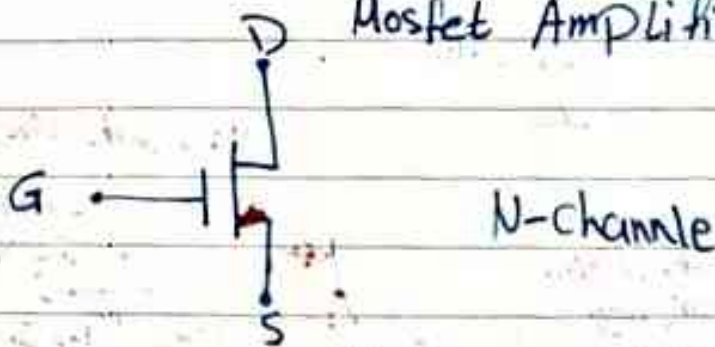
AC & DC analysis
 * when AC is applied, the capacitor acts as a short circuit.
 * when DC is applied, the capacitor acts as an open circuit.

اصغر من ار BJT با كج
 ار noise الليضو اقل من ار BJT (ار β) مفصول عن ار β

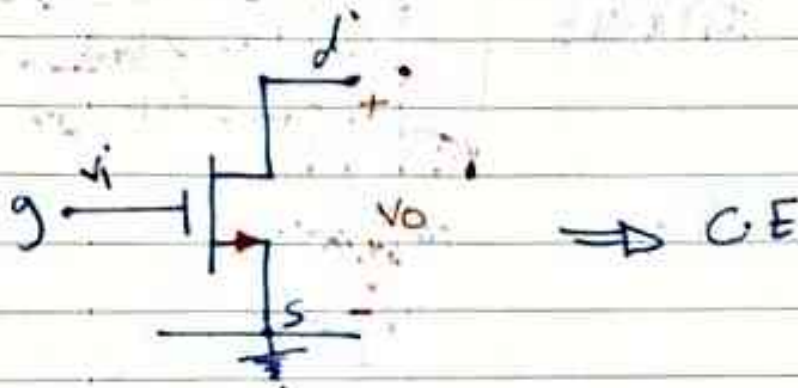
49

Ch XII

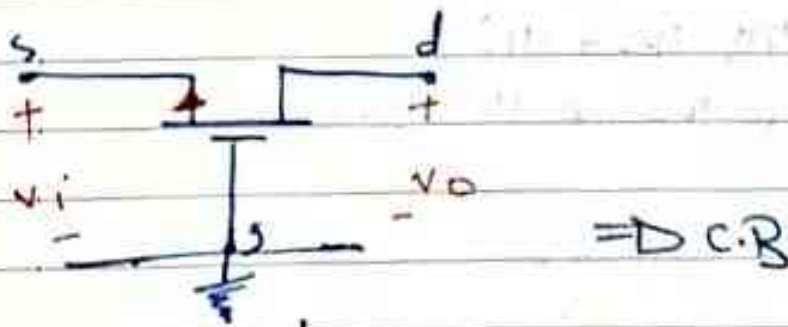
Mosfet Amplifiers.



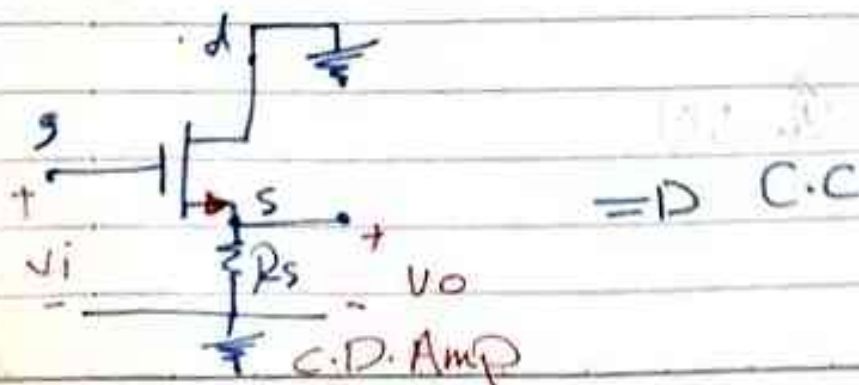
N-channel



C.S. Amp



C.G. Amp



C.D. Amp

* Mosfet must be biased in saturation Region to be used as an Amp.

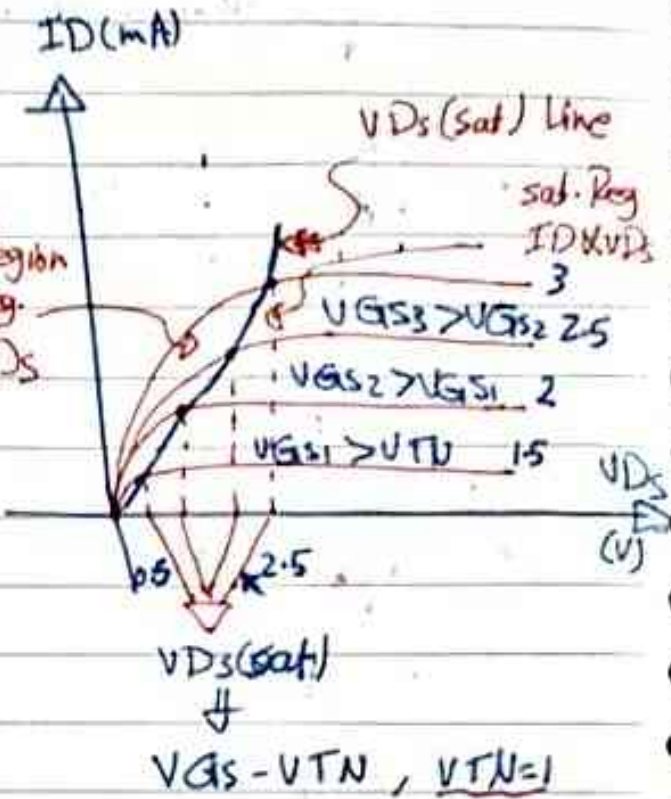
⊕ saturation Region

$$I_D = K_n (V_{GS} - V_{TN})^2$$

$V_{TN} \rightarrow$ Given

$K_n \rightarrow$ Given

non-sat. Region
(Linear) Reg.
 $I_D \propto V_{DS}$



Mosfet is used as an Amp.

⊕ non-sat. Region.
(Linear-Region)

$$I_D = k_n [2(V_{GS} - V_{TN})V_{DS} + V_{DS}^2]$$

for small $V_{DS} \rightarrow V_{DS} \rightarrow$ negligible

$$I_D \approx 2K_n (V_{GS} - V_{TN})V_{DS}$$

$$\frac{V_{DS}}{I_D} = \frac{1}{2K_n (V_{GS} - V_{TN})}$$

$$R_{mos} = \frac{1}{2K_n (V_{GS} - V_{TN})}$$

* In Linear Region I can use Mosfet as a Voltage Variable Resistance

* Assume Mosfet in sat

$$I_D = \frac{1}{2} k_n (V_{GS} - V_{TN})^2$$

$$V_{GS} = V_{G1} - V_S = \frac{5 \times 20}{50} - 0 = 2V$$

$$I_D = \frac{1}{2} (2-1)^2 = 1mA$$

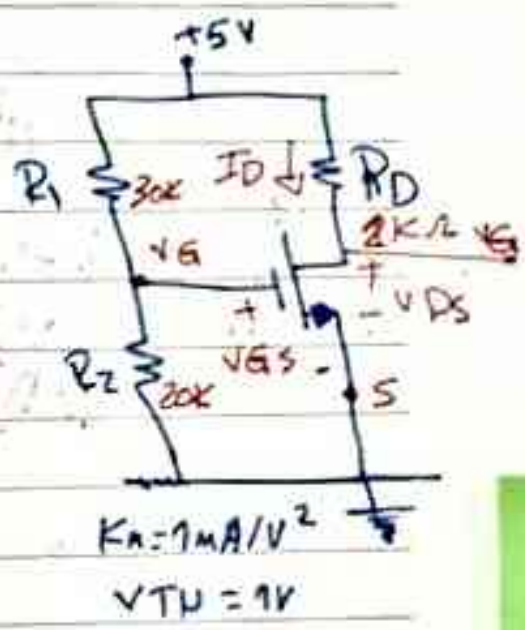
$$-5 + I_D R_D + V_{DS} = 0$$

$$V_{DS} = 5 - 2 \times 1 = 3V$$

$$V_{DS}(\text{sat}) = V_{GS} - V_{TN} = 2 - 1 = 1V$$

since $V_{DS} > V_{DS}(\text{sat})$

∴ Mosfet in sat

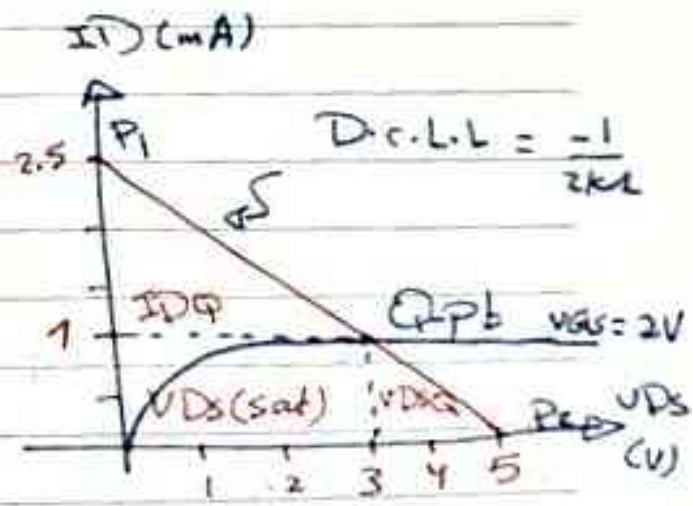


* D.C.L.L

$$-5 + I_D R_D + V_{DS} = 0$$

$$V_{DS} = 5 - I_D R_D$$

$$\text{slope} = \frac{-1}{R_D}$$



$$D.C.L.L = \frac{-1}{2k\Omega}$$

(I) for $I_D = 0$, $V_{DS} = 5V$

$P_1 (5V, 0mA)$

(II) for $V_{DS} = 0$, $I_D = \frac{5}{2} = 2.5mA$

$P_2 (0V, 2.5mA)$

$Q = P_E$, $I_{DQ} = 1mA$, $V_{DSQ} = 3V$

$V_{GSQ} = 2V$
 $V_{DS}(\text{sat}) = 1V$

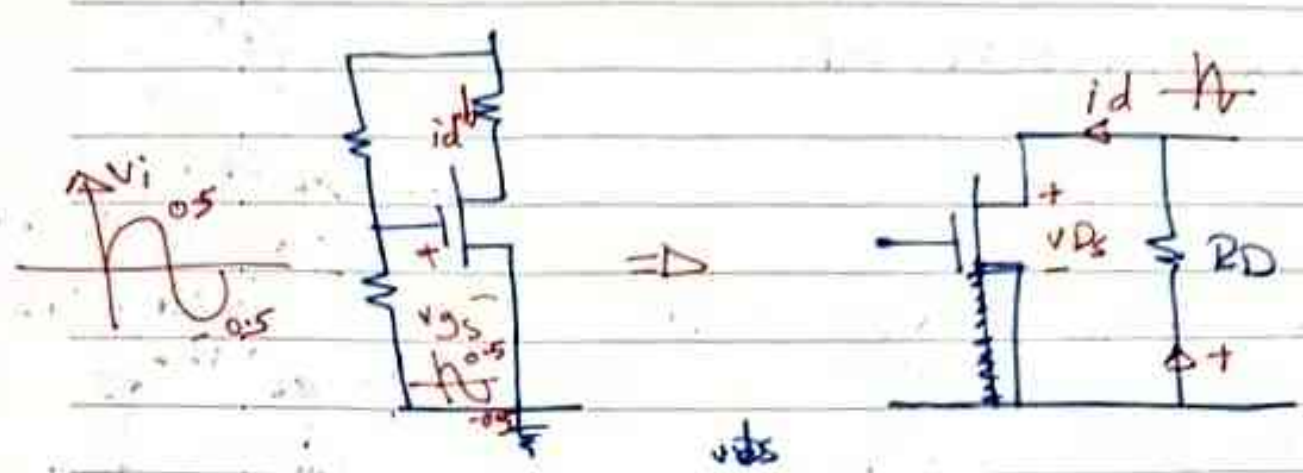


$V_i \Rightarrow V_{GS} \Rightarrow I_D \Rightarrow V_{DS}$ (AC) \Rightarrow voltage controlled device (MOSFET)

$I_G = 0$

$I_G = 0$

52



$V_{DS} = -i_D R_D \Rightarrow$ $A_V = \frac{V_{DS}}{V_i}$

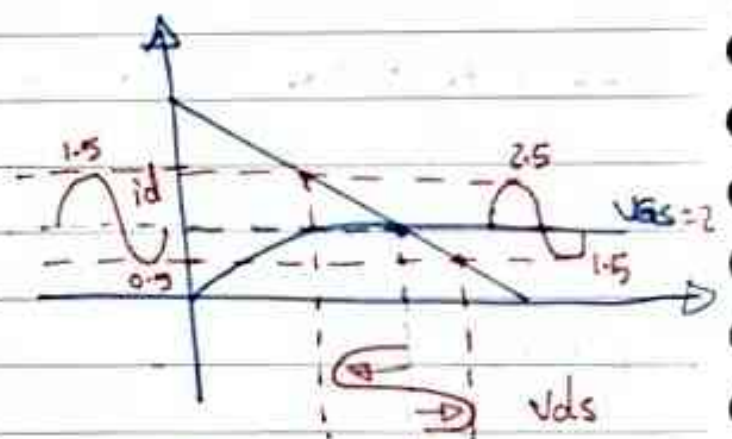
* According to superposition

$i_D = I_{DQ} + i_d$

$V_{GS} = V_{GSQ} + v_{gs}$

total Res. DC AC

$V_{DS} = V_{DSQ} + v_{ds}$

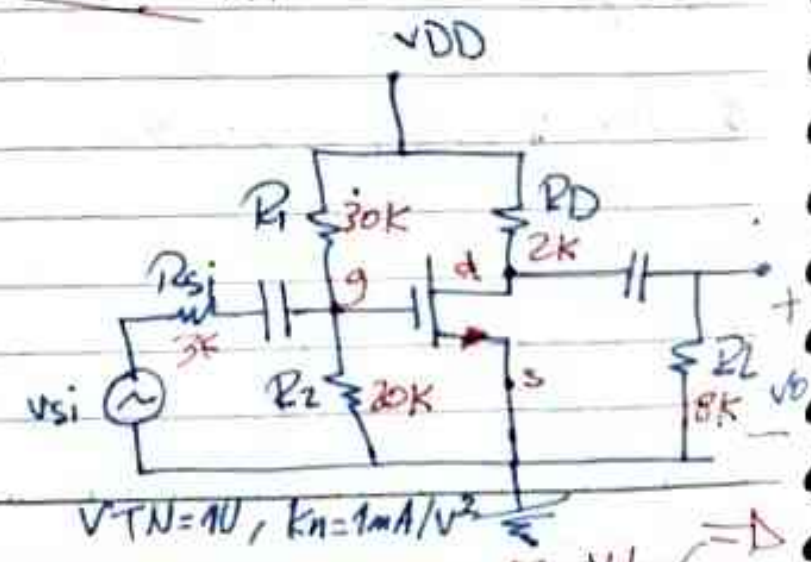


$I_D = k_n (V_{GS} - V_{TN})^2$

① common-source Amp

① Basic C.S

$V_i \rightarrow$ gate
 V_o from drain
 $s \rightarrow$ common terminal



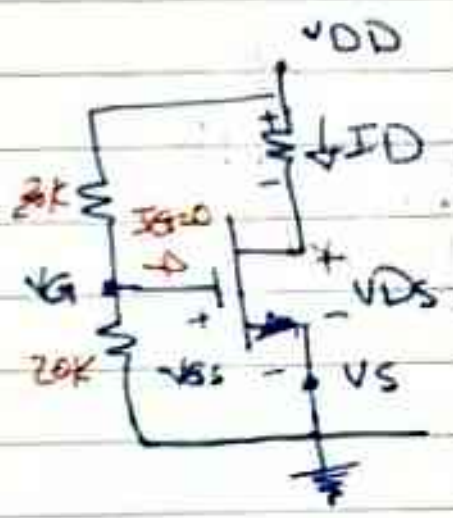
Common Source = Common Emitter \Rightarrow

- 1) - Determine I_{DQ}
 V_{DSQ}
- 2) - Draw s.s. A.c eq ckt
& Find A_v , R_{in} & R_o

Sol:

① D.c Analysis

Assume the Mosfet
in sat Region



$$I_D = k_n (V_{GS} - V_{TN})^2$$

$$V_{GS} = V_G - V_S$$

$$= \frac{V_{DD} \cdot R_2}{R_1 + R_2} - 0 = \frac{5 \times 20}{30} = 2V$$

$$I_D = 1(2-1)^2 = 1mA$$

$$-V_{DD} + I_D R_D + V_{DS} = 0$$

$$V_{DS} = 5 - 1 \times 2 = 3V$$

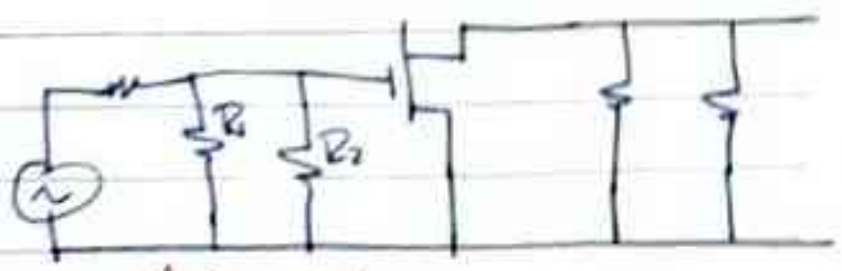
$$V_{DS(sat)} = V_{GS} - V_{TN}$$

$$= 2 - 1 = 1V$$

\Rightarrow Since $V_{DS} > V_{DS(sat)}$
 \therefore Mosfet in sat Reg.

② A.c Analysis

c - D.S.C, D.C - D.S.C

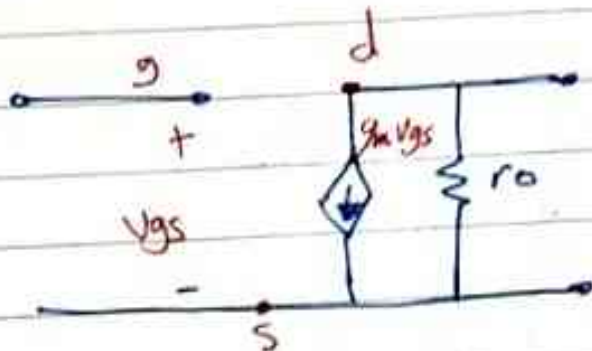
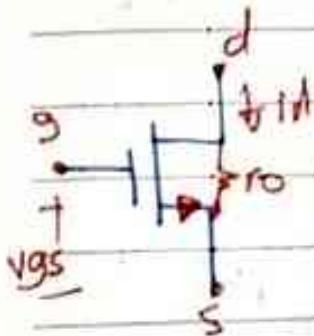
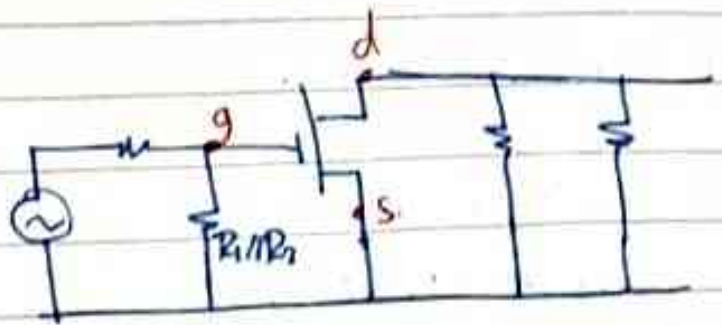


AC. ckt.

\Rightarrow

- * $\lambda = 0 \Rightarrow r_o = \infty$
- * $\lambda = \text{value} \Rightarrow r_o = \text{value}$

54



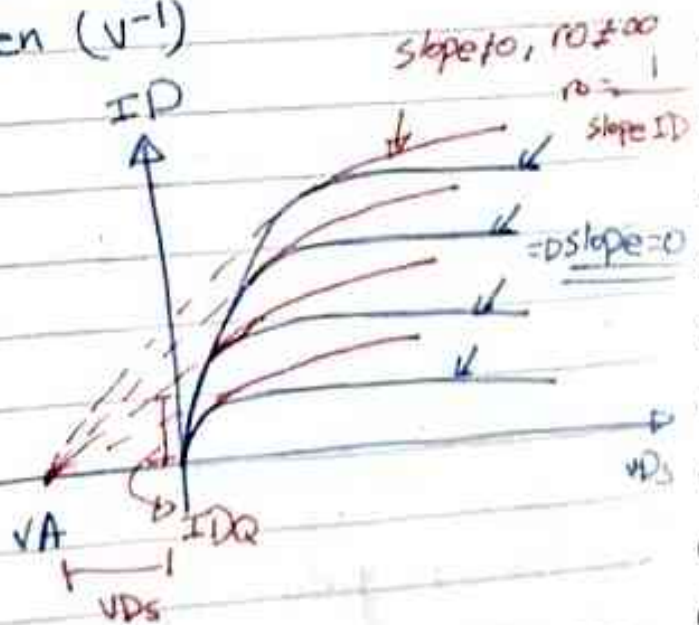
$$r_o = \frac{1}{\lambda I_{DQ}} \quad (\text{MOSFET drain-source Resistance})$$

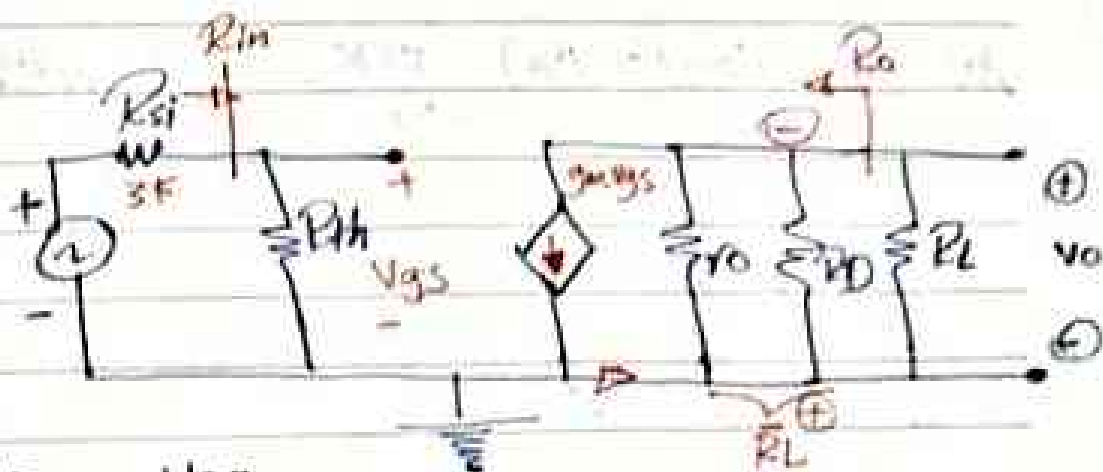
λ : channel length modulation parameter given (V^{-1})

$$\text{slope} = \frac{\Delta I_D}{\Delta V_{DS}}$$

$$\text{slope} = \frac{I_{DQ}}{V_A}$$

$$r_o = \frac{V_A}{I_{DQ}} = \frac{1}{I_{DQ} \lambda}$$





$$A_V = \frac{v_o}{v_{si}} = \frac{v_o}{v_{gs}} \cdot \frac{v_{gs}}{v_{si}}$$

$$v_o = -g_m v_{gs} \bar{R}_L$$

$$\bar{R}_L = v_o / i_D \parallel R_L$$

$$k_n = 1 \text{ mA/V}^2$$

$$V_{TN} = 1 \text{ V}, \lambda = 0.02 \text{ V}^{-1}$$

$$\frac{v_o}{v_{gs}} = -g_m \bar{R}_L, \quad v_{gs} = \frac{v_{si} \cdot R_{th}}{R_{th} + R_{si}}$$

$$\frac{v_{gs}}{v_{si}} = \frac{R_{th}}{R_{th} + R_{si}}$$

$$A_V = -g_m \bar{R}_L \frac{R_{th}}{R_{th} + R_{si}}$$

⊖ means 180° phase shift between v_{si} & v_o (only in CS)

$$g_m = \frac{\partial I_D}{\partial V_{GS}} = \frac{\partial (k_n (V_{GS} - V_{TN})^2)}{\partial V_{GS}}$$

$$g_m = 2k_n (V_{GS} - V_{TN}) \checkmark$$

$$\text{OR } g_m = 2\sqrt{k_n \cdot I_D} \checkmark$$

$$= 2\sqrt{1 \cdot 1} \Rightarrow I_D g_m = \frac{2 \text{ mA}}{1 \text{ V}}$$

$$v_o = \frac{1}{\lambda I_D} = \frac{1}{0.02 \cdot 1 \cdot 10^{-3}} = \underline{\underline{50 \text{ kV}}} \Rightarrow$$

$$A_V = -2 \left(\frac{50 \parallel 2 \parallel 8}{12+3} \right) \frac{12K}{12+3} = -2 \times 1.5 \times 0.8$$

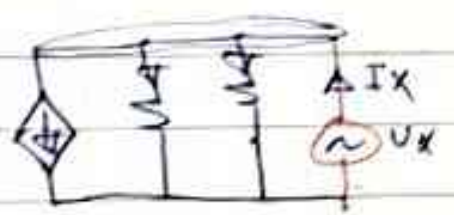
$$\Rightarrow A_V = -2.4$$

$$V_o = -2.4 V_{si}$$

$$* R_{in} = R_{th} = 12K\Omega$$

$$* R_o = ??$$

$$R_o = \frac{V_x}{I_x} \Big|_{V_{si} = 0}$$



KCL at node d

$$I_x = \frac{V_x}{R_D} + \frac{V_x}{r_o} + g_m V_{gs}$$

$$\frac{V_x}{I_x} = R_o = r_o \parallel R_D$$

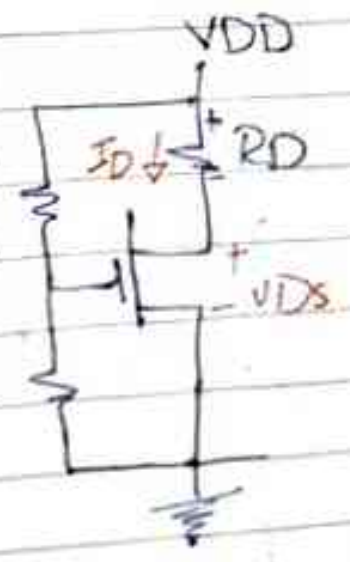
$$R_o = 50K \parallel 2K = 1.85K\Omega$$

③ Draw D.C & A.C LL & find their slopes.

$$-V_{DD} + I_D R_D + V_{DS} = 0$$

$$V_{DS} = V_{DD} - I_D R_D \text{ , D.C.LL}$$

$$\text{slope} = \frac{-1}{R_D} = \frac{-1}{2K}$$



* $P_1 \Rightarrow$ Cut off Voltage ($I=0$)

$P_2 \Rightarrow$ Saturation Point \sim short ckt ($V_{DS}=0$)

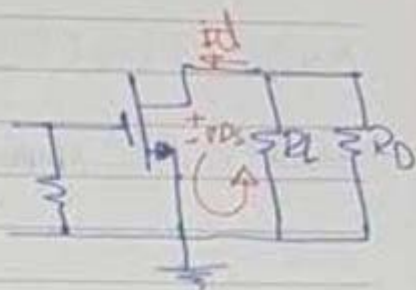
Sub. Reg. \rightarrow \rightarrow

57

$$V_{DS} + i_D(R_D // R_L) = 0$$

$$V_{DS} = -i_D(R_D // R_L) \quad \text{A.C. L.L}$$

$$\text{Slope} = \frac{-1}{R_D // R_L} = \frac{-1}{1.6K}$$



D.C. L.L

From D.C.L.L eq.

(I) For $I_D=0$, $V_{DS} = V_{DD} = 5V$

^{max} + because the current=0

$P_1(5V, 0mA)$

(II) For $V_{DS}=0$, $I_D = \frac{V_{DD}}{R_D} = 2.5mA$

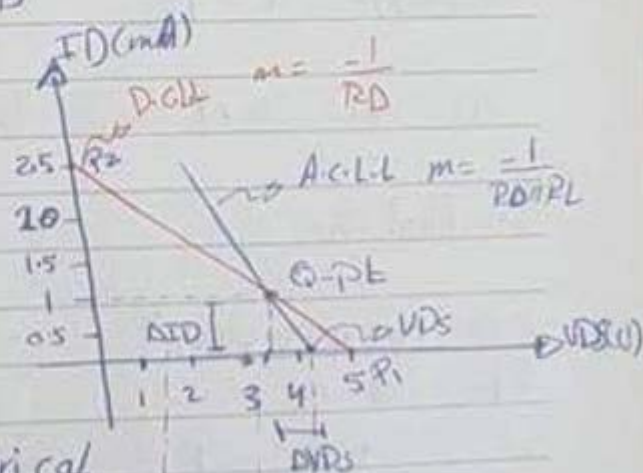
$P_2(0, 2.5mA)$

$$\text{slope} = \frac{1}{(R_D // R_L)} = \frac{\Delta I_D}{\Delta V_{DS}}$$

$$\Delta V_{DS} = \Delta I_D (R_D // R_L)$$

$$\Delta I_D = I_{DQ}$$

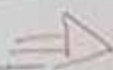
$$\Delta V_{DS} = 1(2/1.6) = 1.6V$$



* ΔV_{DS} :- max peak symmetrical output voltage

\rightarrow max peak voltage

1.4 3 4.6



$$\Delta V_{DS} = \pm I_{DQ} (R_D \parallel R_L)$$

max (P-P) symmetrical o/p voltage = $2I_{DQ} (R_D \parallel R_L)$

II C.S with R_S

for $k_n = 1$

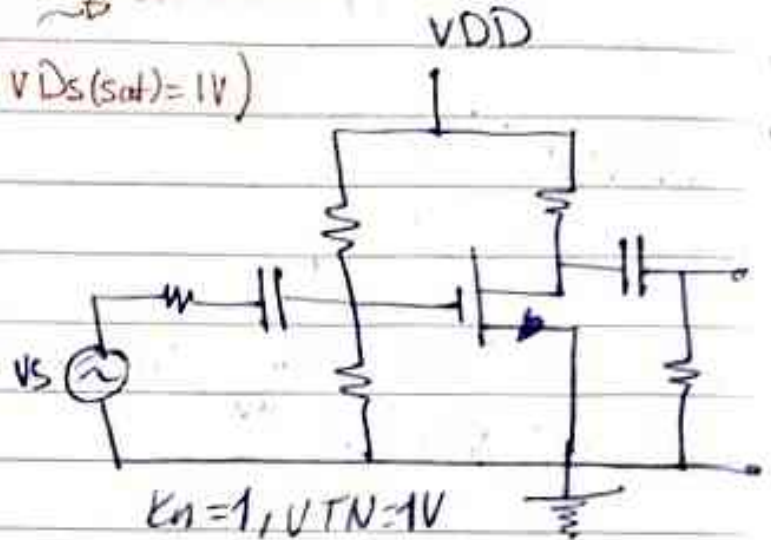
($V_{GS} = 2V, I_D = 1mA, V_{DS} = 3V, V_{DS}(sat) = 1V$)

DC

$$\Rightarrow k_n = 2.5$$

$$V_{GS} = \frac{5 + 20}{50} = 2V \checkmark$$

$$I_D = 2.5(2 - 1)^2 = 2.5 \mu A$$



$$V_{DS} = 5 - 2.5 \times 2 = 0$$

$$V_{DS}(sat) = 2 - 1 = 1V$$

$V_{DS} < V_{DS}(sat) \Rightarrow$ Mosfet in Non-sat

D.C Analysis

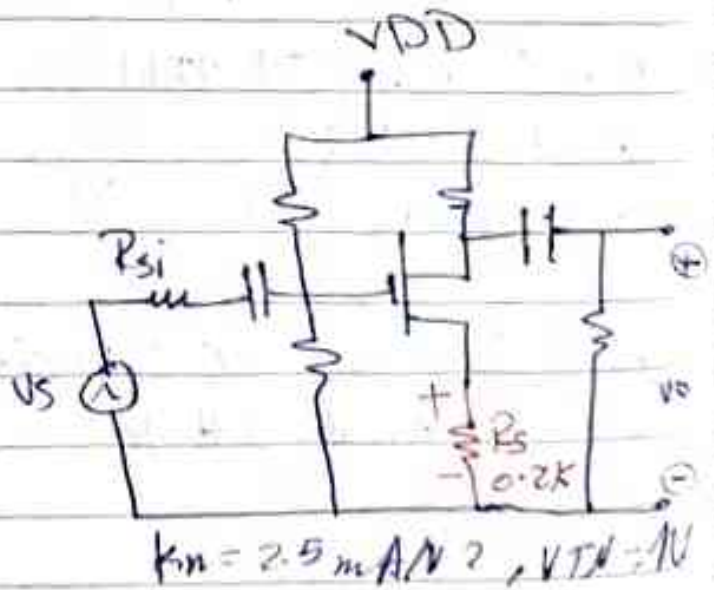
$$I_D = k_n (V_{GS} - V_{TN})^2$$

$$V_{GS} = V_G - V_S$$

$$= \frac{5 + 20}{50} - I_D \cdot R_S$$

$$V_{GS} = 2 - 0.2 I_D$$

$$I_D = \frac{2 - V_{GS}}{0.2}$$



$R_S \Rightarrow$ stabilize QPb against k_n variation \Rightarrow

$$I_D = \frac{2 - V_{GS}}{0.2}$$

$$\frac{2 - V_{GS}}{0.2} = 2.5 (V_{GS} - 1)^2$$

$$2 - V_{GS} = 0.5 (V_{GS}^2 - 2V_{GS} + 1)$$

$$2 - V_{GS} = 0.5 V_{GS}^2 - V_{GS} + 0.5$$

$$1.5 = 0.5 V_{GS}^2$$

$$V_{GS}^2 = 3$$

$$V_{GS} = \pm \sqrt{3} = \pm 1.732 \text{ V}$$

$$I_D = \frac{2 - 1.732 \text{ V}}{0.2} = \frac{0.268}{0.2}$$

$$I_D = 1.35 \text{ mA}$$

$$V_{DS} = V_{DD} - I_D (R_D + R_S)$$

$$= 5 - \frac{1.35 \times 2.2}{3} = \underline{V_{DS} = 2.1 \text{ V}}$$

$$V_{DS}(\text{sat}) = V_{GS} - V_{TN}$$

$$= 1.732 - 1$$

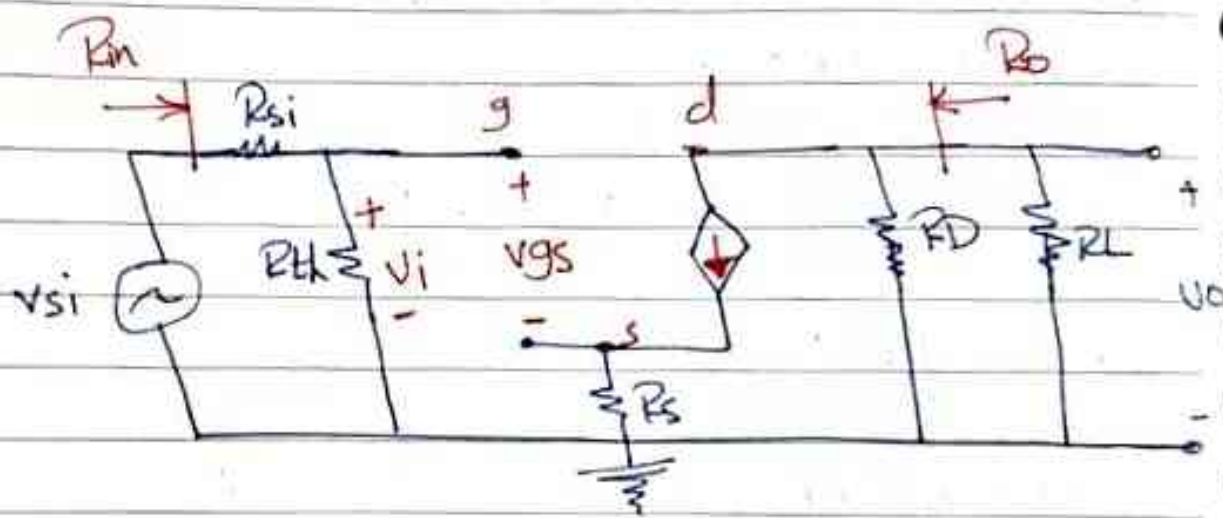
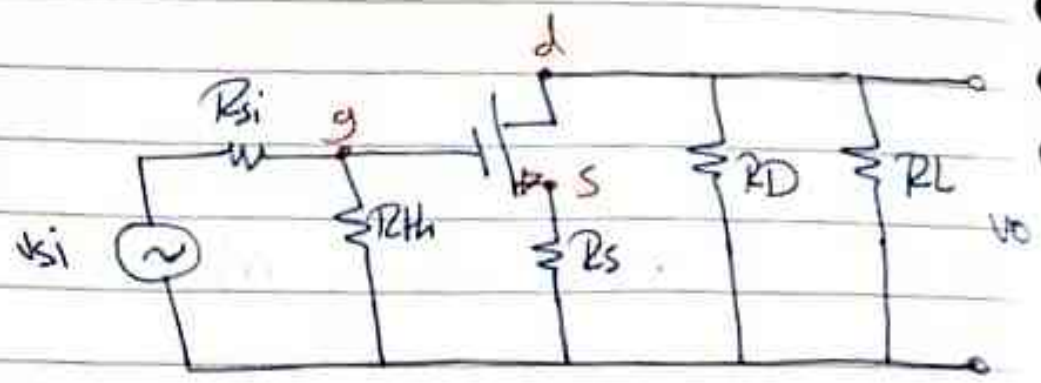
\therefore Mosfet in sat Region.

$$V_{DS}(\text{sat}) = 0.732 \text{ V}$$

* R_S stabilize Q-pt against k_n variation.

* R_S decrease AV (disadvantage)

AC



$$\Rightarrow AV = \frac{v_o}{v_{si}} = \frac{v_o}{v_{gs}} * \frac{v_{gs}}{v_i} * \frac{v_i}{v_{si}}$$

$$v_o = -g_m v_{gs} (R_D // R_L)$$

$$* \frac{v_o}{v_{gs}} = -g_m (R_D // R_L)$$

$$-v_i + v_{gs} + v_s = 0$$

$$v_i = v_{gs} + v_s$$

$$v_i = v_{gs} + g_m v_{gs} * R_s$$

$$\Rightarrow v_i = v_{gs} (1 + g_m R_s)$$



61

$$* \frac{V_i}{V_{gs}} = 1 + g_m R_s \rightarrow \frac{V_{gs}}{V_i} = \frac{1}{1 + g_m R_s} \checkmark$$

$$\Rightarrow \frac{V_i}{V_{si}} = \frac{R_{th}}{R_{th} + R_{si}}$$

* R_s decrease AV (disadv.)

$$AV = \frac{-g_m (R_D \parallel R_U)}{1 + g_m R_s} \therefore \frac{R_{th}}{R_{th} + R_{si}}$$

$$* R_{in} = R_{th}$$

$$* R_o = \frac{V_x}{I_x} \Big|_{V_{si}=0}$$

When $V_{si}=0$, $V_i=0$, $V_{gs}=0$

$g_m V_{gs} = 0$ (D.C source is open)

$$\Rightarrow R_o = R_D$$

* If $R_{th} \gg R_{si}$ & $g_m R_s \gg 1$

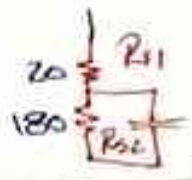
$$\Rightarrow AV \approx - \frac{(R_D \parallel R_U)}{R_s}$$



المزايا والعيوب
 disadvantages, مزايا

$R_S = 200 \Rightarrow$

52

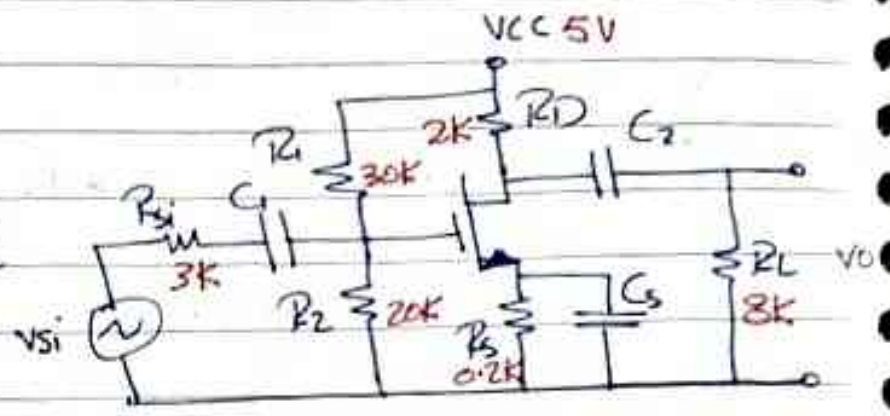


III C.S with bypass capacitor C_S

① D.C Analysis

$R_D, C_S, C_1, C_2 - D.O.C$

* This ckt. is analyzed as a C.S with R_S



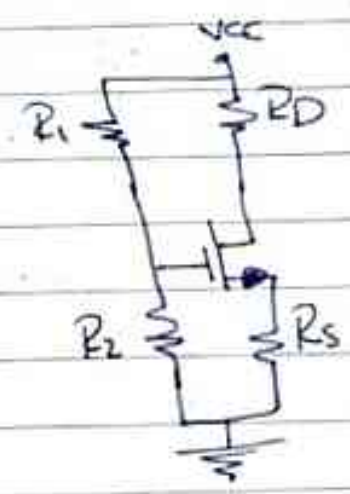
$K_n = 2.5 \text{ mA/V}^2$

$V_{TN} = 1 \text{ V}$

* $V_{GS} = 1.73 \text{ V}$

* $I_D = 1.35 \text{ mA}$

* $V_{DS} = 2.1 \text{ V}$



② A.C Analysis

$C_1, C_2, C_S - C$

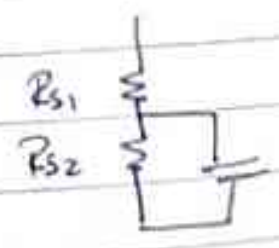
* The ckt behaves as a Basic

* D.C.L.L eqn :-

$-V_{DD} + I_D R_D + V_{DS} + I_D (R_{S1} + R_{S2})$

$V_{DS} = V_{DD} - I_D [(R_{S1} + R_{S2}) + R_D]$

slope = $\frac{-1}{R_{S1} + R_{S2} + R_D}$



* $R_D \rightarrow$ Moderate to high.

* A.C.L.L eqn.

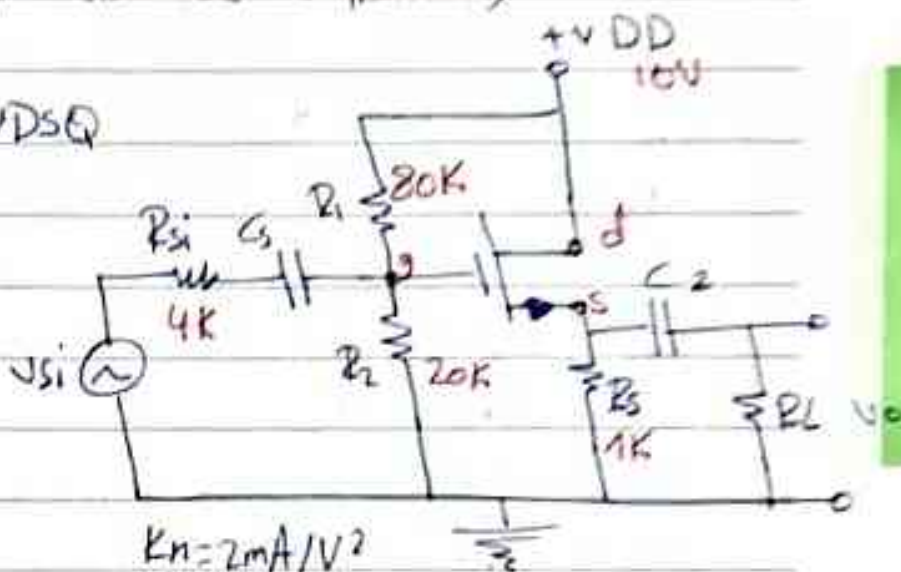
$$-v_{ds} + I_d [R_{S1} + (R_D || R_L)]$$

$$\text{slope} = \frac{-1}{R_{S1} + (R_D || R_L)}$$

② Common-Drain Amp (source follower)

1) - Determine I_{DQ} , V_{DSQ}

2) - Draw s.s.A.C eq ckt & find A_v , R_i , R_o



① D.C Analysis

Assume the mosfet in sat Reg.

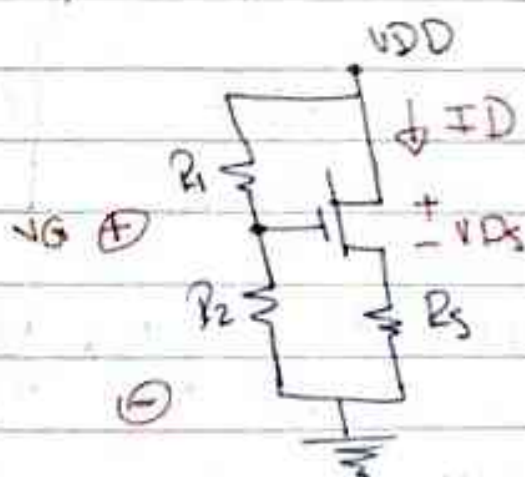
$$\Rightarrow I_D = K_n (V_{GS} - V_{TN})^2$$

$$V_{GS} = V_G - V_S$$

$$V_{GS} = \frac{V_{DD} R_2}{R_1 + R_2} - I_D R_S$$

$$\Rightarrow V_{GS} = 2 - I_D \quad , \quad I_D = 2 - V_{GS}$$

$$\Rightarrow 2 - V_{GS} = 2 (V_{GS}^2 - 2V_{GS} + 1)$$



$$\Rightarrow 2V_{GS}^2 - 3V_{GS} = 0$$

$$V_{GS}(2V_{GS} - 3) = 0$$

$$\Rightarrow V_{GS} = 0 \quad \text{or} \quad V_{GS} = 1.5 \text{ V}$$

$$I_D = 2 - 1.5 = 0.5 \text{ mA}$$

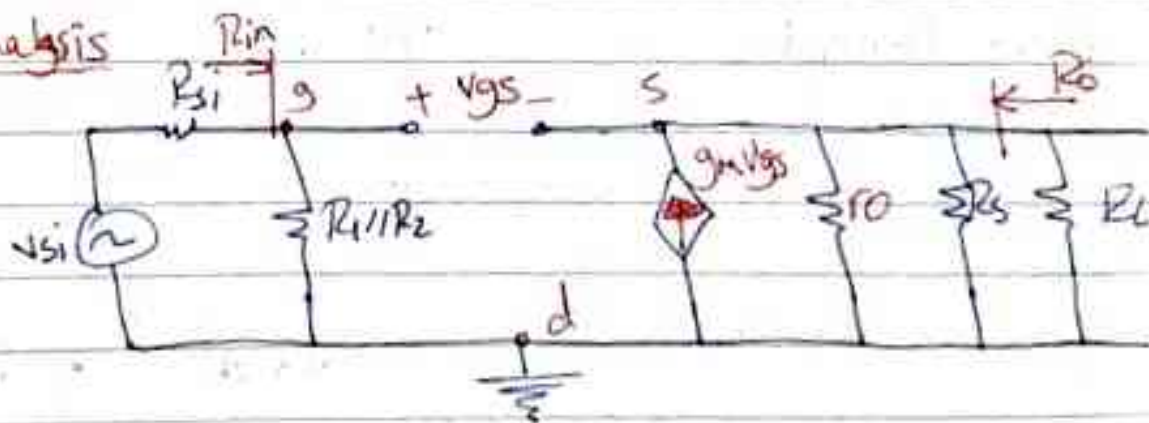
$$\Rightarrow V_{DS} = 10 - 0.5 \times 1$$

$$V_{DS} = 9.5 \text{ V}$$

$$\Rightarrow V_{DS}(\text{sat}) = 1.5 - 1$$

$$V_{DS}(\text{sat}) = 0.5$$

② A-c Analysis



$$\Rightarrow A_V = \frac{V_O}{V_{Si}} = \frac{V_O}{V_{GS}} \times \frac{V_{GS}}{V_i} \times \frac{V_i}{V_{Si}}$$

$$\ast V_O = g_m V_{GS} (R_D \parallel R_S \parallel R_L) \quad \bar{R}_L \dots$$

$$\ast \frac{V_O}{V_{GS}} = g_m \bar{R}_L$$

$$\Rightarrow$$

$$\textcircled{1} \phi = 0^\circ$$

$\textcircled{3} R_i$ depends on R_1 & R_2

$$\textcircled{2} A_V < 1$$

$\textcircled{4} R_o$ low

$\textcircled{5}$

$$\Rightarrow -v_i + v_{gs} + v_o = 0$$

$$v_i = v_{gs} + g_m v_{gs} \bar{R}_L$$

$$v_i = v_{gs} (1 + g_m \bar{R}_L)$$

$$\star \frac{v_{gs}}{v_i} = \frac{1}{1 + g_m \bar{R}_L}$$

$$\Rightarrow \frac{v_i}{v_s} = \frac{R_{th}}{R_{th} + R_{si}}$$

$$\Rightarrow A_V = \frac{g_m \bar{R}_L}{1 + g_m \bar{R}_L} \times \frac{R_{th}}{R_{th} + R_{si}}$$

\star If $R_{th} \gg R_{si}$ & $g_m \bar{R}_L \gg 1$

$$\Rightarrow A_V = 1 = \frac{v_o}{v_{si}}$$

$\hookrightarrow v_o$ follows v_{si} in magnitude & phase
& r_o is taken from source, so it is called
source follower

$$\star R_{in} = R_{th}$$

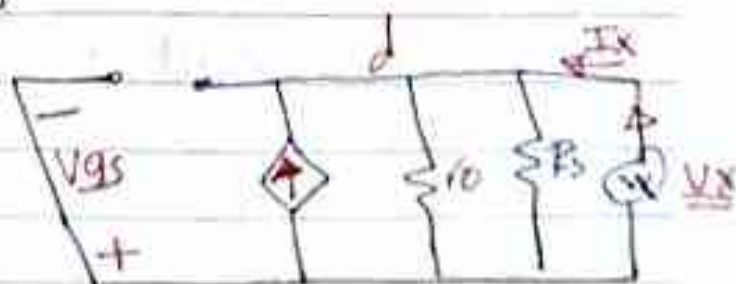
$$\star R_o = ?? \Rightarrow R_o = \left. \frac{v_x}{i_x} \right|_{v_{si}=0}$$

\star KCL at node d

$$i_x + g_m v_{gs} = \frac{v_x}{r_o} + \frac{v_x}{R_s}$$

$$v_{gs} = -v_x$$

$$i_x = v_x \left(g_m + \frac{1}{r_o} + \frac{1}{R_s} \right)$$



\Rightarrow

$$\Rightarrow P_o = \frac{1}{g_m} \parallel r_o \parallel R_s$$

③ Common-Gate Amp (C.G)

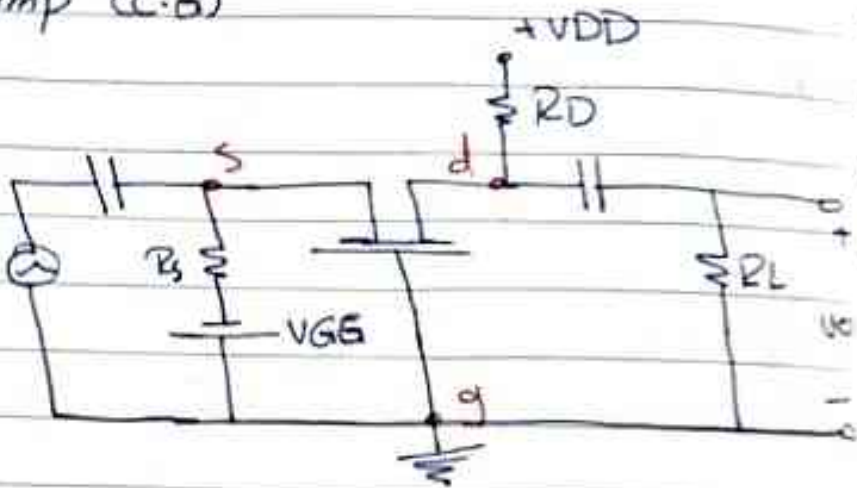
DC

$v_i = \text{source}$

$v_o = \text{Drain}$

Gate - common term

Solve for V_{GS} , I_D
& V_{DS}



$$\Rightarrow I_D = k_n (V_{GS} - V_{TN})^2$$

$$V_{GS} + I_D R_s - V_{GG} = 0$$

$$V_{GS} = V_{GG} - I_D R_s$$

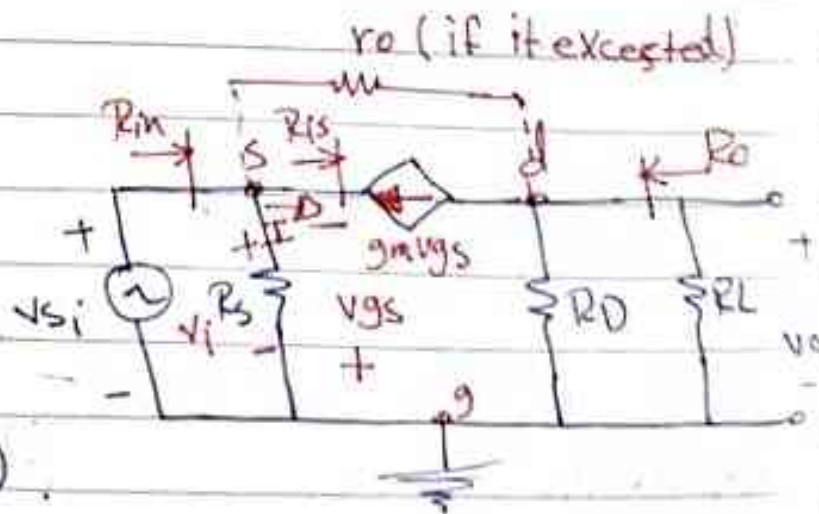
$$I_D = \frac{V_{GG} - V_{GS}}{R_s}$$

AC

$$V_o = -g_m V_{gs} (R_D \parallel R_L)$$

$$V_{gs} = -V_{si}$$

$$\frac{V_o}{V_{si}} = g_m (R_D \parallel R_L)$$



$$\Rightarrow \angle \phi = 0^\circ$$

$$\textcircled{2} AV \geq 1$$

$$\star R_{in} = R_s \parallel R_{is}$$

$$\Rightarrow R_{is} = \frac{v_i}{i} = \frac{-v_{gs}}{-g_m v_{gs}} = \frac{1}{g_m}$$

$$\Rightarrow R_{in} = R_s \parallel \frac{1}{g_m} \Rightarrow \textcircled{3} \text{ Low } R_{in}$$

$$\star R_o = ??$$

$$\Rightarrow R_o = \frac{v_x}{i_x} \Big|_{v_{si} = 0}$$

When $v_{si} = 0$, $v_{gs} = 0$

$g_m v_{gs} = 0$ (D.C source - D.O.C)

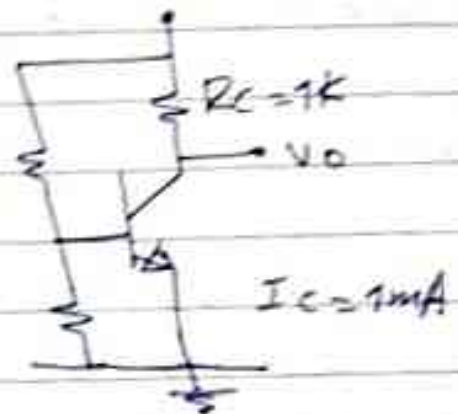
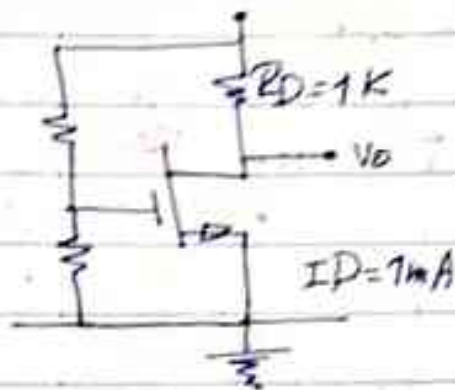
$$\Rightarrow R_o = R_D$$

• C.D & C.G mixed to Loading

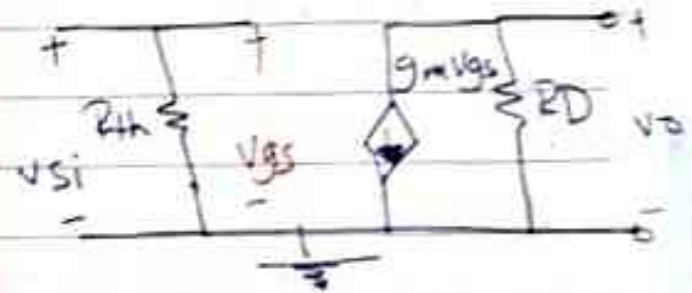
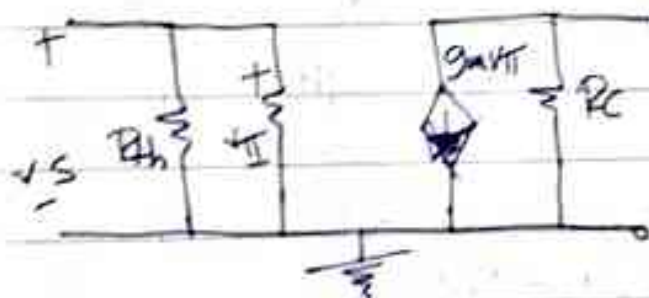
for the same current value $\Rightarrow g_m \rightarrow \text{C.D}$

53

• AV for Mosfet Amp is less than AV for BJT Amp due to low g_m value for the same current level.



$\oplus \ominus$ \rightarrow $\text{C.D} \rightarrow \text{C.G}$



$$A_V = -g_m R_C$$

$$= \frac{-1 \text{ mA} \cdot 1 \text{ K}}{0.026}$$

$$A_V = -38.5$$

$$A_V = -g_m R_D$$

$$g_m = 2 \sqrt{K_n I_D}$$

For $K_n = 10$

$$g_m = 2 \sqrt{10 \cdot 1} = 6.6 \text{ mA/V}$$

$$A_V = -6.6$$

Amp	C.S	C.D	C.G
AV	> 1	< 1	> 1
AI	—	—	1
Ri	Rth	Rth	Low
Ro	mod-high	Low	mod-high
ϕ	180	ϕ	ϕ

* cascode => E.S & CG => المرحلتين من الترانزستور

69

multistage Amp.

① cascode multistage Amp.

* Design the ckt to have

$I_{DQ} = 1 \text{ mA}$

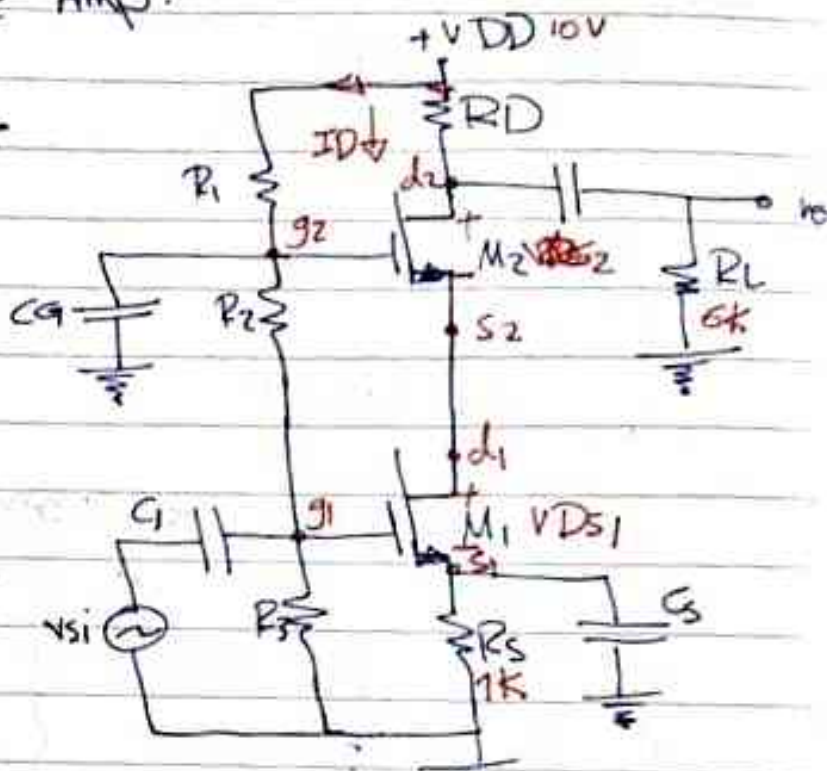
$V_{DS1} = V_{DS2} = 3 \text{ V}$

① Find R_1, R_2, R_3, R_D

② Draw S.S.A.C eq. ckt

& Find A_V, R_i, R_o

- Let $I = 10\% I_D$



Sol:-

$R_D ??$

$K_{n1} = K_{n2} = 1 \text{ mA/V}^2$

$-10 + I_D R_D + V_{DS2} + V_{DS1} + I_D R_S = 0 \quad V_{TN1} = V_{TN2} = 1 \text{ V}$

$I_D R_D = 10 - V_{DS1} - V_{DS2} - 1 \times 1 = 3 \text{ V}$

$R_D = \frac{3 \text{ V}}{I_D} = 3 \text{ k}\Omega$

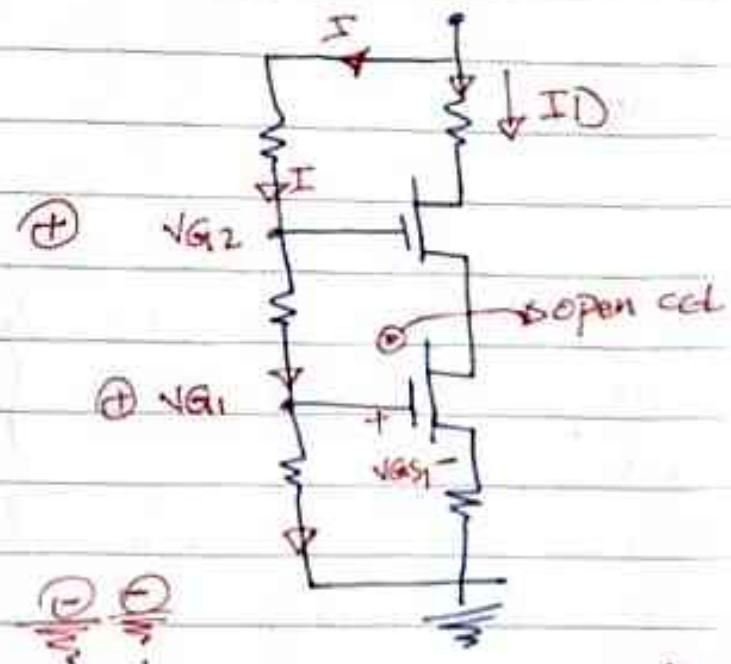
$R_3 = \frac{V_{G1}}{I}, \quad R_2 = \frac{V_{G2} - V_{G1}}{I}$

$R_1 = \frac{V_{DD} - V_{G2}}{I}$

$-V_{G1} + V_{GS1} + I_D R_S = 0$

$V_{G1} = V_{GS1} + I_D R_S$

$I_D = K_n (V_{GS} - V_{TN})^2$



=>

$$V_{GS} = V_{TN} + \sqrt{\frac{I_D}{k_n}}$$

$$V_{GS1} = 1 + \sqrt{\frac{I}{k}} = 2V \quad \text{OR} \quad 0 = V_{GS2}$$

$$V_{G1} = 2 + 1 \times 1 = 3V$$

$$I = 0.1 \times I_D = 0.1 \text{ mA}$$

$$R_3 = \frac{3V}{0.1} = 30 \text{ k}\Omega$$

$$-V_{G2} + V_{GS2} + V_{DS1} + I_D R_3 = 0$$

$$V_{G2} = 2 + 3 + 1 \times 1 = 6V$$

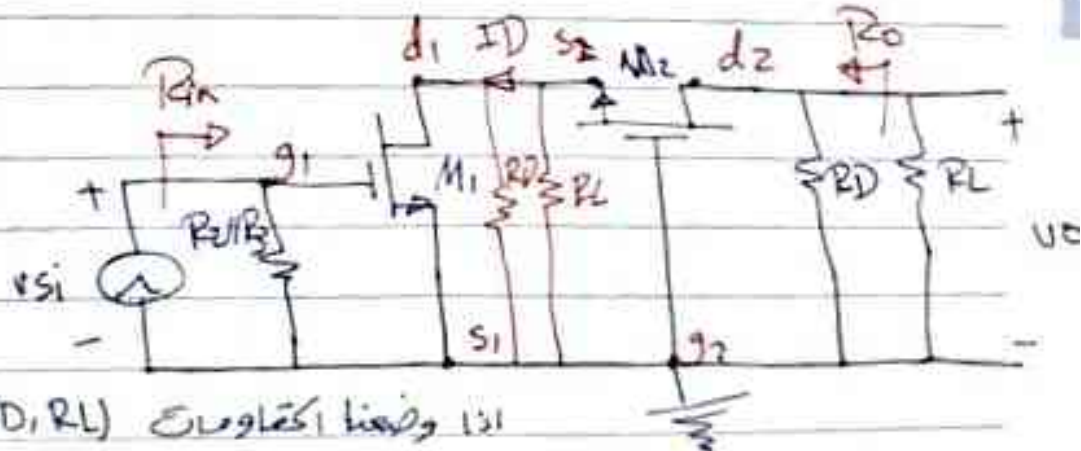
$$R_2 = \frac{6 - 5}{0.1} = 30 \text{ k}\Omega$$

$$R_T = 30 + 30 + 40 = 100 \text{ k}\Omega$$

$$R_T = \frac{V_{DD}}{I_D} = \frac{10V}{0.1} = 100 \text{ k}\Omega \quad (\text{for checks})$$

$$R_1 = \frac{10 - 6}{0.1} = 40 \text{ k}\Omega$$

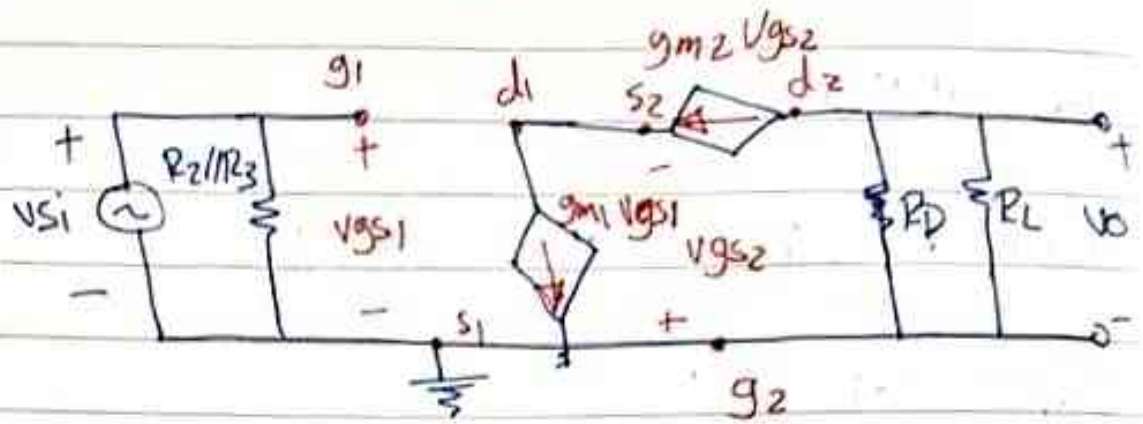
② AC Analysis



إذا وضعتا مكافؤات (R_D, R_L) عند M_1
 فإن v_o أو v_{out} بحسبك لأنه الدارة الثانية
 $A_{V1} = 1$ و $G_{V1} = G_{V2}$ و $A_{V2} = 1$ و v_o
 لـ G_{V1} يدخل فيه صابغة التيار ومعايير التيار
 unity current gain أو $v_o = 1$

* this ckt is used to Amplify frequency f as a wide band Amplifier.

71



$$A_V = \frac{V_O}{V_{S_i}} = \frac{-g_{m1} V_{gs1} (R_D \parallel R_L)}{V_{gs1}}$$

$$= -g_m (R_D \parallel R_L)$$

$$R_i = R_2 \parallel R_3 = 15 \text{ k}\Omega$$

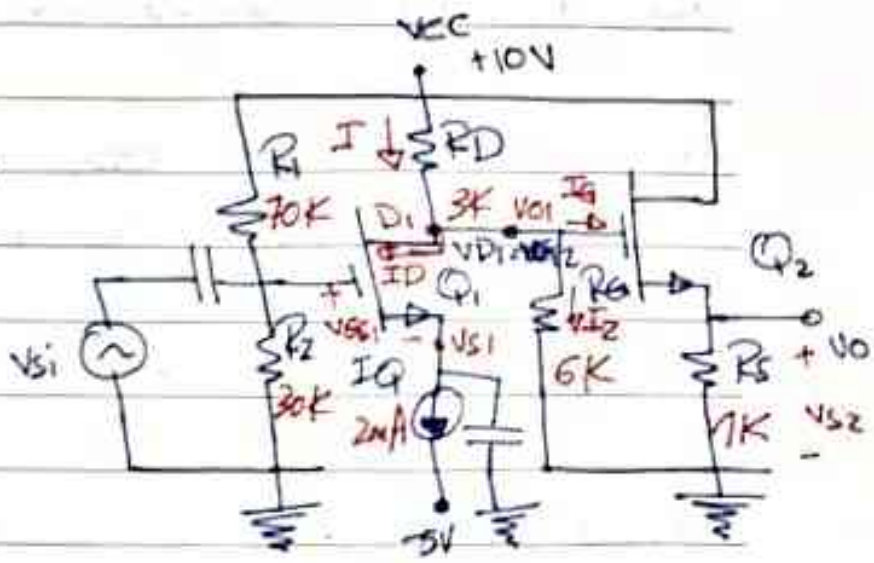
$$R_o = \left. \frac{V_X}{I_X} \right|_{V_{S_i}=0} = R_D$$

$$g_{m1} = g_{m2} = 2 \sqrt{K_n I_D} = 2 \text{ mA/V}$$

$$A_V = -2(3/6) = -4$$

② cascade multistage

- 1) - Find $V_{D1}, I_{D2}, V_{D_{S2}}, V_{S1}$
- 2) - Draw s.s.A.C eq cct
 & Find $A_V = \frac{V_O}{V_{S1}}, R_{in}$
 $R_o, R_{in2}, A_{V1} = \frac{V_{O1}}{V_{S1}}$



Soln:

① D.C Analysis

$K_{n1} = K_{n2} = 2 \text{ mA/V}^2$

$I_{D1} = 2 \text{ mA}$

$V_{TN} = ? \quad \lambda = 0.02 \text{ V}^{-1}$

KCL at node D1

$V_{TN1} = V_{TN2} = 1 \text{ V}$

$I = I_D + I_2$

$$\frac{10 - V_{D1}}{3} = 2 + \frac{V_{D1}}{6}$$

$$20 - 2V_{D1} = 12 + V_{D1} \Rightarrow V_{D1} = \frac{8}{3} = 2.66 \text{ V}, \quad \underline{V_{D1} = V_{G2}}$$

$$I_{D2} = K_n (V_{GS2} - V_{TN})^2$$

$V_{GS1} = V_{G1} - V_{S1}$

$V_{GS} = V_{TN} + \sqrt{\frac{I_{D1}}{K_{n1}}} = 1 + \sqrt{\frac{2}{2}} = 2 \text{ V} \quad \underline{O.K.}$

$V_{S1} = V_{G1} - V_{GS1}$

$$= \frac{10 \times 30}{100} - 2 = \underline{1 \text{ V}}$$

$V_{D_{S1}} = V_{D1} - V_{S1} = 2.66 - 1 = 1.66 \text{ V}$

$V_{D_{S1}} (\text{sat}) = V_{GS1} - V_{TN} = 1 \text{ V}$

$$V_{GS2} = V_{G2} - V_{S2} = 2.66 - I_{D2} R_S = 2.66 - I_{D2}$$

$$I_{D2} = 2.66 - V_{GS2} = 2.66 - V_{GS2}$$

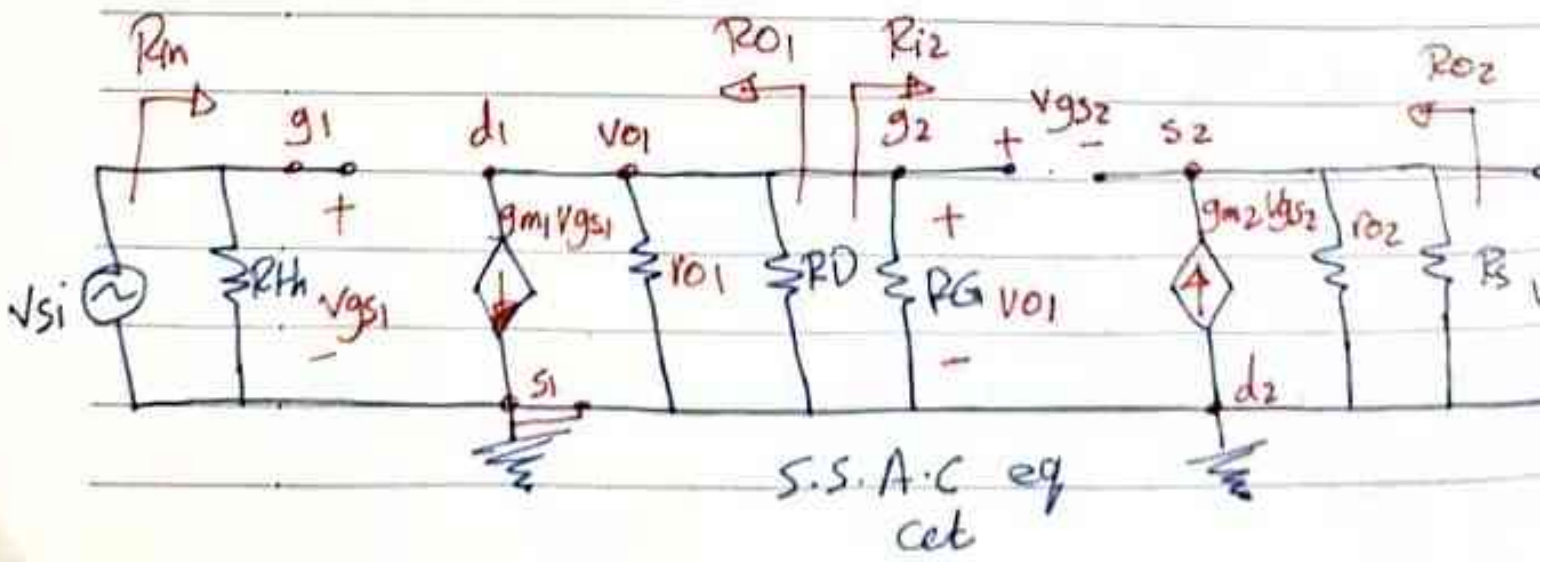
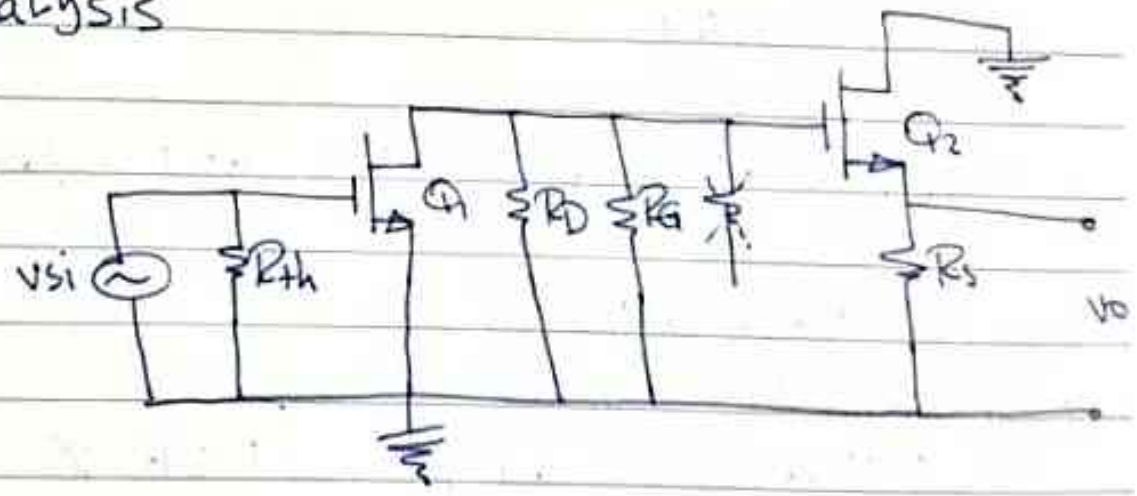
$$2.66 - V_{GS2} = 2 (V_{GS2}^2 - 2V_{GS2} + 1)$$

$$2V_{GS2}^2 - 3V_{GS2} - 0.66 = 0$$

$$V_{GS2} = \frac{3 \pm \sqrt{9 + 4 \times 2 \times 0.66}}{4}$$

$$V_{GS2} = \frac{3 \pm \sqrt{14}}{4} = \frac{3 \pm 3.6}{4} = 1.66 \text{ V}$$

② A.C. Analysis



الجزء من الstage الاول وليس من الثاني يعني ما يتقبل بار R_{in}

74

$$R_{in} = R_{in1} = R_{th}$$
$$(70 // 30) = 21 k\Omega$$

$$A_v = \frac{V_o}{V_{si}} = \frac{V_o}{V_{o1}} \cdot \frac{V_{o1}}{V_{si}}$$

$$V_o = g_{m2} V_{gs2} (R_s // r_{o2}) \quad \cdot \quad g_{m1} \neq g_{m2} \text{ because } \underline{ID}$$

$$-V_{o1} + V_{gs2} + g_{m2} V_{gs} (R_s // r_{o2})$$

$$V_{o1} = V_{gs2} (1 + g_{m2} R_s // r_{o2})$$

$$\frac{V_o}{V_{o1}} = \frac{g_{m2} (R_s // r_{o2})}{1 + g_{m2} (R_s // r_{o2})} \Rightarrow \underline{A_{v2}}$$

$$V_{o1} = -g_{m1} V_{gs1} (r_{o1} // R_D // R_G)$$

$$\underline{V_{gs1} = V_{si}}$$

$$\frac{V_{o1}}{V_{si}} = -g_{m1} (r_{o1} // R_D // R_G) \Rightarrow \underline{A_{v1}}$$

$$A_v = \frac{g_{m2} (r_{o2} // R_s)}{1 + g_{m2} (r_{o2} // R_s)} \cdot \underbrace{(-g_{m1} r_{o1} // R_D // R_G)}_{A_{v1}}$$

$$r_{o1} = \frac{1}{\lambda I_{D1}} = \frac{1}{0.02 \times 4 \times 10^{-3}} = \frac{10^5}{4} = 25 k\Omega$$

$$r_{o2} = \frac{1}{0.02 \times 1 \times 10^{-3}} = 50 k\Omega$$

$$g_{m1} = 2 \sqrt{K_{n1} I_{D1}} = 4 \text{ mA/V}$$

طبع A_v من الstage الاول \Rightarrow يتلقى V_{si}

75

$$g_{m2} = 2\sqrt{k_{n2}I_{D2}}$$

$$A_{V1} = -4 * (25 // 3 // 6) = -7.2 \text{ volt}$$

$$A_{V2} = \frac{2.82 \text{K}\Omega}{1 + 2.8} = 0.9$$

$$\Rightarrow A_V = -7.2 (0.9) \Rightarrow A_V = -6.7$$

$$R_{in2} = R_G = 6 \text{K}\Omega$$

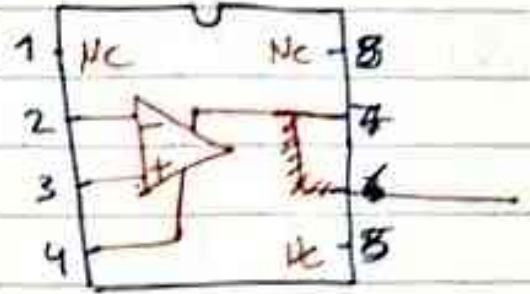
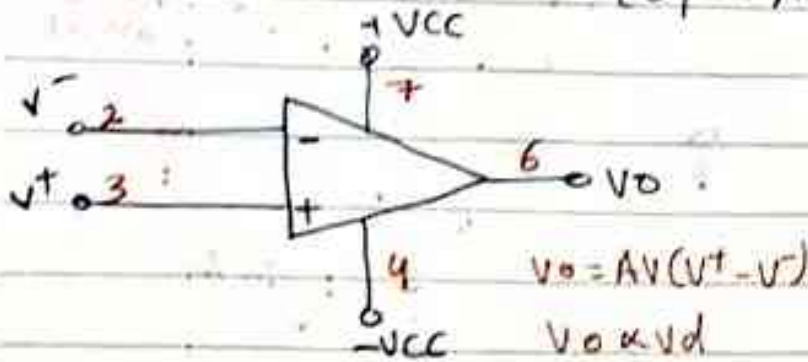
$$R_{o1} = R_D // r_{o1} = 2.5 \text{K}\Omega$$

$$R_o = R_{o2} = \frac{V_x}{I_x} \Big|_{v_{si}=0}$$

$$R_o = R_{o2} = \frac{1}{g_{m2}} // r_{o2} // R_S$$

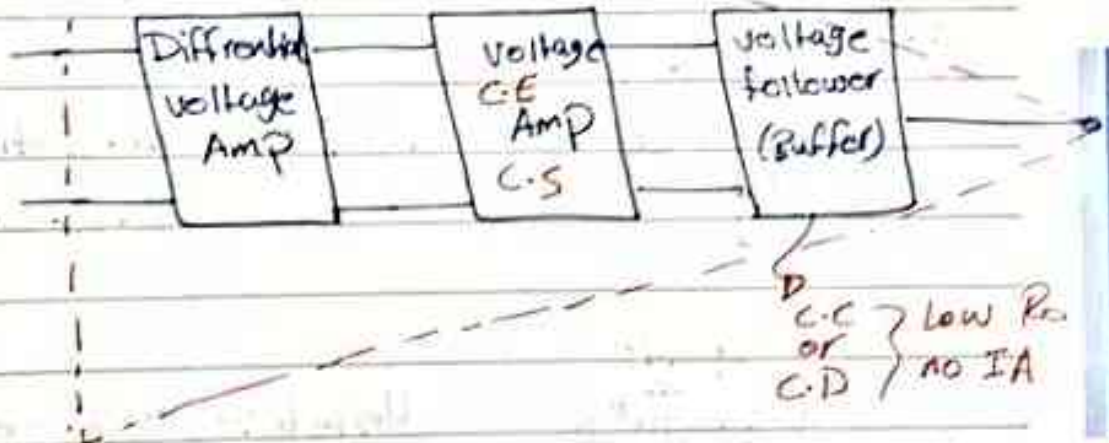
$$= \frac{10^2}{2.8} // 50 \text{K} // 1 \text{K} = 500 \Omega$$

Operational Amplifier (OP-Amp)



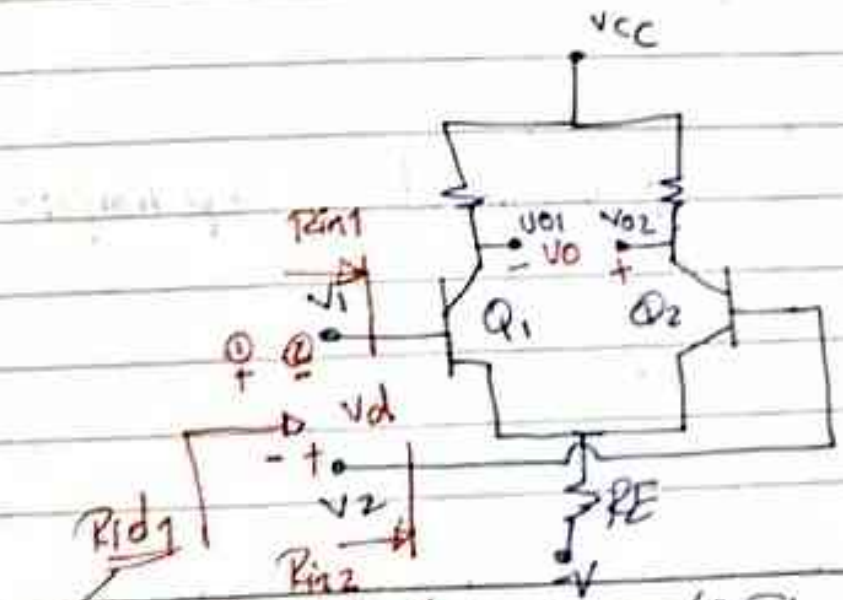
741

- * v^+ :- non inverting terminal
- * v^- :- inverting terminal



$$v_o = A_d \cdot v_d$$

$$= \frac{v_o}{v^+ - v^-}$$



R_{in} differential ($R_{in1} \parallel R_{in2}$)

* R_{in} for Mos op-Amp $\approx \infty$

* ~~BJT~~ op-Amp \Rightarrow cap \rightarrow $L \rightarrow L \rightarrow A \& D \rightarrow$ is \rightarrow \rightarrow

* its a very high gain direct coupled voltage Amp

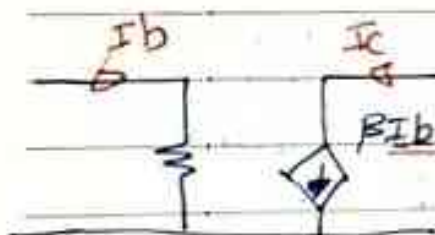
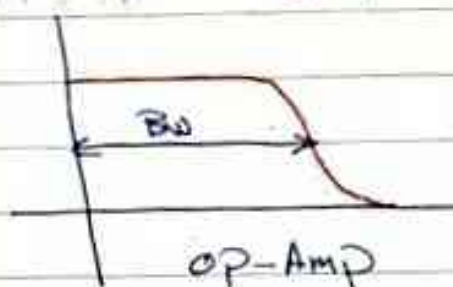
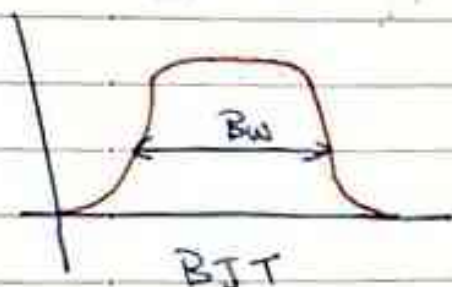
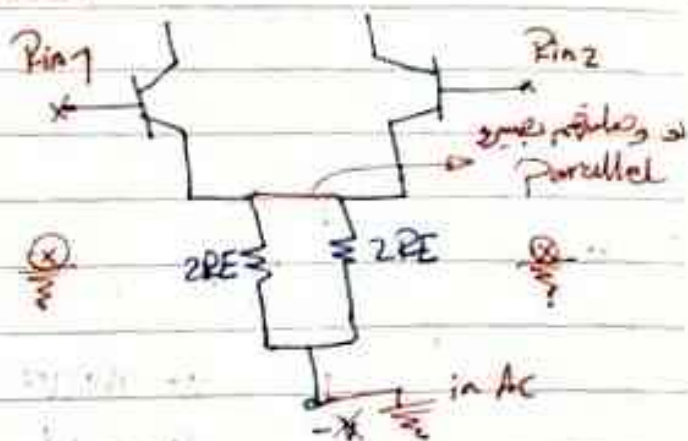
[77]

$$R_{in1} = 2RE(\beta+1) + r_{\pi1}$$

$$R_{in2} = 2RE(\beta+1) + r_{\pi2}$$

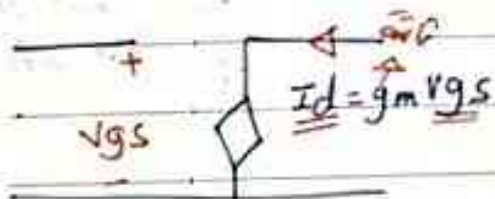
$$R_{id} = R_{in1} + R_{in2}$$

$$= 4RE(\beta+1) + r_{\pi1} + r_{\pi2}$$



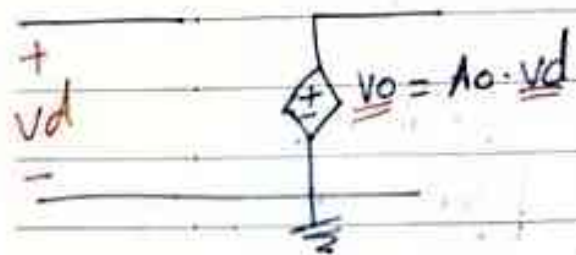
$$\beta I_b = I_c$$

BJT :- Cur. control. cur. source
C.C.C.S



$$I_d = g_m v_{gs}$$

Mosfet :- Volt. cont. cur. source
V.C.C.S



$$v_o = A_0 \cdot v_d$$

op-Amp :- Volt. cur. volt. source
V.C.V.S

gain (تغییر پیدا)

* open loop \Rightarrow

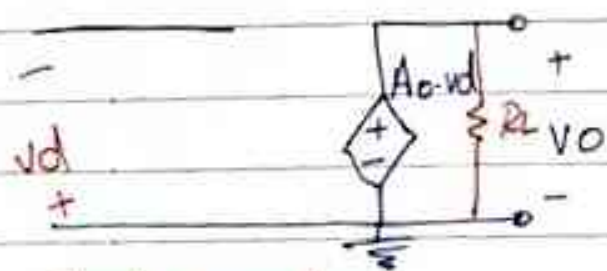
closed loop \Rightarrow

open loop \Rightarrow \rightarrow in data sheet (given)

OP-Amp cks

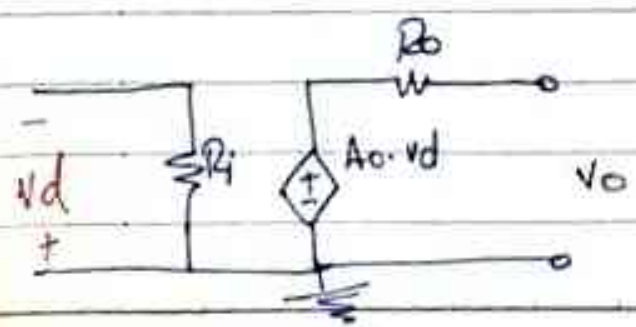
	ideal op-Amp	LM13800 (MOSFET)	NON-ideal (741-Bipolar)
R_i	∞	$10^{12} \Omega$	$2M \Omega$
R_o	0	20Ω	$(60 \rightarrow 75) \Omega$
open loop gain A_o	∞	10^4	2×10^5
Band width BW	∞	$2MHz$	$1M Hz$
I/P bias current	0	$< 10 fA$ $F=10^{15}$	$(1-10) pA$

for knowledge.



$v_o = A_o \cdot v_d$
 $\Rightarrow v_o$ is independent on R_L

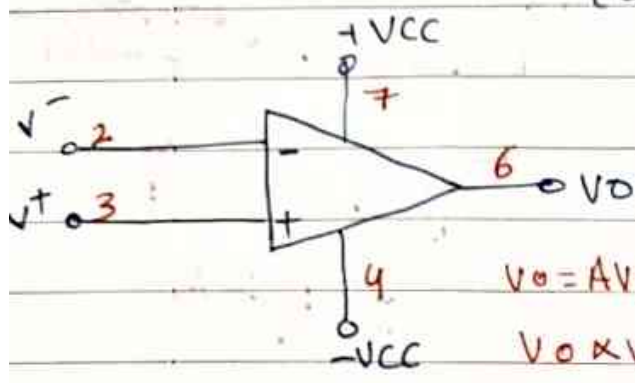
Ideal op-Amp



$v_o = \frac{A_o \cdot v_d \cdot R_L}{R_L + R_o}$
 $\Rightarrow v_o$ depends on R_L

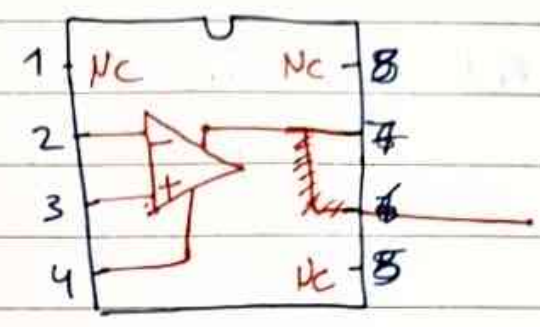
Non-Ideal-Amp

Operational Amplifier (OP-Amp)



$$V_O = A_V (V^+ - V^-)$$

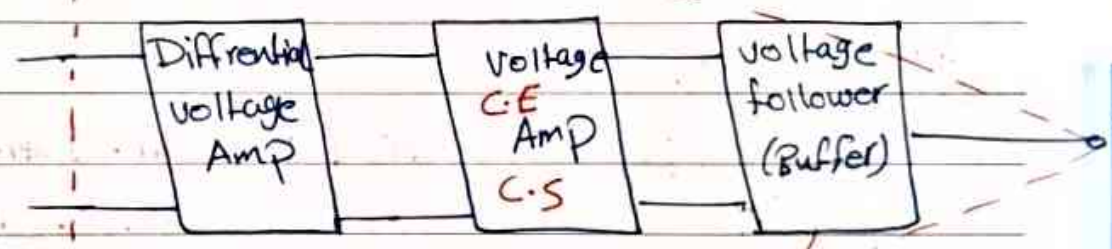
$$V_O \propto V_d$$



741

V^+ :- non inverter terminal

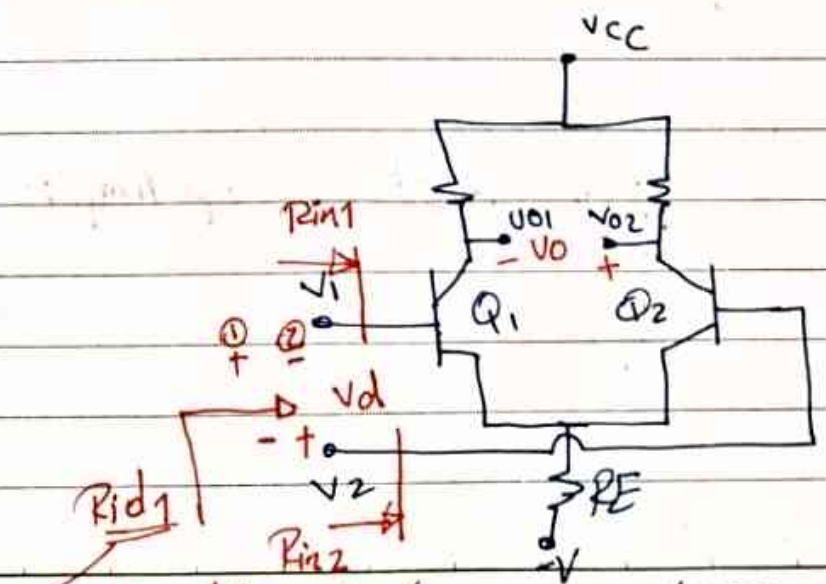
V^- :- inverter term.



C.C or C.D } Low R_o
NO I_A

$$V_o = A_d \cdot V_d$$

$$= \frac{V_O}{V^+ - V^-}$$

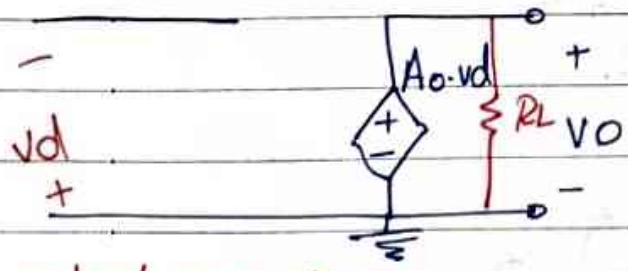


R_{in} differential. ($R_{in} \approx 2R_{in1}$)

OP-Amp c/s

	ideal op-Amp	LM13600 (MOSFET)	NON-ideal (741-Bipolar)
R_i	∞	$10^{12} \Omega$	$2M \Omega$
R_o	0	20Ω	$(60 \rightarrow 75) \Omega$
open loop gain A_o	∞	10^4	2×10^5
Band width BW	∞	$2MHz$	$1M Hz$
I/P bias current	0	$< 10 fA$ $f = 10^{15}$	$(1-10) pA$

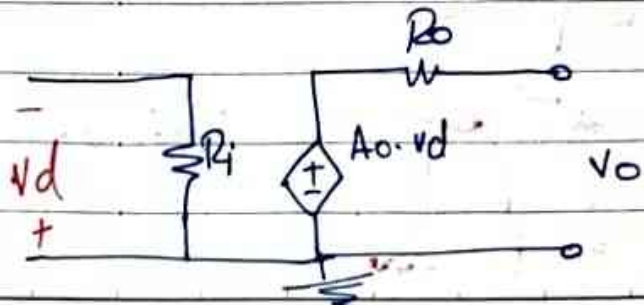
↳ for knowledge.



$$v_o = A_o \cdot v_d$$

$$\Rightarrow v_o \text{ is independent on } \underline{R_L}$$

Ideal op-Amp



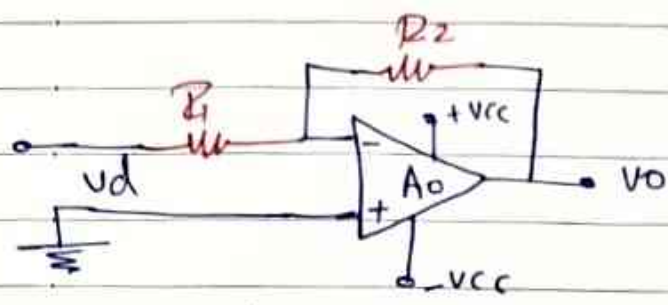
$$v_o = \frac{A_o \cdot v_d \cdot R_L}{R_L + R_o}$$

$$\Rightarrow v_o \text{ depends on } \underline{R_L}$$

NON-ideal - Amp

- * virtual short $\Rightarrow V_{node1} = V_{node2}$ & neither goes to Gnd
- * virtual Gnd $\Rightarrow V_{node1} = V_{node2}$ & one of them = = =

[80]



$$\Rightarrow v_o = \frac{R_2}{R_1} v_i$$

↳ زيادة الجهد

(closed loop)

ال ratio بين الجهد الخارج والجهد الداخل v_o/v_i
 بحيث يكون الجهد الخارج أكبر من الجهد الداخل $v_o > v_i$

op-Amp Applications

A Linear Applications ($v_o \times v_i$)

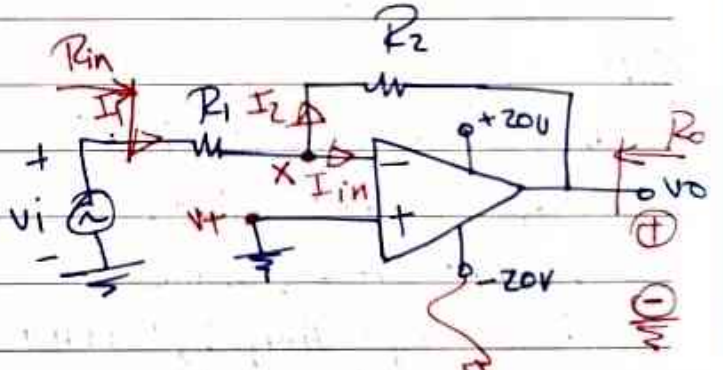
↳ C.E & C.S

I Inverting Amplifier

* KCL at node X

$$I_1 = I_2 + I_{in}$$

$$\frac{v_i - v_x}{R_1} = \frac{v^- - v_o}{R_2} + I_{in}$$



but for ideal op-Amp.

$$I_{in} = 0, (R_{in} = \infty)$$

$$v^- = v^+ = 0, (\text{virtual ground})$$

$$v_o = A_o (v^+ - v^-)$$

For ideal op-Amp: $A_o = \infty$

$$v^+ - v^- = \frac{v_o}{\infty} = 0 \Rightarrow v^+ = v^-$$

but $v^+ = 0, \therefore v^- = 0$ (virtual ground)

* الجهد الخارج أكبر من الجهد الداخل
 $v_o > v_i$
 زيادة الجهد
 $\pm V_{CC}$ الجهد الخارج أكبر من الجهد الداخل

الجهد الخارج $v_o = 1000$ (بزيادة الجهد)

every

- * virtual ground = virtual short
- ↳ virtual short \neq virtual ground

$$v_x = v^-$$

$$\frac{V_i}{R_1} = -\frac{V_o}{R_2}$$

$$\Rightarrow V_o = -\frac{R_2}{R_1} V_i$$

* closed-loop gain

$$AV = \frac{V_o}{V_i} = -\frac{R_2}{R_1}$$

* $R_{in} = \Delta -V_i + I_1 R_1 + 0 = 0$, R_{in} for cct = value
 $R_{in} = \frac{V_i}{I_1} = R_1$ R_{in} for operational Amp = ∞

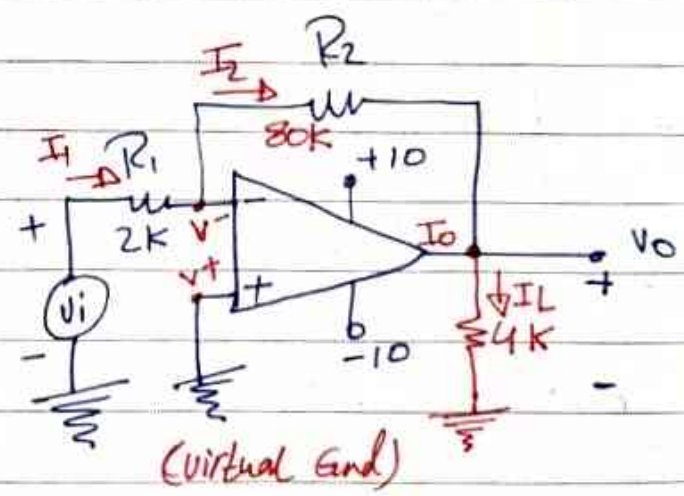
* $R_o = R_{op-Amp} = 0$

EX:-

1)- Design an Inverting Amp to have $AV = -40$ & $R_{in} = 2K\Omega$ (assume ideal op-Amp), $V_{CC} = \pm 10V$.

2.) - If $V_i = 0.3 \sin(\omega t)$ [V]
 \Rightarrow draw $V_o(t)$

3)- If $R_L = 4K\Omega$, $V_i = 0.2$ V (d.c) , calculate I_L , I_1 , I_2 , I_o



SOL:-

$$R_{in} = R_1 = 2K\Omega$$

$$AV = -\frac{R_2}{R_1} \Rightarrow -40 = -\frac{R_2}{2K} \quad , \quad R_2 = 80K\Omega$$

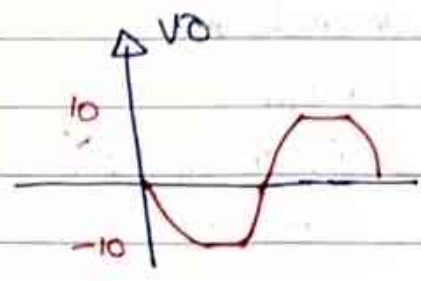
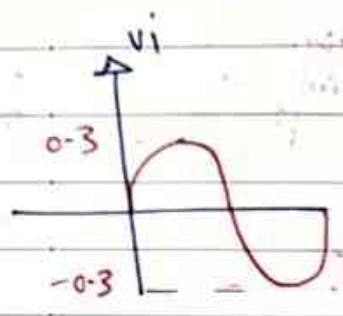


* I_o is the current through the load resistor R_L and is given by $I_o = \frac{V_o}{R_L}$

- * I_O \rightarrow sink \Rightarrow sinks op-Amp
- * I_O \rightarrow source \Rightarrow source op-Amp.

[82]

② $V_O(t) = A_V \cdot v_i = -40(0.3 \sin \omega t)$
 $= -12 \sin \omega t$ [V]



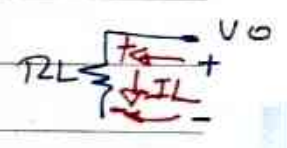
③ $I_L = \frac{V_O}{R_L}$

$V_O = A_V \cdot v_i = -40(0.2) = -8V$

$I_L = \frac{-8}{4} = -2mA$

$\downarrow I_L = -2mA$

$\uparrow I_L = 2mA$



$I_1 = \frac{v_i - V^-}{R_1}$

$V^- = V^+ = 0 (V.G)$

$\Rightarrow I_1 = \frac{0.2V}{R_1} = \underline{0.1mA}$

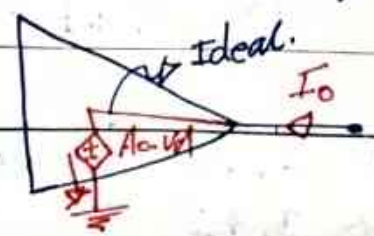
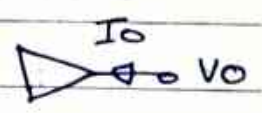
$\Rightarrow I_2 = \frac{V^- - V_O}{R_2} = \frac{0 - (-8)}{80} = \underline{0.1mA}$

must be the same because the op-Amp Ideal.

$I_2 = I_O + I_L$

$\Rightarrow I_O = I_2 - I_L = 0.1 - (-2) = \underline{2.1mA}$

\Rightarrow The op-Amp sinks current

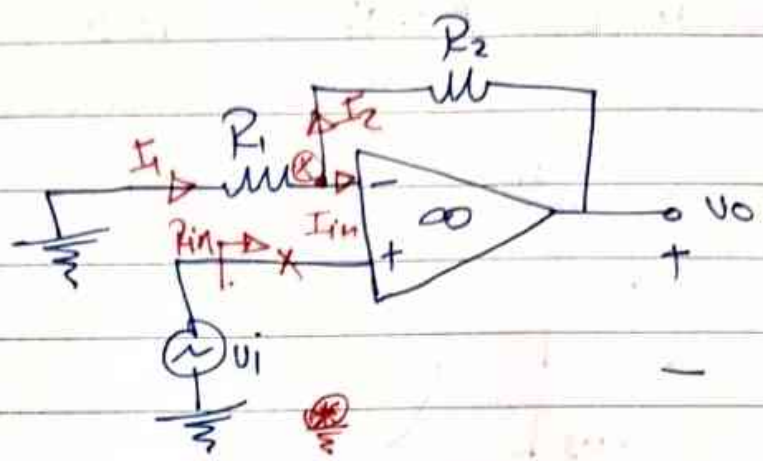


II Non Inverting Amp.

* KCL at node ⓧ

$$I_1 = I_2 + I_{in}$$

$$\frac{0 - V^-}{R_1} = \frac{V^- - V_0}{R_2} + I_{in}$$



but $V^- = V^+ = V_i$ (virtual short)
 $I_{in} = 0$

For Ideal op-Amp \Rightarrow

$$\frac{-V_i}{R_1} = \frac{V_i - V_0}{R_2}$$

$$\frac{V_0}{R_2} = \frac{V_i}{R_2} + \frac{V_i}{R_1}$$

$$V_0 = V_i \left(1 + \frac{R_2}{R_1} \right)$$

$$\Rightarrow AV = \frac{V_0}{V_i} = 1 + \frac{R_2}{R_1}$$

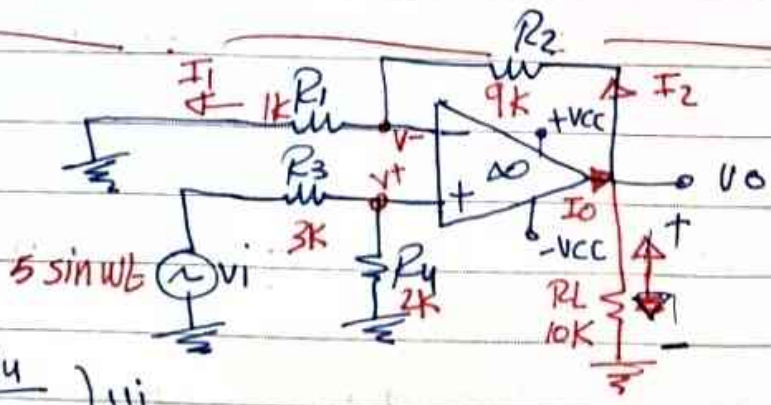
* $R_{in} = R_i(\text{OP-Amp}) = \infty$

Ex:-

$$V_0 = \left(1 + \frac{R_2}{R_1} \right) V^+$$

$$V^+ = \frac{V_i \cdot R_4}{R_3 + R_4}$$

$$V_0 = \left(1 + \frac{R_2}{R_1} \right) \left(\frac{R_4}{R_3 + R_4} \right) V_i$$



بصورتی که
 ولتاژ ورودی مثبت است

- * $V_0 = +ve \Rightarrow I_1 \& I_2$ (counter clock wise), $I_L \downarrow$, $I_0 \rightarrow$
- * $V_0 = -ve \Rightarrow I_1 \& I_2$ (C.W), $I_L \uparrow$, $I_0 \rightarrow$

$$A_V = \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4}{R_3 + R_4}\right)$$

* For the previous figure :-
 calculate :- $A_V, I_1, I_2, I_L, V_{O1}, I_O$

Sol:-

$$A_V = \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_4}{R_3 + R_4}\right) = \left(1 + \frac{9}{1}\right) \left(\frac{2}{2+3}\right) = 10 * 0.4 = 4$$

$$V_O = A_V \cdot V_i = 4 * 5 \sin \omega t = 20 \sin \omega t \text{ V} \quad (V_O = +V_E)$$

\rightarrow source
 $\rightarrow I_O = \text{down}$

$$\Rightarrow I_L = \frac{V_O}{R_L} = \frac{20 \sin \omega t}{10} = 2 \sin \omega t \text{ mA}$$

$$\Rightarrow I_1 = \frac{V^- - 0}{R_1} \quad ; \quad V^- = V^+ = \frac{V_i * R_4}{R_3 + R_4} = 2 \sin \omega t \text{ V}$$

$$\therefore I_1 = \frac{2 \sin \omega t}{1 \text{ K}} = 2 \sin \omega t \text{ mA}$$

$$\Rightarrow I_2 = \frac{V_O - V^-}{R_2} = \frac{(20 \sin \omega t - 2 \sin \omega t)}{9}$$

$$\therefore I_2 = 2 \sin \omega t \text{ mA} \quad , \quad \underline{I_1 = I_2} \text{ (Ideal)}$$

$$\Rightarrow I_O = I_2 + I_L = 2 \sin \omega t + 2 \sin \omega t = 4 \sin \omega t \text{ mA}$$

\therefore op-Amp \Rightarrow source current.

* Ideal Buffer \approx Common Drain (MOSFET)
(Op-Amp)

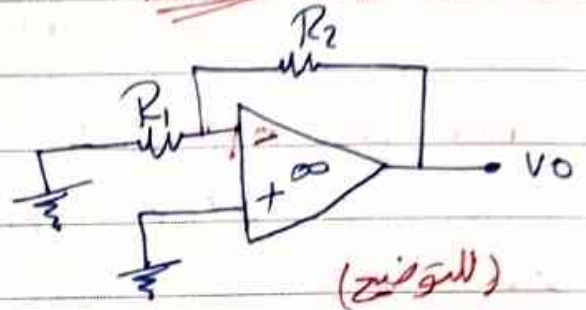
85

III voltage follower (Buffer) \approx

non-inv. (المضخم غير العكسي)

$R_1 = \infty \Rightarrow V_O = (1 + \frac{R_2}{R_1}) V_i$
(O.C) $\Rightarrow V_O = V_i$

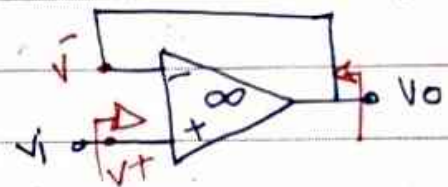
$R_2 = 0 \Rightarrow V_O = (1 + \frac{0}{R_1}) V_i$
(S.C) $\Rightarrow V_O = V_i$



(المضخم)

\Downarrow
= (C.D)

$\frac{V_O}{V_i} = 1 \Rightarrow V_O = V_i$



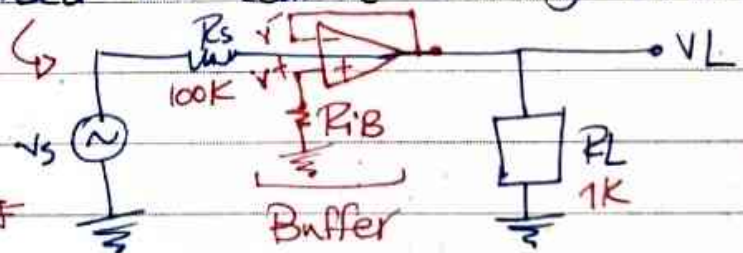
① $A_V = 1$

④ $R_O = 0$

② $\phi = 0^\circ$

⑤ It is used to cancel loading effect.

③ $R_{in} = \infty$



$V_L = \frac{V_S \cdot R_L}{R_L + R_S} = 0.01 V_S$

\hookrightarrow only 1% of V_S is

across load. (sever loading effect) \rightarrow هذه النسبة بترتيب

Buffer

* after adding a Buffer.

$V_X = \frac{V_S \cdot R_{iB}}{R_{iB} + R_S}$

Since $R_{iB} \gg R_S$

$V_X \approx V_S$, but $V_X = V^+ = V^- = V_L$

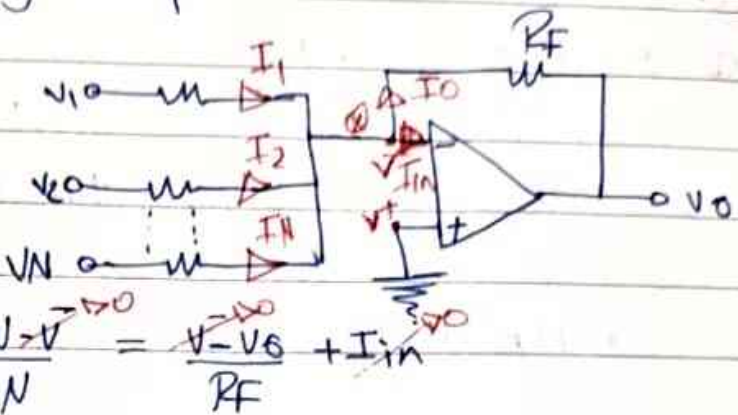
$\therefore V_L = V_S$

\Rightarrow No Loading effect.

IV Inverting summing Amp

Kcl at node \otimes

$$I_1 + I_2 + \dots + I_N = I_o + I_{in}$$



$$\Rightarrow \frac{V_1 - V^-}{R_1} + \frac{V_2 - V^-}{R_2} + \dots + \frac{V_N - V^-}{R_N} = \frac{V^- - V_o}{R_F} + I_{in}$$

but $V^- = V^+ = 0$ ($V^-:G$)

$$I_{in} = 0$$

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_N}{R_N} = -\frac{V_o}{R_F}$$

$$V_o = -\left(\frac{R_F}{R_1} V_1 + \frac{R_F}{R_2} V_2 + \dots + \frac{R_F}{R_N} V_N \right)$$

* V_1, V_2 & V_N can be
Ac, D.C or Ac & D.C

* **Special case.**

$$R_1 = R_2 = R \sim \text{Gain Amplifier}$$

$$\Rightarrow V_o = -\frac{R_F}{R} (V_1 + V_2 + \dots + V_N)$$

EX:- use ideal op-Amp. to design a.cct to give:-

(I) $V_o = -10 (V_1 + V_2)$

(II) $V_o = -(10V_1 + 5V_2 + 3V_3)$



Sol:-

$$\textcircled{I} V_0 = -\frac{R_F}{R} (V_1 + V_2)$$

compared to $V_0 = -10(V_1 + V_2)$

$$\frac{R_F}{R} = 10 \rightarrow \text{Let } R_1 = 1 \text{ k}\Omega$$

$$\therefore R_F = 10 \text{ k}\Omega$$

$$\textcircled{II} V_0 = -\left(\frac{R_F}{R_1} V_1 + \frac{R_F}{R_2} V_2 + \frac{R_F}{R_3} V_3\right)$$

$$\frac{R_F}{R_1} = 10, \quad \frac{R_F}{R_2} = 5, \quad \frac{R_F}{R_3} = 3$$

Let $R_F = 15 \text{ k}\Omega$ \sim Design N مقاومة من $8 \text{ k}\Omega$ إلى $15 \text{ k}\Omega$ V_1 \times
 و V_2 و V_3 من $1 \text{ k}\Omega$ إلى $3 \text{ k}\Omega$ $\#$ للمرتبة

$\therefore R_2 = 3 \text{ k}\Omega, R_1 = 1.5 \text{ k}\Omega$ Range V من R_F بمفرده

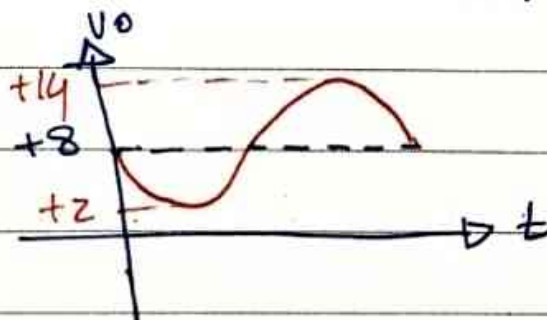
$$R_3 = 5 \text{ k}\Omega$$

EX:- calculate & Draw $V_0(t)$ for $V_1 = -2 \text{ V d.c}$,
 $V_2 = 3 \sin \omega t$ (V). , $V_0 = -(4V_1 + 2V_2)$.

Sol:-

$$V_0 = -(-4 * 2 + 2 * 3 \sin \omega t)$$

$$= (8 \text{ V} - 6 \sin \omega t)$$

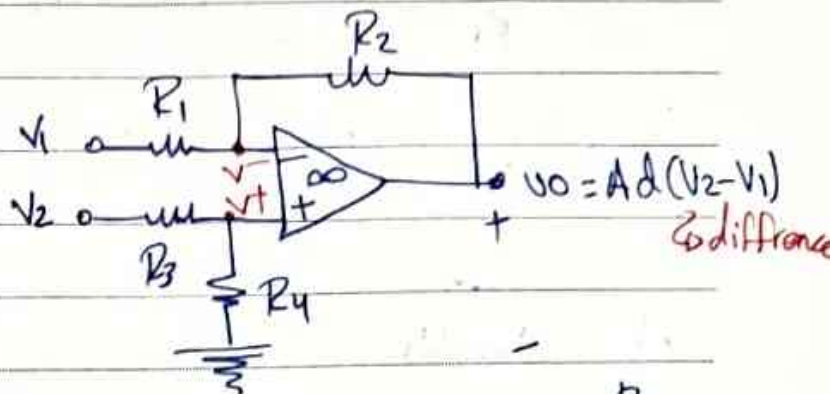


no Amp the difference between 2 signals

(V) Difference Amplifier

* use super position

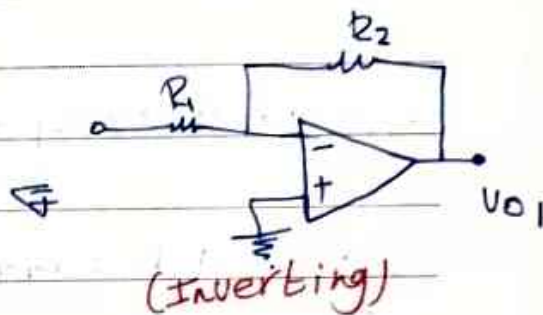
① Effect of V_1 ($V_2=0$)



$$V^+ = \frac{V_2 \cdot R_4}{R_3 + R_4} = 0$$

↳

$$V_{O1} = -\frac{R_2}{R_1} V_1$$

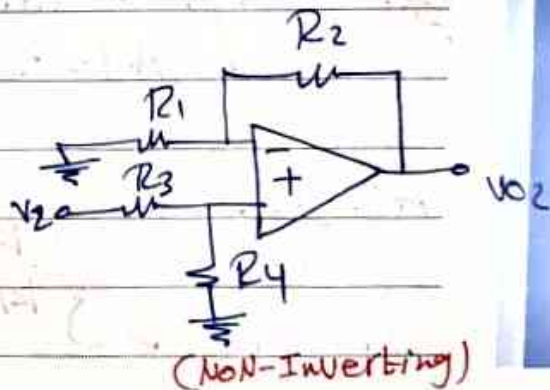


② Effect of V_2 ($V_1=0$)

$$V^+ = \frac{V_2 \cdot R_4}{R_4 + R_3} = V^+$$

↳

$$V_{O2} = \left(1 + \frac{R_2}{R_1}\right) V^+$$



$$\Rightarrow V_{O2} = \left(1 + \frac{R_2}{R_1}\right) \cdot \left(\frac{\frac{R_4}{R_3}}{1 + \frac{R_4}{R_3}}\right) V_2$$

$$\therefore V_0 = V_{O1} + V_{O2}$$

$$\Rightarrow V_0 = \left[\left(1 + \frac{R_2}{R_1}\right) \cdot \frac{\frac{R_4}{R_3}}{\left(1 + \frac{R_4}{R_3}\right)} \cdot V_2 - \frac{R_2}{R_1} V_1 \right]$$

* If we choose $\frac{R_4}{R_3} = \frac{R_2}{R_1}$ then

ratio = ratio ✓
~~ratio~~
 Example: $\frac{R_4}{R_3} = \frac{R_2}{R_1}$
 Example: $\frac{10k}{10k} = \frac{10k}{10k}$



$R_{in} = R_1$ \rightarrow R_1 is in series with branch 1 \rightarrow $R_{in} = R_1 + R_3$ \rightarrow R_1 is in series with branch 1 \rightarrow $R_{in} = R_1 + R_3$ \rightarrow 2 branches \rightarrow $R_{in} = R_1 + R_3$

89

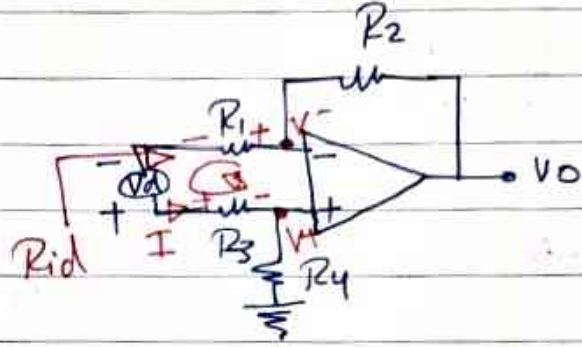
$$V_o = \frac{R_2}{R_1} = \frac{R_4}{R_3} (V_2 - V_1)$$

$$\therefore \frac{V_o}{V_2 - V_1} = A_d = \frac{R_2}{R_1} = \frac{R_4}{R_3}$$

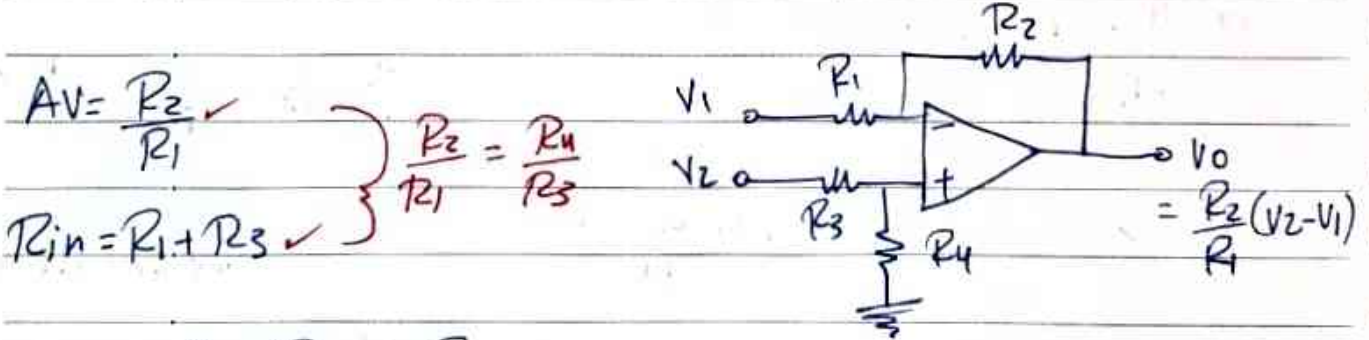
$$V_d = V_2 - V_1$$

$$-V_d + IR_3 + IR_1 = 0$$

$$\frac{V_d}{I} = R_d = R_1 + R_3$$



Ex:- Design a difference Amp. to have $R_{in} = 20k\Omega$ and $A_d = 500$.



To satisfy $\frac{R_2}{R_1} = \frac{R_4}{R_3}$

We can choose $R_1 = R_3$ & $R_2 = R_4$

$$\therefore R_{in} = R_1 + R_3 = 2R_1 = 2R_3$$

$$R_1 = R_3 = 10k\Omega$$

$$A_d = \frac{R_2}{R_1} = 500$$

$$R = \rho \frac{L}{A}$$

$$L_{5M} = 500 L_{10k} \text{ (pract. X)}$$

* To increase A_d , $R_{in} \Rightarrow R_2$ should be very big and that's undesired in Design \Rightarrow

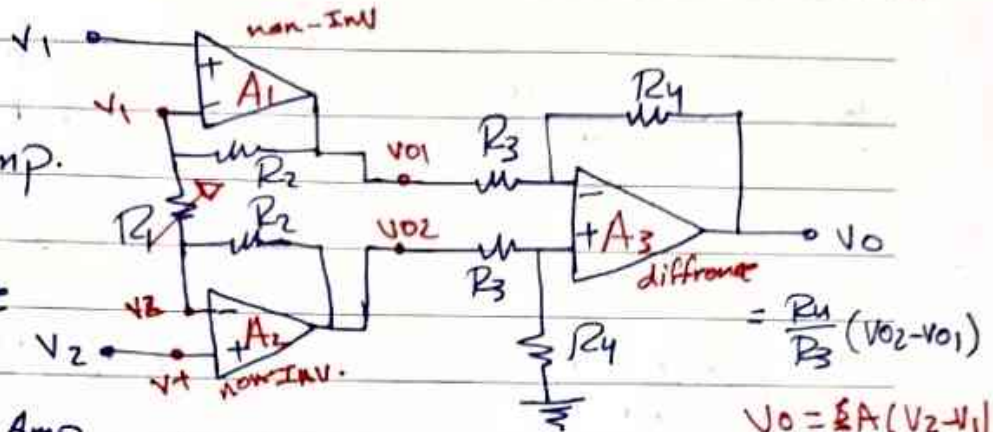
- ⇒ very High K_{in} , gain ⇒ adjustable
- ⇒ ~~single~~ single element dependent
- ⇒ using reasonable values 10 of Resistance (in $k\Omega$ range)

$$R_2 = 500 \times 10 = 5M\Omega$$

$$R_2 = R_4 = 5M\Omega$$

(VI) Instrumentation Amp.

- a) - contains:- difference Amp. → A_3
- Two non-Inverting Amp → A_1 & A_2



$$= \frac{R_4}{R_3} (V_{02} - V_{01})$$

$$V_0 = \frac{R_4}{R_3} (V_2 - V_1)$$

↳ desired o/p

[It is used to achieve, high, adjustable and single element dependent gain, also very high i/p Resistance values ($k\Omega$) range]

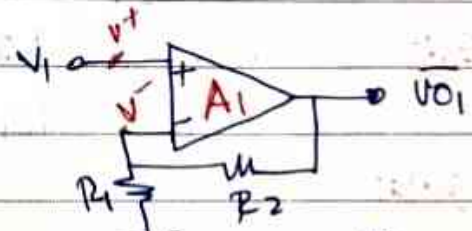
$$\Rightarrow V_0 = \frac{R_4}{R_3} (V_{02} - V_{01})$$

* using super position.

For A_1 :-

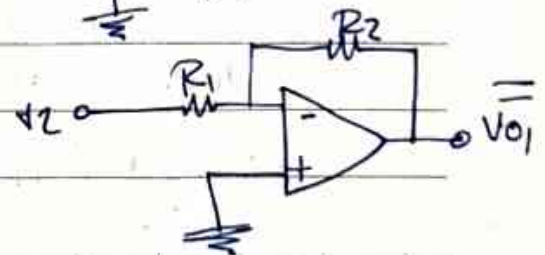
(I) effect of V_1 ($V_2 = 0$)

$$\bar{V}_{01} = \left(1 + \frac{R_2}{R_1}\right) V_1$$



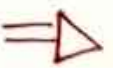
(II) effect of V_2 ($V_1 = 0$)

$$\bar{V}_{01} = -\frac{R_2}{R_1} V_2$$



$$\Rightarrow V_{01} = \bar{V}_{01} + \bar{V}_{01} = \left(1 + \frac{R_2}{R_1}\right) V_1 - \frac{R_2}{R_1} V_2$$

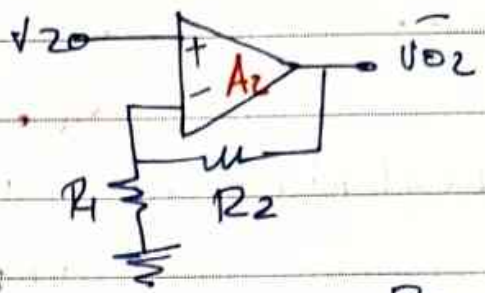
* R_1 → to control A (gain)



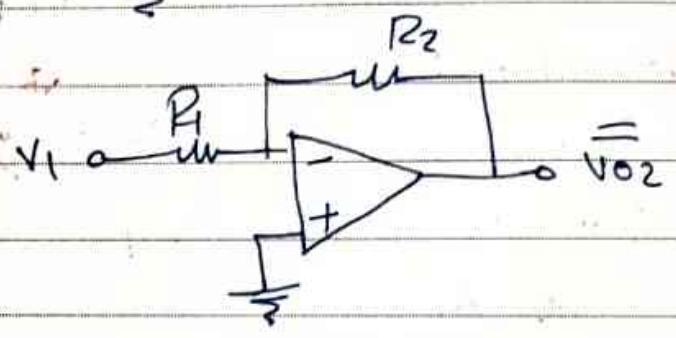
For A_2 :-

* $V_{O2} = \bar{V}_{O2} + \underline{V}_{O2}$

$\underline{V}_{O2} = \left(1 + \frac{R_2}{R_1}\right) V_2$



$\bar{V}_{O2} = -\frac{R_2}{R_1} V_1$



$\Rightarrow V_{O2} = \left(1 + \frac{R_2}{R_1}\right) V_2 - \frac{R_2}{R_1} V_1$

$\Rightarrow V_O = \frac{R_4}{R_3} \left[\left\{ \left(1 + \frac{R_2}{R_1}\right) V_2 - \frac{R_2}{R_1} V_1 \right\} - \left\{ \left(1 + \frac{R_2}{R_1}\right) V_1 - \frac{R_2}{R_1} V_2 \right\} \right]$

$V_O = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_1}\right) (V_2 - V_1)$

$\frac{V_O}{V_2 - V_1} = A_d = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_1}\right)$

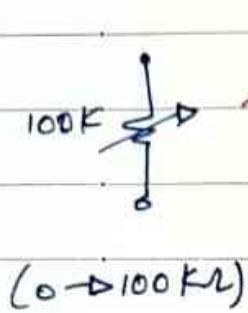
Ex:- Design an AI to have adjustable gain (5-500)
The max Resistor must Not exceed 100 k Ω .

Sol:-

$5 \rightarrow 500$
 $A_{min} \quad A_{max}$

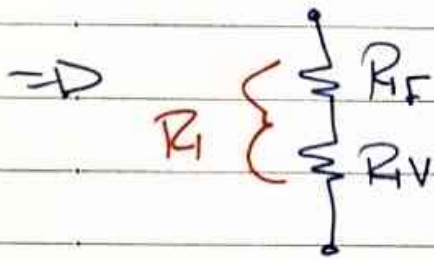
$A_d = \frac{R_4}{R_3} \left(1 + \frac{2R_2}{R_1}\right)$

Choose R_1 to be variable Resistor



but at $R=0 \Rightarrow A_d = \dots\dots\dots (1 + \frac{2R_2}{R_1})$

So the gain will equal ∞
 & the op-Amp enter the sat mode
 so I should separate R_1 into two
 Resistor's, one fixed & the other
 variable



* $A_{min} \rightarrow R_1 \text{ max}$

* $A_{max} \rightarrow R_1 \text{ min}$

Let R_{IV} to be a potenehometer of 100 k Ω

$$R_{1 \text{ max}} = R_{IF} + R_{IV} (\text{max}) = R_{IF} + 100 \text{ K}$$

$$R_{1 \text{ min}} = R_{IF} + R_{IV} (\text{min}) = R_{IF}$$

$$5 = \frac{R_4}{R_3} (1 + \frac{2R_2}{R_F + 100})$$

Let $\frac{R_4}{R_3} = 2$

$\frac{A_{min}}{R_{ratio}} > 1$
 او بجزئته

* انا صرت الجزئ

$$5 = 2 \left(1 + \frac{2R_2}{R_{1F} + 100} \right)$$

$$1.5 = \frac{2R_2}{R_{1F} + 100K}$$

$$2R_2 = 1.5R_{1F} + 150K \quad \text{--- (1)}$$

$$\Rightarrow 500 = 2 \left[1 + \frac{2R_2}{R_{1F}} \right]$$

$$249 = \frac{2R_2}{R_{1F}}$$

$$2R_2 = 249 R_{1F} \quad \text{--- (2)}$$

equating 1 & 2

$$1.5 R_{1F} + 150 = 249 R_{1F}$$

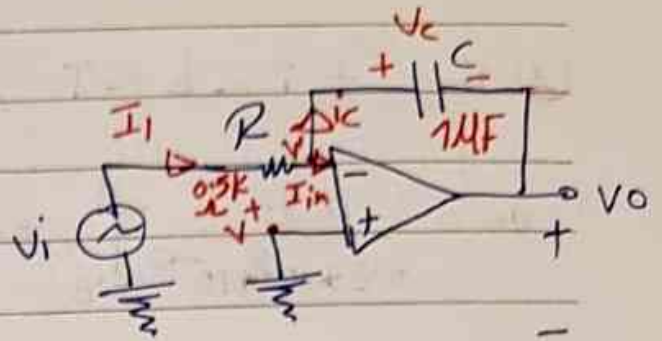
$$R_{1F} = \frac{150}{247} = 0.62 k\Omega$$

$$R_2 = \frac{249 * 0.62}{2} = 75 k\Omega$$

$$\text{Let } R_3 = 1 k\Omega$$

$$R_4 = 2 k\Omega$$

VII Integrator



$$I_1 = I_{in} + I_C$$

$$\frac{V_i - V^-}{R} = I_{in} + C \frac{dV_C}{dt}$$

$$V_C = V^- - V_O \rightarrow V_O = V_C$$

but for ideal OP-Amp

$$I_{in} = 0, V^+ = V^- = 0 \text{ (V.G)}$$

$$\Rightarrow \frac{V_i}{R} = -C \frac{dV_O}{dt} \Rightarrow dV_O = -\frac{V_i}{RC} dt$$

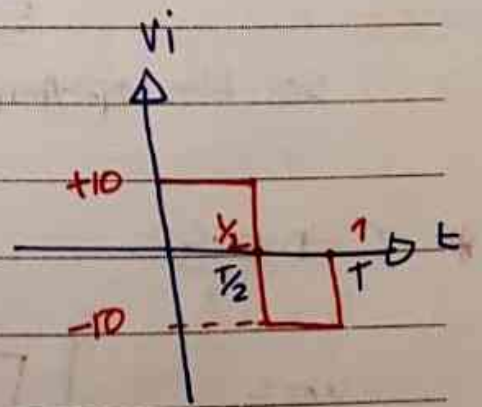
$$\int dV_O = \int -\frac{V_i}{RC} dt$$

$$\Rightarrow \underline{V_O = -\frac{1}{RC} \int V_i dt + K}$$

* Draw $v_o(t)$ for the input shown.

① For $0 < t < T/2 \Rightarrow V_i = 10V$

$$V_O = -\frac{1}{RC} \int_0^{T/2} 10 dt = -\frac{10t}{RC} \Big|_0^{0.5ms}$$



$$\Rightarrow V_O = -\frac{10t}{0.5 \times 10^3 \times 1 \times 10^{-6}} \Big|_0^{0.5ms}$$

$$F = 1KHz, T = \frac{1}{1K} = 1ms$$

$$V_O = \frac{-10 \times 10^3}{0.5} (0.5 - 0) \times 10^{-3} = \frac{-5}{0.5} = -10$$

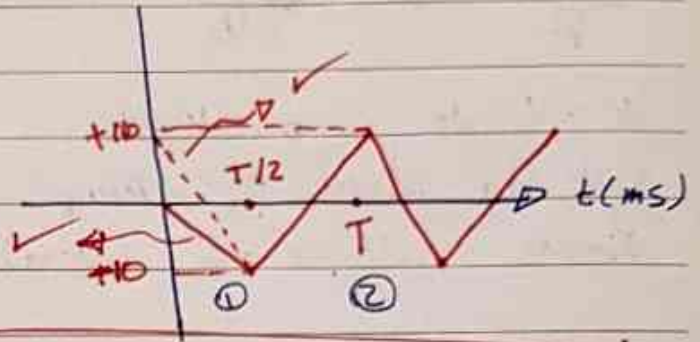
* $\frac{1}{RC} \Rightarrow$ Gain

* Amp & Integrate at the same time \Rightarrow Integrator

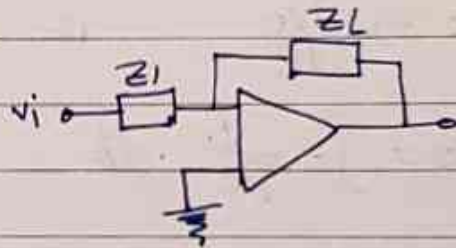
95

② For $\frac{1}{2}T < t < T$, $v_i = -10V$

$$v_o = \frac{10t}{0.5 \times 10^3 \times 10^{-6}} \Big|_{0.5}^1 = +10V$$



* $AV = -\frac{Z_2}{Z_1}$, $Z_1 \rightarrow R_1$



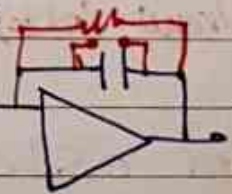
$$Z_2 = X_C = \frac{1}{2\pi f C}$$

f_c : - Low freq $\Rightarrow X_C = \infty$, $AV = \infty$

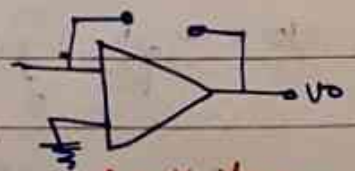
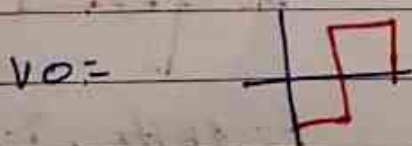
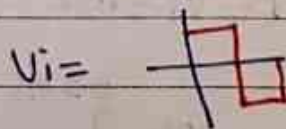
Loop parallel \Rightarrow Res. Res. \Rightarrow Res. \Rightarrow Res.

OC \neq C \Rightarrow OC \neq C

So the op-Amp in sat. \downarrow



* $C \rightarrow \underline{D} \rightarrow C$



Voltage comparator

* $C \rightarrow \underline{S} \rightarrow C$ \Rightarrow Buffer ($v_i \rightarrow$ Gnd)

* dc or very low freq. signal \Rightarrow not practical.

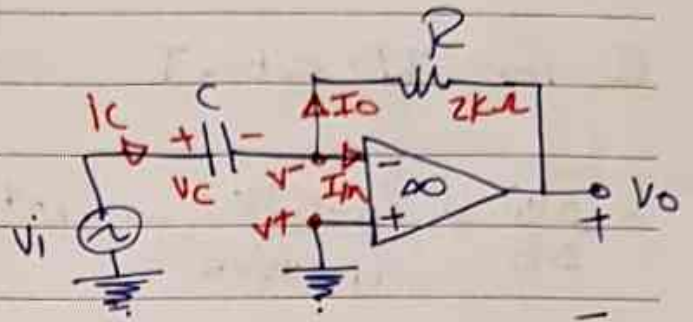
* v_{in} = very high freq. signal \Rightarrow problem (9.8)

96

(IX) Differentiator

$$i_c = I_o + I_{in}$$

$$c \frac{dv_c}{dt} = \frac{v^- - v_o}{R} + I_{in}$$



but $I_{in} = 0$, $v^- = v^+ = 0$ } ideal op-Amp.

$$v_c = v_i - v^- \Rightarrow v_c = v_i$$

$$\Rightarrow c \frac{dv_i}{dt} = -\frac{v_o}{R}$$

$$v_o = -Rc \frac{dv_i}{dt} \Rightarrow v_o \propto \frac{dv_i}{dt}$$

* Draw $v_o(t)$ for the shown $v_i(t)$.

(1) For $0 < t < T/2$

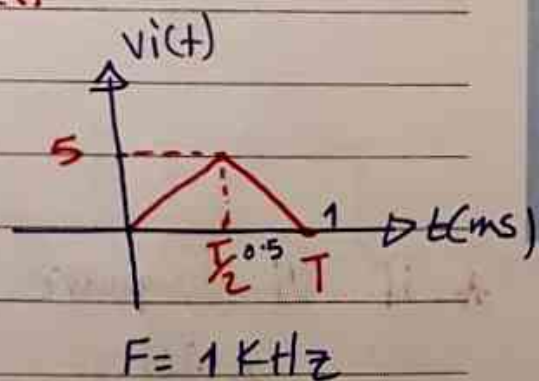
$$v_o = -Rc \frac{dv_i}{dt}$$

$$\frac{dv_i}{dt} = \frac{\Delta v_i}{\Delta t} = \frac{(5-0)V}{(0.5-0)mS}$$

$$= 10 \times 10^3 \text{ V/S}$$

$$\Rightarrow v_o = -2 \times 10^3 \times 1 \times 10^{-6} \times 10^4$$

$$v_o = -20 \text{ Volt.}$$

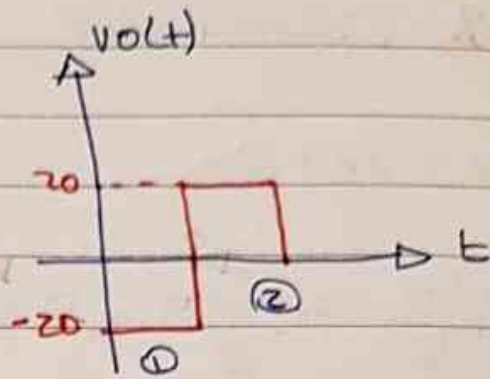


② For $T/2 < t < T$

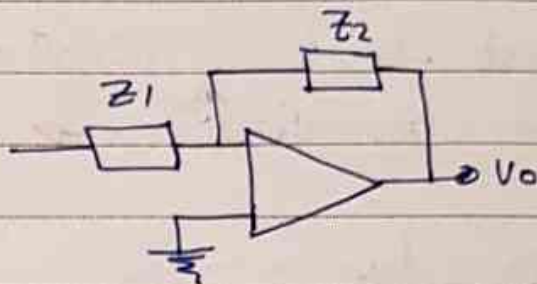
$$\frac{\Delta V_i}{\Delta t} = \frac{(0-5)V}{(1-0.5)ms} = -10^4 V/s$$

$$\Rightarrow V_o = -2 \times 10^3 \times 10^{-6} (-10^4)$$

$$V_o = +20 \text{ Volt.}$$

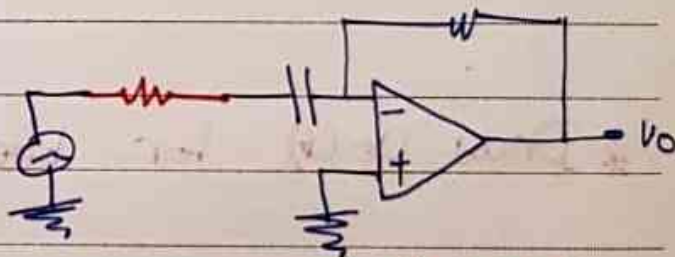


* $A_V = -\frac{Z_2}{Z_1}$



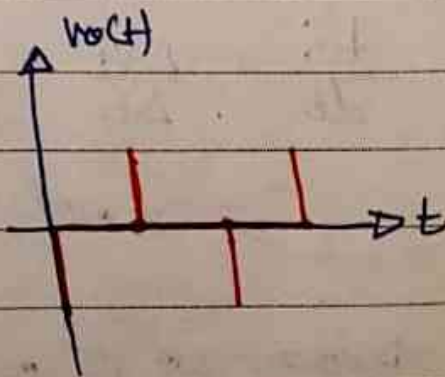
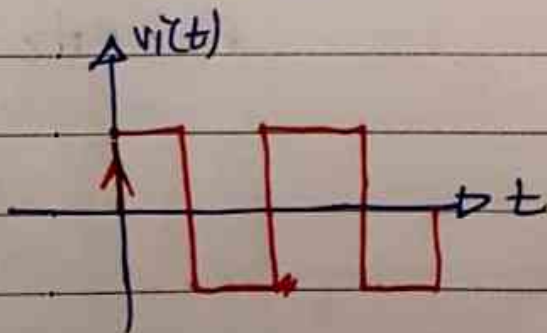
$$Z_1 = X_C = \frac{1}{2\pi f c}, \quad f_c :- \text{very big}$$

$$\therefore X_C = 0 \Rightarrow A_V = \infty$$



(practical diff.)

* if $V_i = \text{square}$



(Trigger)

Train Pulse

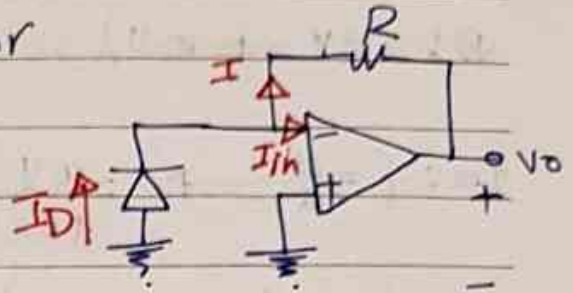


* ID ~
 تقيس التيار
 الضوء

98

(IX) current-to-voltage convertor

$V_o \propto I_D$



$I_D = I_{in} + I$

$I_D = I_{in} + \frac{V^- - V_o}{R}$

but $I_{in} = 0$, $V^- = V^+ = 0$ (V.G)

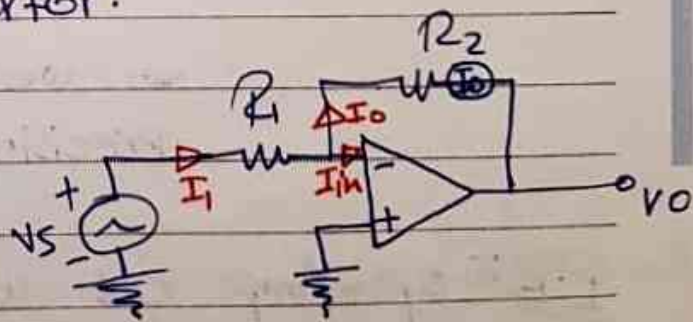
$\Rightarrow V_o = -R I_D$

I_D (mA)	V_o
1mA	-1V
2mA	-2V
3	-3
5	-5V

(X) Voltage-to-current convertor.

$I_1 = I_o + I_{in}$

$\frac{V_s - V^-}{R_1} = I_o + I_{in}$



for ideal op-Amp

$V^+ = V^- = 0$ (V.G), $I_{in} = 0$

$I_o = -\frac{V_s}{R_1}$

$I_o \propto V_s$

for $R_1 = 1k\Omega$



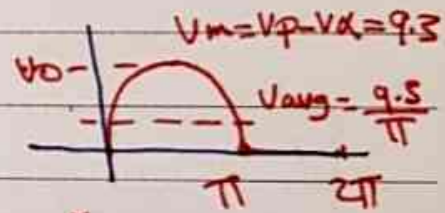
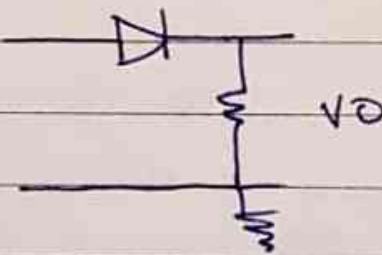
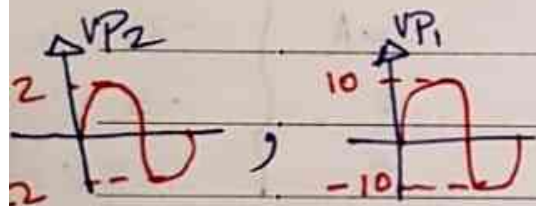
$V_S: (2V \rightarrow 10V)$

$I_D: (\frac{-2V}{1K} \rightarrow \frac{-10V}{1K})$

$I_o: (-2mA \rightarrow -10mA)$

Non Linear Applications

⊕ Precision Rectifier.



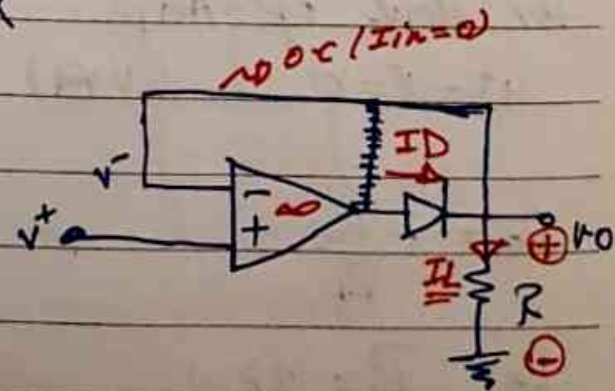
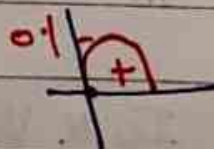
For V_{P1}
 For $V_{P2} \Rightarrow$ no Rectify because $V_P < V_D$

so we use Precision Rectifier

P.R: op-Amp circuit with Diodes used to Rectify A.C signal with $V_P < V_D$

P.HWR

⊕ during to +ve cycle

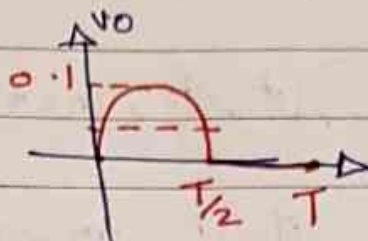


$\Rightarrow V_o = V_i \rightarrow +ve$ H.C, $i_L \downarrow$

* the op-Amp cancel the effect of VX when D-off

100

$i_L = i_D$, the loop will be closed and $v_o = v_i$

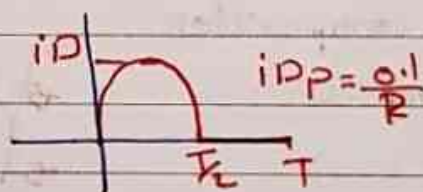
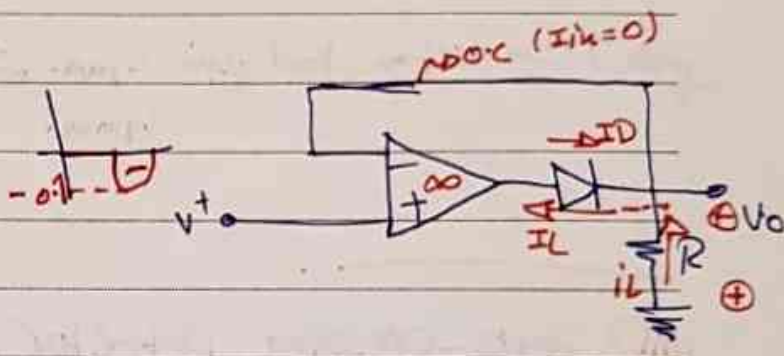


(I) For -ve Half cycle

$v_o = v_i \Rightarrow -ve$, so $i_L \uparrow$

$i_D = -i_L \Rightarrow D$ (D-off)

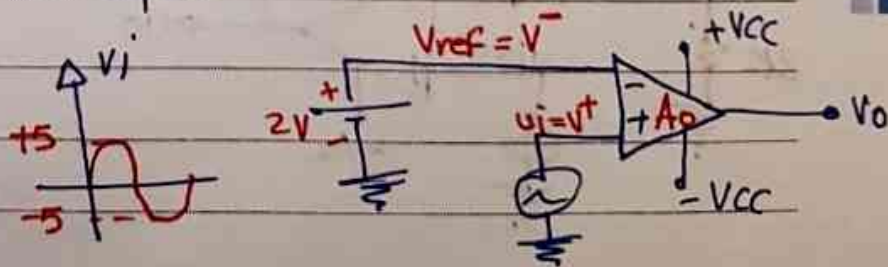
Loop is open $\Rightarrow v_o = 0$



(II) Voltage comparator

\rightarrow op-Amp works in open loop mode

$\rightarrow v_o = \mp V_{CC}$



v_d
 $v_o = A_o (v^+ - v^-)$

For Ideal op-Amp, $A_o = \infty$

(i) For $v^+ > v^-$, $v_d = +ve$, $v_o = +V_{CC}$

(ii) For $v^+ < v^-$, $v_d = -ve$, $v_o = -V_{CC}$

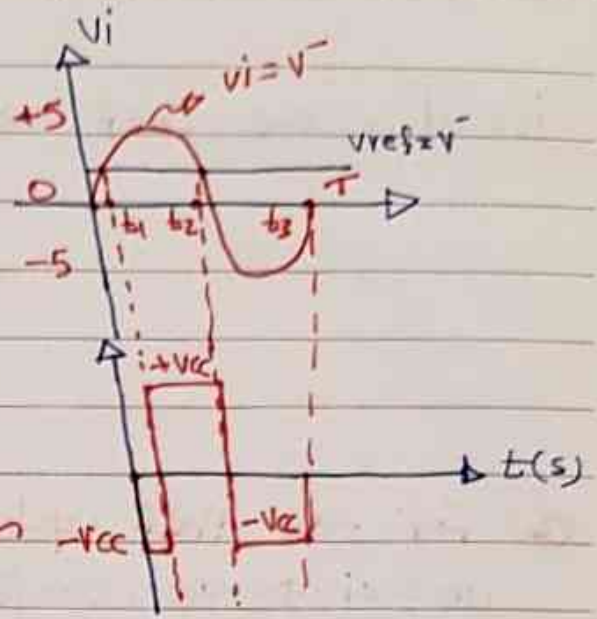
\Rightarrow

- * OP Amp - Open Loop
- * O/P -> symmetrical square wave
- * Zero crossing Detector [101] = volt. comp with $V_{ref} = 0$

① $0 < t < t_1$, $V^+ < V^-$, $V_o = -V_{CC}$

② $t_1 < t < t_2$, $V^+ > V^-$, $V_o = +V_{CC}$

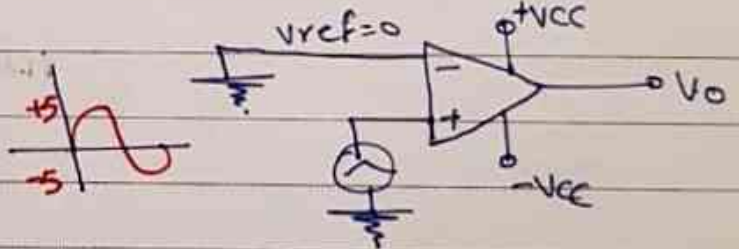
③ $t_2 < t < t_3$, $V^+ < V^-$, $V_o = -V_{CC}$



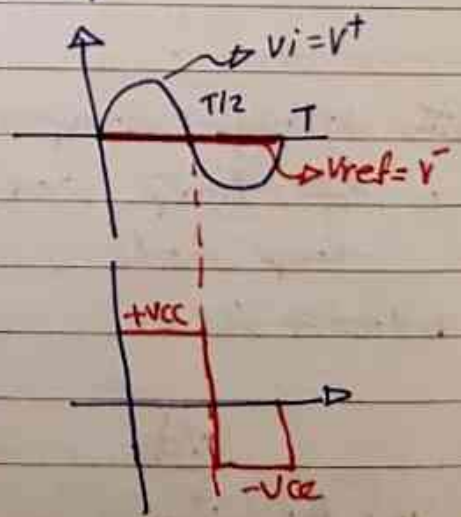
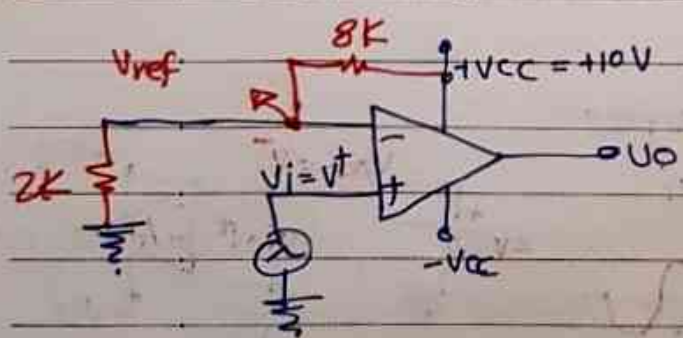
me) $V_{ref} = 0$ (as) comp. symm. \rightarrow symm.

III Zero-crossing Detector (sin \rightarrow square wave)

- * voltage comparator which $V_{ref} = 0$



- * If we add R's



$$\Rightarrow V_{ref} = \frac{10 * 2}{8 + 2} = 2V$$

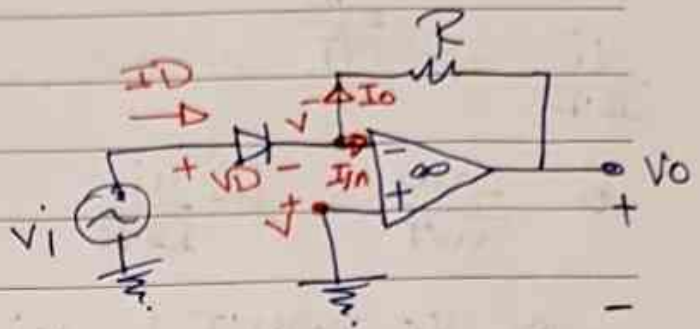
\rightarrow no connection with V_o

- * no connection between V_o & $V_{(in)}$
- * open loop $\Rightarrow V^+ \neq V^-$

IV Exponential Amp.

$$I_D = I_{in} + I_o$$

$$I_s e^{\frac{V_D}{nV_T}} = I_{in} + \frac{V - V_o}{R}$$



but $v^+ = v^- = 0$ (V-G) }
 $I_{in} = 0$

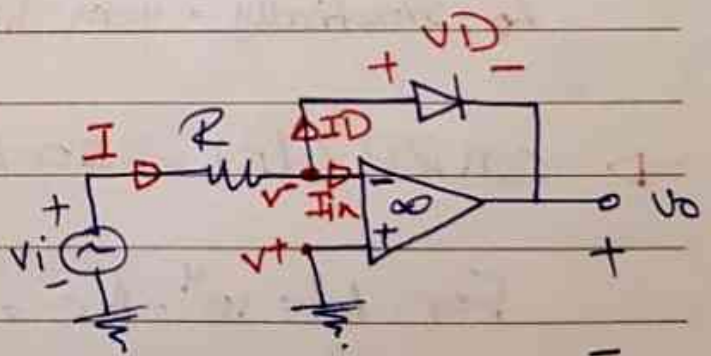
$$\Rightarrow V_D = v_i - v^- = v_i$$

$$I_s e^{\frac{v_i}{nV_T}} = -\frac{V_o}{R} \Rightarrow V_o = -I_s e^{\frac{v_i}{nV_T}} \cdot R$$

$n=1, V_T = 0.026V, I_s \rightarrow$ given

VI Logarithmic Amp.

$$I = I_D + I_{in}$$



$$\frac{v_i - v^-}{R} = I_s e^{\frac{V_D}{nV_T}} + I_{in}$$

but $v^+ = v^- = 0$ (V-G) }
 $I_{in} = 0$ ($R_i = \infty$) }

$$V_D = v^- - v_o = -v_o$$

$$\Rightarrow \frac{v_i}{R} = I_s e^{-\frac{v_o}{nV_T}}$$

$$\frac{V_i}{I_S \cdot R} = e^{\frac{-V_O}{nVT}}$$

$$\Rightarrow \frac{-V_O}{nVT} = \ln \frac{V_i}{I_S \cdot R}$$

$$\Rightarrow V_O = -nVT \ln \frac{V_i}{I_S \cdot R}$$

* C.M.R.R :- Common-mode-Rejection Ratio

→ given in data sheet

$$CMRR = \frac{A_d}{A_c}, \quad A_d :- \text{diff mode gain}$$

$A_c :- \text{common-mode gain}$

↳ Ideally = ∞

↳ Practically = very high #

$$\Rightarrow CMRR (dB) = 20 \log \frac{A_d}{A_c}$$

$$\text{For } A_d = 10^4, A_c = 0.1$$

$$CMRR (dB) = 20 \log \frac{10^4}{0.1}$$

$$= 20 \log 10^5$$

$$= \underline{\underline{100 \text{ dB}}}$$

* for this ckt $A_c = 0 \Rightarrow CMRR$ close to Ideal

* $CMRR_1 \rightarrow \text{Ideal}$ و $CMRR_2 \rightarrow \text{غير}$ → أفضل

* $CMRR_1 = 80$, $CMRR_2 = 100$, \geq best than $\frac{1}{2}$

Ex:- Given CMRR = 80 dB, $A_d = 10^3$, $A_c = ??$

Sol:-

$$80 = 20 \log \frac{A_d}{A_c}$$

$$\frac{80}{20} = \log \frac{A_d}{A_c} \Rightarrow 4 = \log \frac{A_d}{A_c}$$

$$\frac{A_d}{A_c} = 10^4 \Rightarrow A_c = \frac{10^3}{10^4} = 0.1$$

$$-10 + I_Z \cdot 2K + V_Z = 0$$

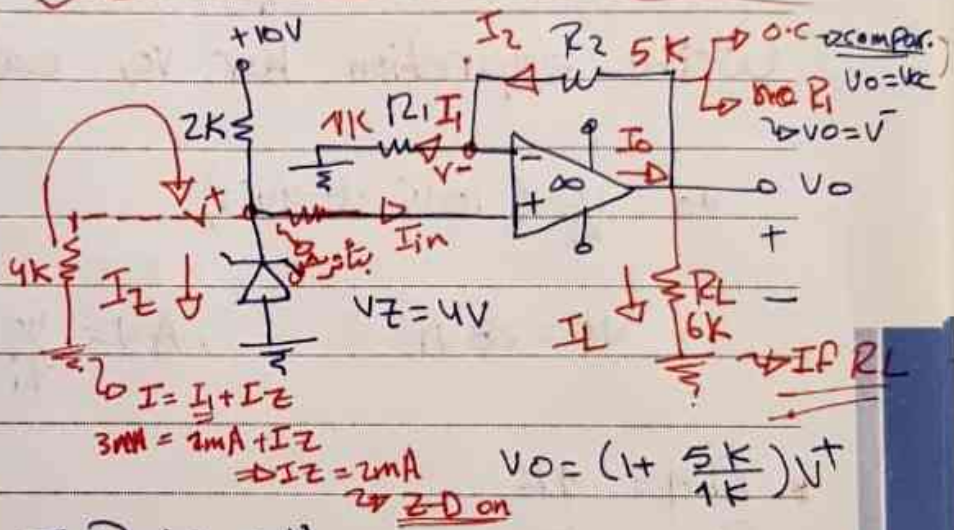
$$I_Z = \frac{10 - V_Z}{2K} = \frac{10 - 4}{2}$$

$$I_Z = 3mA$$

Since $I_Z > 0 \therefore Z-D$ is ON

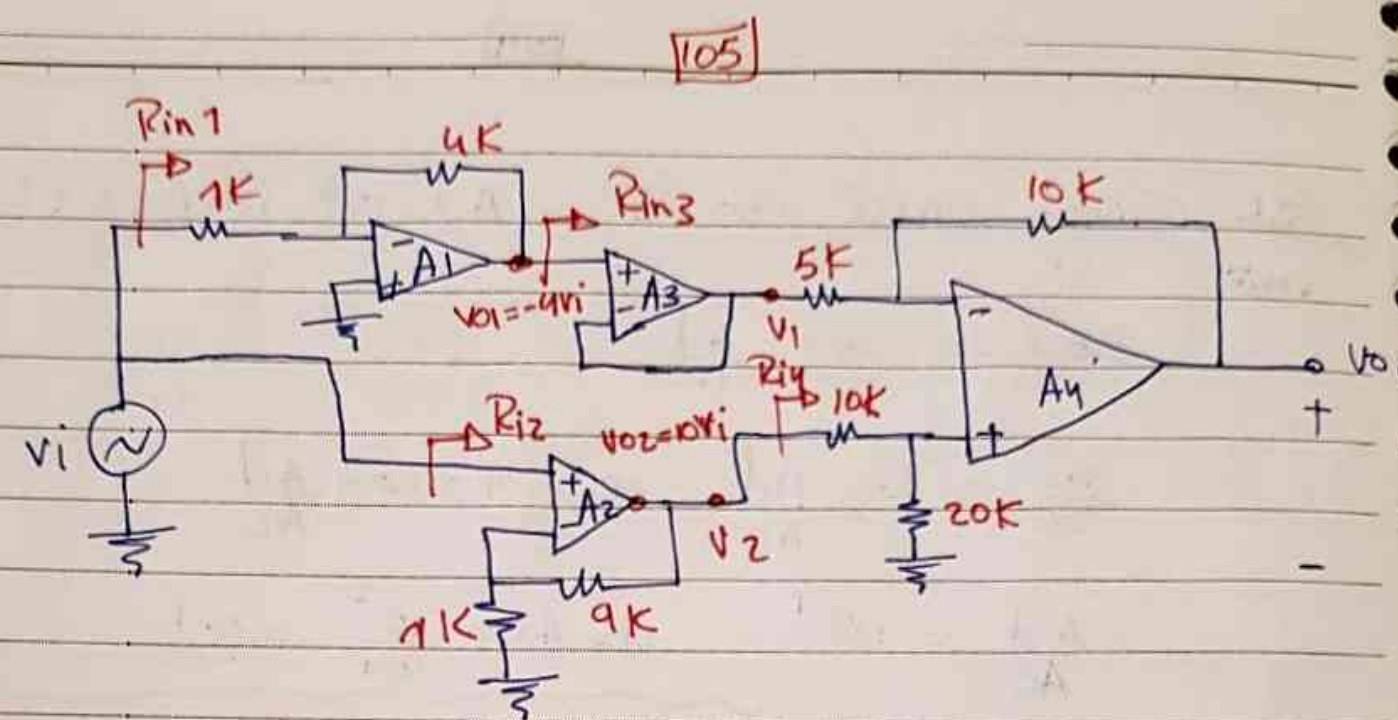
$$\Rightarrow V^+ = V_Z = 4V \quad \frac{1}{1} V_Z = 4V$$

↳ because Zener Diode is off



$V^+ = +10V$ off & $Z-D$ (1/1) *

Superposition's Ratio) 105



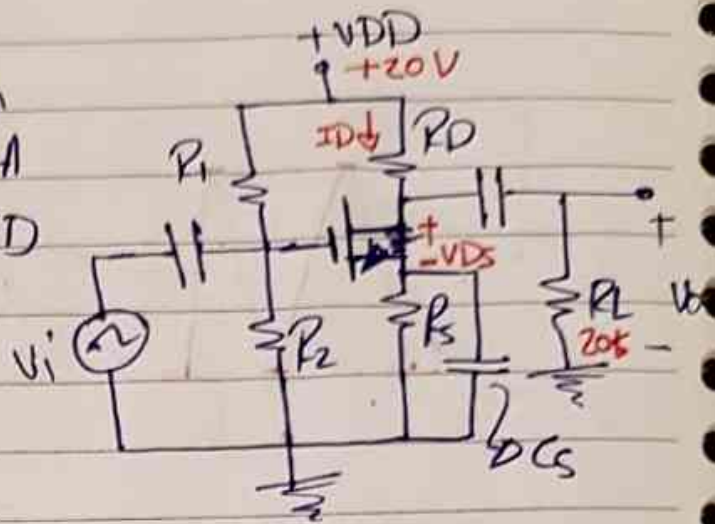
Write expression for v_o , calculate A_V .

$$v_o = \frac{10}{5} (10v_i - (-4v_i))$$

$$v_o = 28v_i, \quad A_V = \frac{v_o}{v_i} = 28$$

- * $R_{in1} = 1K$
- * $R_{in2} = \infty$
- * $R_{in3} = \infty$
- * $R_{in4} = 5 + 10$

Ex:- Design the ckt such
 1) - that $A_V = -8$, $I_{DQ} = 1\text{mA}$
 $V_{DSQ} = 10\text{V}$, $I_{DQ} = 10\% I_D$
 Find (R_D, R_S, R_1, R_2) ??
 2) - Draw s.s.A.c eq ckt
 & find R_i & R_o .



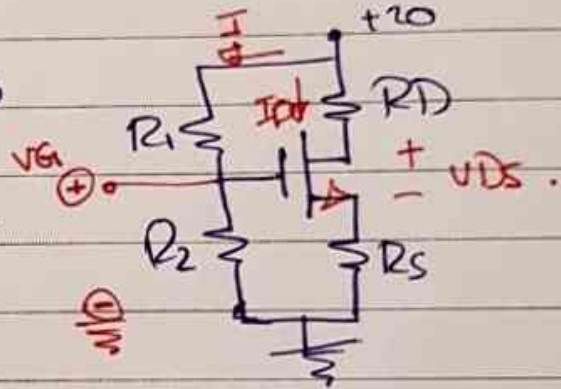
Sol:-

Given:- $V_{TN} = 1\text{V}$, $K_n = 1\text{mA/V}^2$

* From D-c

$$-20 + I_D R_D + V_{DS} + I_D R_S = 0$$

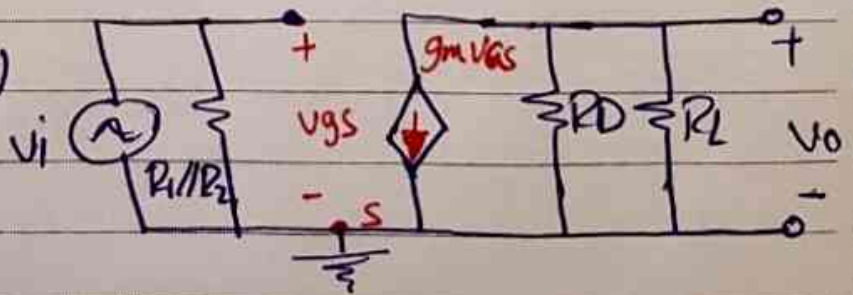
$$R_D + R_S = \frac{(20 - 10)\text{V}}{1\text{mA}} = 10\text{k}\Omega$$



* AC Analysis

$$A_V = \frac{V_O}{V_i} = -\frac{g_m V_{GS} (R_D \parallel R_L)}{V_{GS}}$$

$$\Rightarrow A_V = -g_m (R_D \parallel R_L)$$



$$g_m = 2\sqrt{K_n I_D} = 2\sqrt{1 \times 1} = 2\text{mA/V}$$

$$-8 = -2(R_D \parallel R_L) \Rightarrow (R_D \parallel R_L) = 4\text{k}\Omega$$

$$4 = \frac{R_D \cdot 20\text{k}}{R_D + 20} \Rightarrow R_D = \frac{20 \times 4}{20 - 4} = 5\text{k}\Omega$$

$$\therefore R_S = 10 - 5 = 5\text{k}\Omega$$

$$\text{if } R_{in} = 45$$

بدون R_{in} الجهد V_{GS}
في V_{GS} الجهد
الذي

$$\text{if } R_o = 5k \quad \text{بدون الجهد V_{GS}
في V_{GS} الجهد
الذي}$$

$$\Rightarrow R_o = R_D$$

107

$$I = 0.1 \text{ mA} = 0.1 \text{ mA}$$

$$-20 + I(R_1 + R_2) = 0$$

$$R_1 + R_2 = \frac{20}{0.1} = 200 \text{ k}\Omega$$

$$\Rightarrow R_2 = \frac{V_G}{I}$$

$$V_{GS} = V_G - V_S$$

$$\Rightarrow V_G = V_{GS} + V_S$$

$$* V_{GS} = V_{TN} + \sqrt{\frac{I_D}{K_n}} \\ = 1 + \sqrt{11} = \underline{2V} \text{ OR } \underline{0V}$$

$$* V_S = I_D \cdot R_S = 1 \text{ mA} \cdot 5 \text{ k}\Omega = \underline{5V}$$

$$\Rightarrow V_G = 5 + 2 = \underline{7V}$$

$$\Rightarrow R_2 = \frac{V_G}{I} = \frac{7V}{0.1} = 70 \text{ k}\Omega$$

$$R_1 + R_2 = 200 \text{ k}\Omega$$

$$\Rightarrow \underline{R_1 = 130 \text{ k}\Omega}$$

$$\boxed{*} \text{ D-c slope } \Rightarrow \frac{-1}{R_D + R_S}$$

$$\boxed{*} \text{ A-c slope } \Rightarrow \frac{-1}{R_D // R_L}$$

$$\boxed{*} R_{in} = R_1 // R_2 = 130 // 70 = \frac{130 \cdot 70}{200} = 45.5 \text{ k}\Omega$$

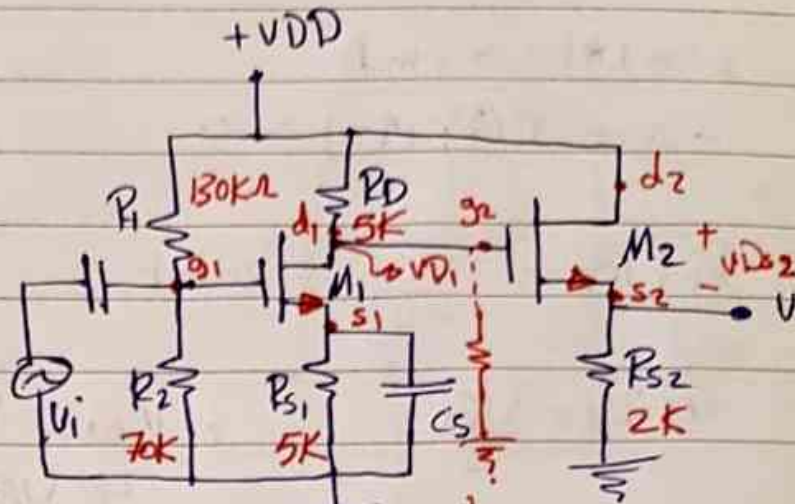
$$\boxed{*} R_o = R_D = 5 \text{ k}\Omega$$

=>

EX:-

- ① & ② → as the previous Ex.
- ③ I_{D2}, V_{DS2}
- ④ Draw s.s. A.c eq cct & Find A_{V2} ,

$$A_V = \frac{V_O}{V_i}$$



$$K_{n1} = K_{n2} = 1 \text{ mA/V}^2$$

$$V_{TN1} = V_{TN2} = 1 \text{ V}$$

$$\lambda_1 = \lambda_2 = 0$$

لو طيناهو $I_{D1} = I_{D2}$ في تفرق على الكمان

SOL:-

$$I_{D2} = K_{n2} (V_{GS2} - V_{TN2})^2$$

$$V_{GS2} = V_{G2} - V_{S2}$$

$$V_{S2} = I_{D2} \cdot R_{S2}$$

$$\Rightarrow V_{G2} = V_{D1} = 20 - I_{D1} R_{D1} \Rightarrow V_{G2} = 15 \text{ V}$$

$$V_{GS2} = 15 - 2 I_{D2}$$

$$I_{D2} = \frac{15 - V_{GS2}}{2} \Rightarrow \frac{15 - V_{GS2}}{2} = 1 (V_{GS2} - 1)^2$$

$$\Rightarrow = V_{GS2}^2 - 2V_{GS2} + 1$$

$$(2V_{GS2})^2 - 3V_{GS2} - 13 = 0$$

$$V_{GS2} = \frac{3 \pm \sqrt{9 + 104}}{4} \Rightarrow V_{GS2} = \frac{3 \pm 10.5}{4} = \underline{3.9 \text{ V}} \quad \checkmark$$

$$\Rightarrow V_{GS2} = \underline{3.9 \text{ V}}$$

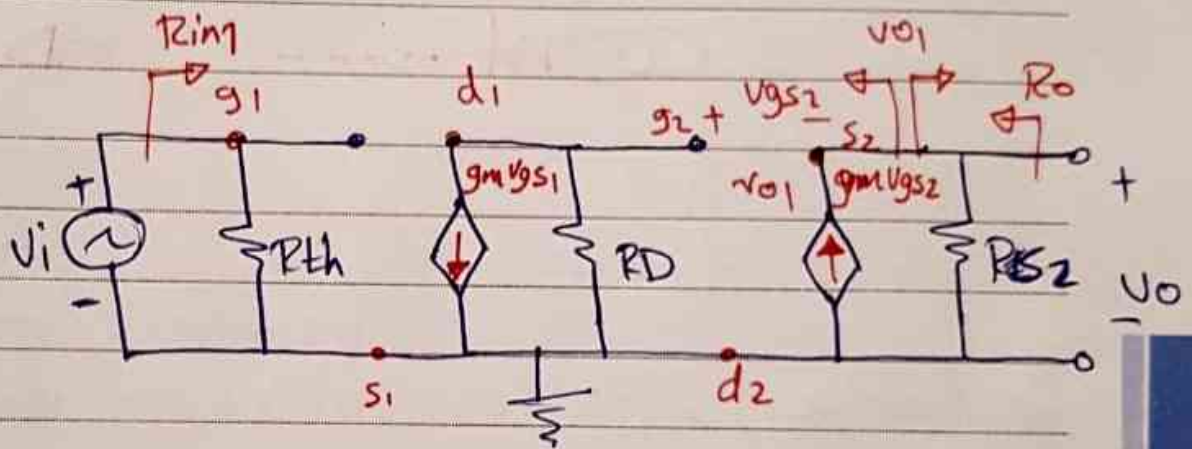
$\Rightarrow I_D = \frac{15 - 3.9}{2} \rightarrow I_D = 5.4 \text{ mA}$

$-20 + V_{D_{S2}} + I_{D2} R_{S2} = 0$

$V_{D_{S2}} = 20 - 5.4 \cdot 2 = 9.2 \text{ V}$

$V_{D_S}(\text{sat}) = V_{G_{S1}} - V_{T_{N1}}$

$\rightarrow V_{D_S}(\text{sat}) = 2.9 \text{ V}$



* $A_V > 1$

* $R_o \rightarrow \text{all } = R_{S2} \parallel \frac{1}{g_{m2}} \quad \underline{\underline{\text{C.D}}}$

* $\phi = 180^\circ$

* $R_{in2} = R_{Th}$

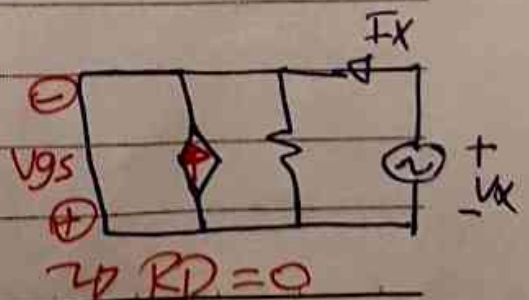
* $R_{o1} = R_D$

* $R_{in2} = \infty$

$\Rightarrow A_V = A_{V1} * A_{V2}$

$= -g_{m1} R_D \cdot \frac{g_{m2} R_{S2}}{1 + g_{m2} R_{S2}}$

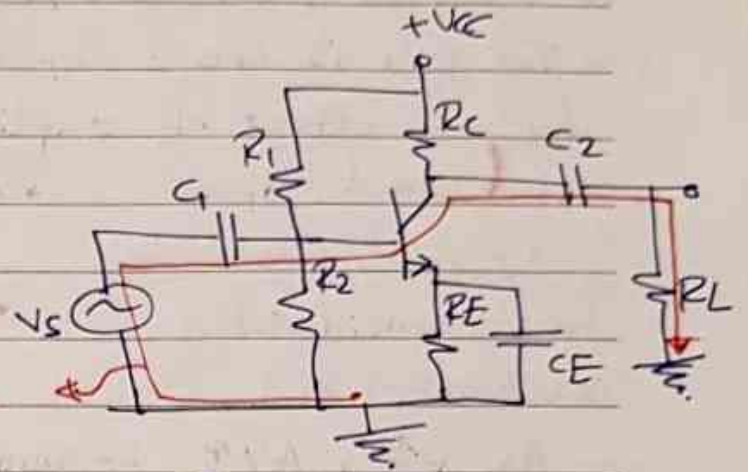
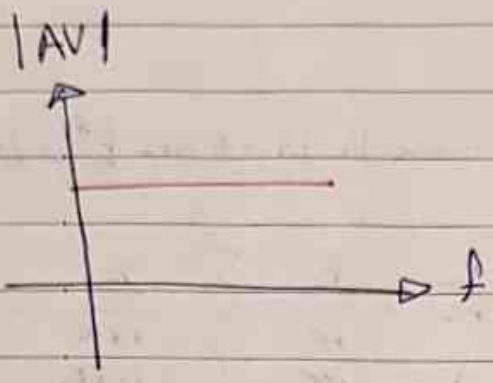
$\Rightarrow R_o = \left. \frac{V_X}{I_X} \right|_{V_i=0}$



frequency. \rightarrow 2nd Amp \rightarrow Gain \rightarrow $\frac{V_o}{V_s}$ \rightarrow $\frac{I_o}{I_s}$

* Any Amp. should have at least coupling or bypass capacitors 110

Frequency Response of Amp.



series path of input signal:

$\beta \checkmark, V_{BE} \checkmark.$

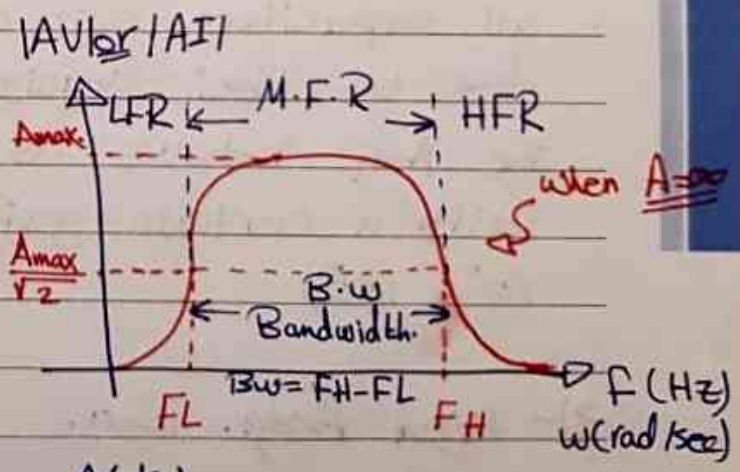
* F.R. :- Is a plot of Amp gain AV or AI versus frequency.

- The frequency can be in (Hz) or $\omega \rightarrow$ rad/sec

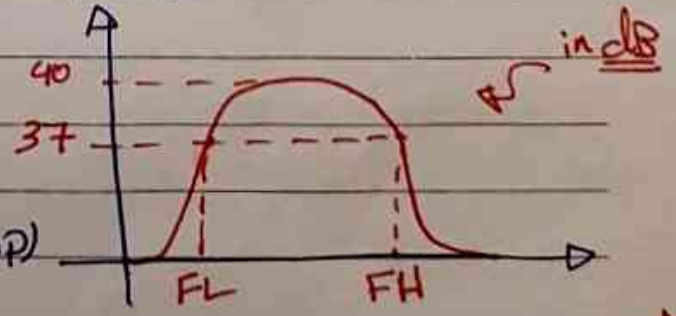
- The gain can be unitless

$$AV = \frac{V_o}{V_s}, \quad AI = \frac{I_o}{I_s}$$

in dB \rightarrow $AV(dB) = 20 \log \frac{V_o}{V_s}$
 $AI(dB) = 20 \log \frac{I_o}{I_s}$



A(dB)



* $A = \left| \frac{V_o}{V_s} \right|, \quad V_s = 2 \sin 2\pi ft$

\rightarrow so. V_o change equally with A, because $V_s = \text{cons. (Amp)}$

* in Low & high \rightarrow frequency dependent with AV \rightarrow
 \downarrow f_{KAU} \downarrow f_{KH} * In medium AV & f \rightarrow Independent

① Typical frequency Response has 3 main Regions.

1) - Low-freq Region. (LFR)

- extends from $(0 \rightarrow FL)$

- The gain is freq. dependant. such that as $f \uparrow$, $A \uparrow$ due to effect of coupling

$(C_1 \& C_2)$ and bypass

cap (C_E) , where they

have considerable

reactance (X_C)

* $X_C = \frac{1}{2\pi f C}$	<u>F</u>	<u>X_C</u>
	10	17K
* $X_C \propto \frac{1}{f}$	100	1.7K
	1K	170
	10K	17
	100K	1.7

- As $f \uparrow$, $A \uparrow$ because these caps are in the series path of input signal, as $f \uparrow$, $X_C \downarrow$, voltage drop across $X_C \downarrow$, $V_o \uparrow$, $A \uparrow$

2) - medium freq. Reg. (MFR)

- all capacitors are considered short cct.

due to their Negligible reactances $X_C \approx 0$,

The Amp behaves as a pure resistive Amp.

with a certain gain A_{vm} & a certain Phase $(0^\circ, 180^\circ)$

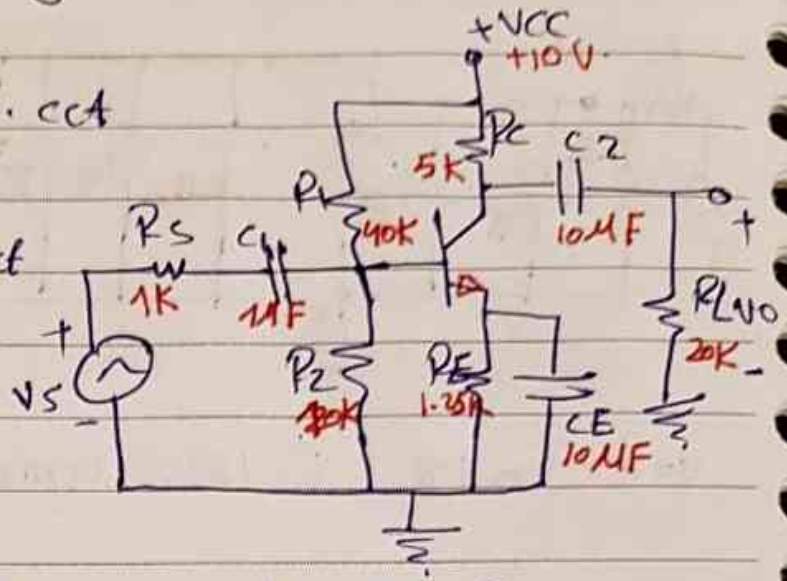
3) - High Freq. Reg. (HFR).

\Rightarrow

* at medium Reg. the capacitor's values (X_C) can be negligible.

II Frequency Response Analysis.

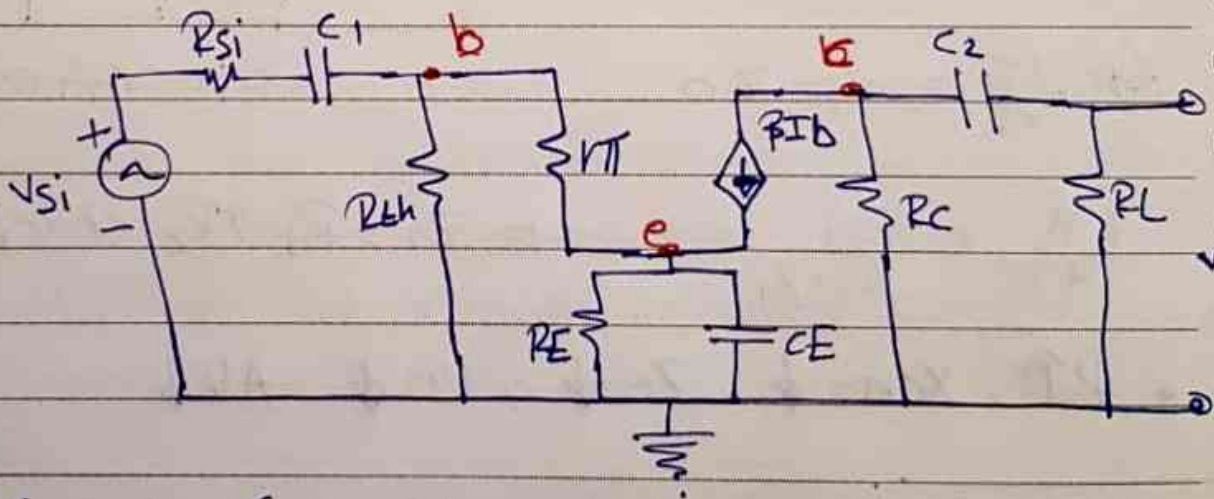
- 1) - Draw M.F.S.S.A.c eq. cct & Find A_{Vm} .
- 2) - Draw M.F.S.S.A.c eq. cct & Find f_L .
- 3) - Draw H.F.S.S.A.c eq. cct & Find f_H .
- 4) - Sketch Freq Response (Bode plot). [$A_V(dB)$ versus Freq.]



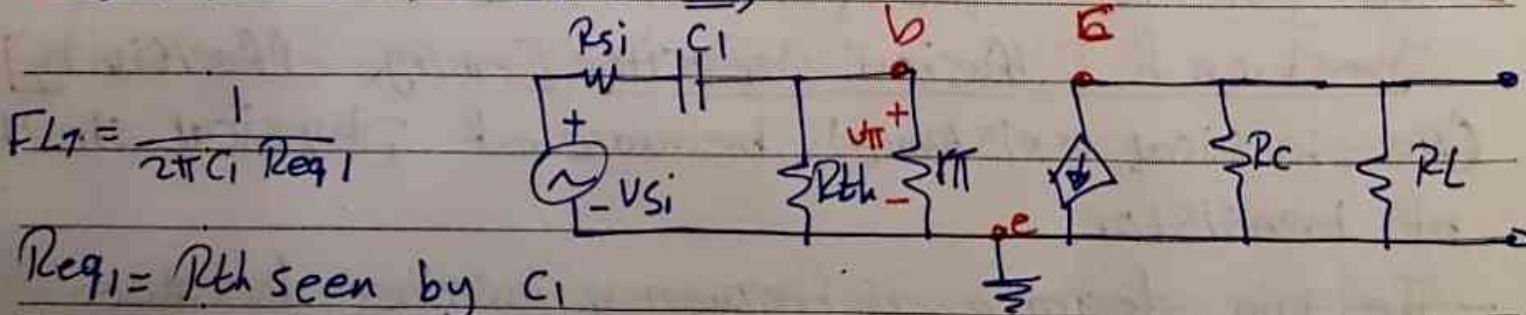
$\beta = 100, V_{BE} = 0.7V$
 $V_A = \infty, C_T = 20PF$
 $C_M = 5PF$

Sol:-

① $C_1, C_2, C_E = \text{Exist}, C_T, C_M = 0 (X_C = 0)$



I Effect of C_1 (C_2, C_E s.c)



$$f_{L1} = \frac{1}{2\pi C_1 R_{eq1}}$$

$R_{eq1} = R_{th}$ seen by C_1

$$Z_{in} R_{eq1} = [R_{si} + (R_{th} \parallel R_{\pi})], \quad R_{th} = R_1 \parallel R_2$$

$$R_{\pi} = \frac{\beta V_T}{I_{CQ}}$$



- * $C=0 \Rightarrow D.O.C$
- * $C=\infty \Rightarrow D.S.C$

114

P.C Analysis (to Find I_{CQ})

$$V_{th} = \frac{10 \times 10}{50} = 2V, \quad R_{th} = 8K\Omega$$

$$\Rightarrow I_B = \frac{(2 - 0.7)}{8 + 101 \times 1.25} = \frac{1.3}{13} = 0.01 mA, \quad I_{CQ} = 1 mA.$$

$$\Rightarrow r_{\pi} = \frac{100 \times 26}{1 mA} \Rightarrow R_{eq} = [1 + (9/12.6)] = 3K\Omega$$

$$\Rightarrow F_{L1} = \frac{1}{2\pi \times 1 \times 10^{-6} \times 3 \times 10^3} \Rightarrow F_{L1} = \frac{10^3}{20} \Rightarrow F_{L1} = 50 Hz$$

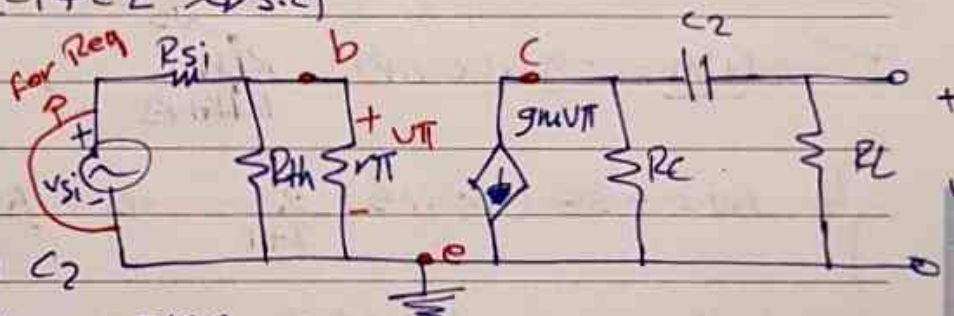
II Effect of C_2 (C_1 & $C_E \rightarrow D.S.C$)

$$F_{L2} = \frac{1}{2\pi C_2 R_{eq2}}$$

$R_{eq2} = R_{th}$ seen by C_2

$$\Rightarrow R_{eq2} = R_C + R_L = 25K\Omega$$

$$\Rightarrow F_{L2} = \frac{1}{2\pi \times 1 \times 10^{-6} \times 25 \times 10^3} \Rightarrow F_{L2} = \frac{10^3}{50\pi} = 6.4 Hz$$



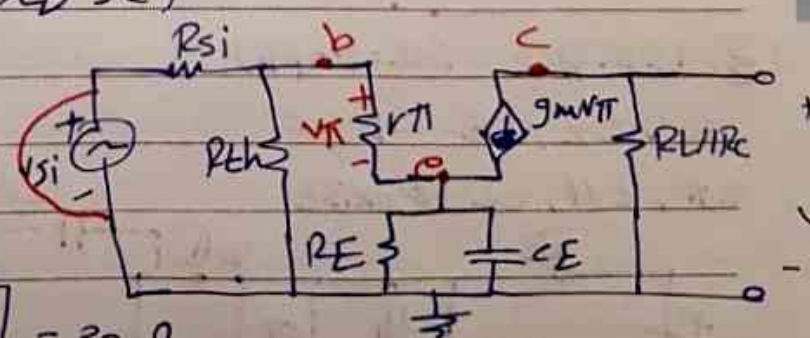
III Effect of C_E (C_1 & $C_2 \rightarrow D.S.C$)

$$F_{L3} = \frac{1}{2\pi C_3 R_{eq3}}$$

$R_{eq3} = R_{th}$ seen by C_E

$$R_{eq} = \left[\frac{(R_{si} \parallel R_{th}) + r_{\pi}}{\beta + 1} \parallel R_E \right] = 30 \Omega$$

$$F_{L3} = \frac{1}{2\pi \times 10 \times 10^{-6} \times 30} \Rightarrow F_{L3} = \frac{10^4}{20} = 500 Hz$$

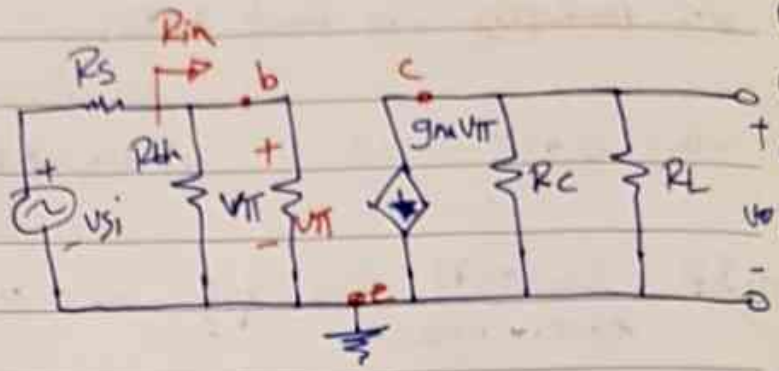


$\Rightarrow F_L$ is the high value = 500 Hz.

$\Rightarrow R_{eq}$

② M.F.R

$C_1, C_2, C_E \rightarrow \infty$ (s.c)
 $C_T, C_M \rightarrow 0$ (o.c)



$$A_V = \frac{V_O}{V_S} = \frac{V_O}{V_{TT}} \cdot \frac{V_{TT}}{V_S}$$

$$\rightarrow V_O = -g_m V_{TT} (R_C || R_L), \quad V_{TT} = \frac{V_S \cdot R_{in}}{R_s + R_{in}}$$

$$\rightarrow A_V = -g_m V_{TT} (R_C || R_L) \cdot \frac{V_S \cdot R_{in}}{R_s + R_{in}}$$

$R_{in} = R_{th} || r_{\pi}$

$R_{in} = 2$

$$\rightarrow A_{Vm} = -g_m (R_C || R_L) \cdot \frac{R_{in}}{R_s + R_{in}}, \quad g_m = \frac{I_{CQ}}{V_T} = \frac{1m}{26m} = \frac{38mA}{V}$$

$$\rightarrow A_V = -38 \left(\frac{20 || 5}{2+1} \right) = -100$$

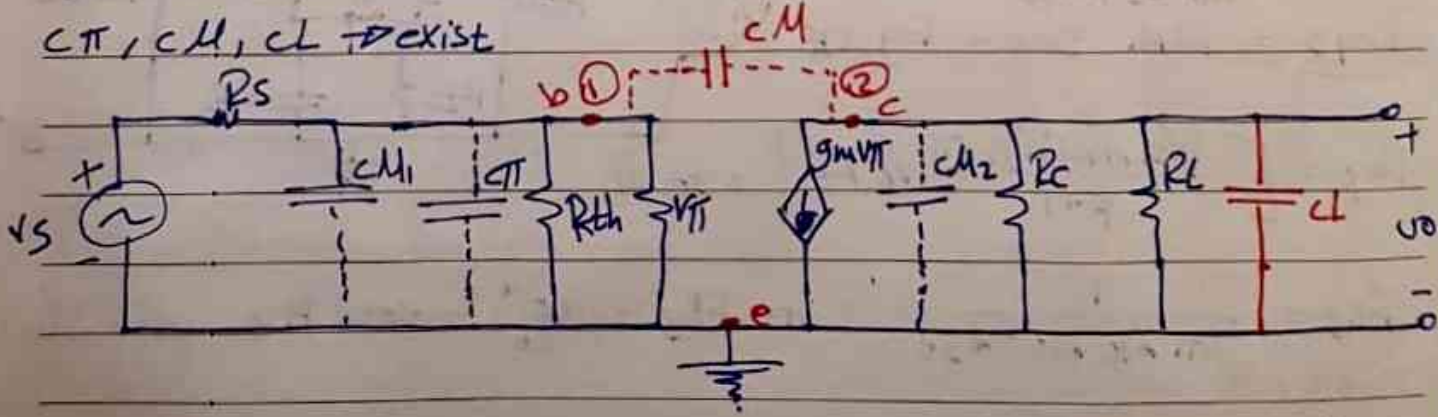
$$A_V(dB) = 20 \log(A_V) = 20 \log(100)$$

calc 200 x
 phase shift = calc 1 x

$$\rightarrow A_V(dB) = 40 dB$$

③ H.F.R (C_L = 200 pF)

$C_1, C_2, C_E \rightarrow$ s.c
 $C_T, C_M, C_L \rightarrow$ exist



$C_i = (C_{M1} + C_T)$... R_{in} ...

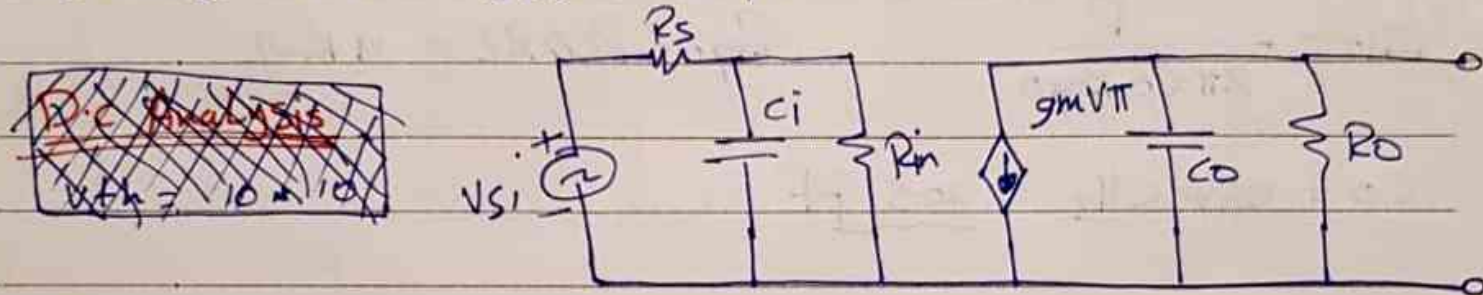
* $cM_1 = cM(1-K)$

* $cM_2 = cM(1-\frac{1}{K})$

* $K = \frac{V_2}{V_1} = \frac{V_O}{V_{\pi}} = \frac{-g_m V_{\pi} (R_C \parallel R_L)}{V_{\pi}} \Rightarrow K = -152$

$\Rightarrow cM_1 = 5(1 - (-152)) = 765 \text{ pF}$

$\Rightarrow cM_2 = 5(1 - (\frac{1}{-152})) = 5 \text{ pF}$



* $R_{in} = r_{\pi} \parallel R_{th} = 2 \text{ k}\Omega$

* $C_i = cM_1 + C_{\pi} = 785 \text{ pF}$

* $C_o = cM_2 + C_L = 205 \text{ pF}$

* $R_o = R_C \parallel R_L = 4 \text{ k}\Omega$

$\hookrightarrow F_{Hi} = \frac{1}{2\pi C_i R_{eq}}$ (effect of C_i)

$\hookrightarrow F_{Ho} = \frac{1}{2\pi C_o R_{eqo}}$ (co), R_{eqi} : R_{th} seen by C_i

$R_{eqi} = R_S \parallel R_{in} = 0.66 \text{ k}\Omega$

$\Rightarrow F_{Hi} = \frac{1}{2\pi * 0.66 * 785 * 10^{-12}} \Rightarrow F_{Hi} = \frac{10}{3140} = 0.3 \text{ MHz}$

$\Rightarrow F_{Ho} = 0.194 \text{ MHz}$

* نأخذ أقل F_H وهو 0.194 MHz الكوت بترية

*

$$f_{Hi} = \frac{1}{2\pi \cdot 0.7 \cdot 10^3 \cdot 785 \cdot 10^{-12}} \approx \frac{10^9}{1.4 \cdot 785 \cdot \pi}$$

$$\Rightarrow f_{Hi} = \frac{10^9}{3200} = \frac{10^7}{32} = \frac{0.298}{0.32} \cdot 10^6 = \underline{298 \text{ KHz}}$$

$$f_{H0} = \frac{1}{2\pi C_0 R_{eq0}} \quad , \quad R_{eq0} = R_C // R_L = 4 \text{ K}\Omega$$

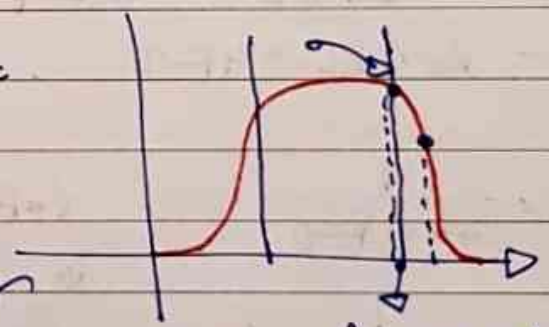
$$C_0 = C_L + C_{M2} = \underline{205 \text{ pF}}$$

$$f_0 = \frac{1}{2\pi \cdot 4 \cdot 10^3 \cdot 2.05 \cdot 10^{-10}} = \frac{10^7}{16\pi} = \underline{194 \text{ KHz}}$$

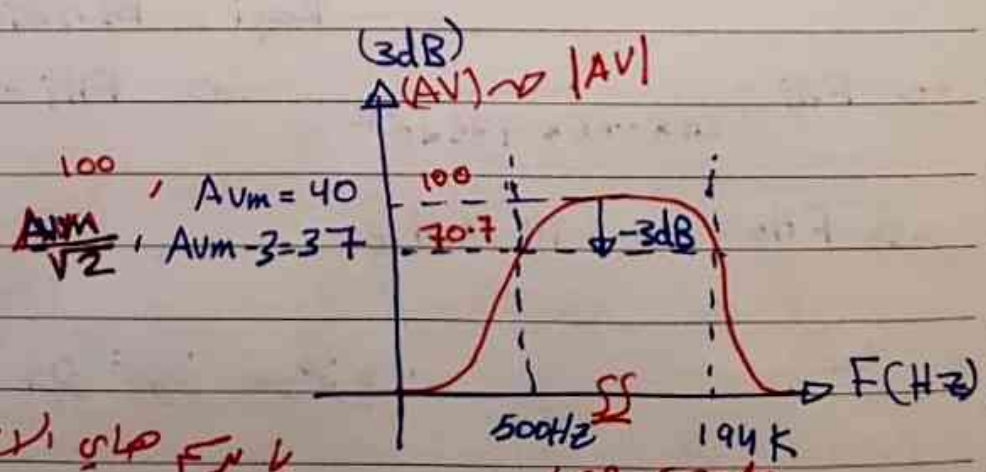
$\therefore f_H$ effective = the lowest value

$$\therefore f_H = 194 \text{ KHz}$$

دالة باؤ الاق



f_H effective.



Log. scale
 في رسم دالة باؤ الاق، f_H و f_L هما قيمتان على مقياس لوغاريتمي
 عند الرسم على مقياس لوغاريتمي، f_H و f_L هما قيمتان على مقياس لوغاريتمي

$$500 \text{ Hz} \text{ و } 194 \text{ KHz}$$

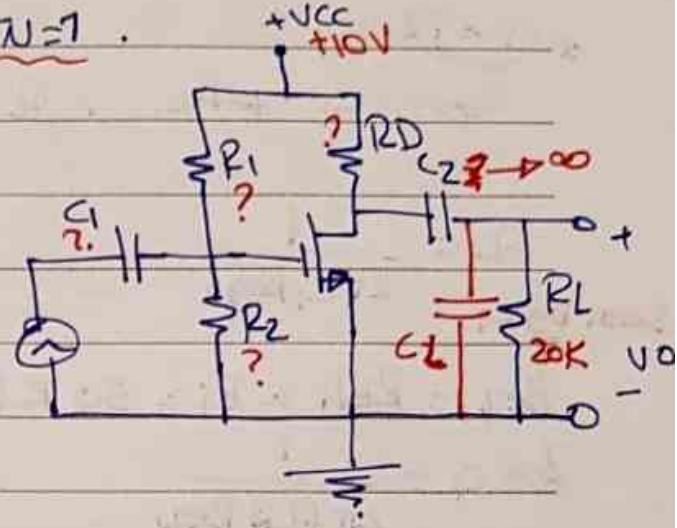
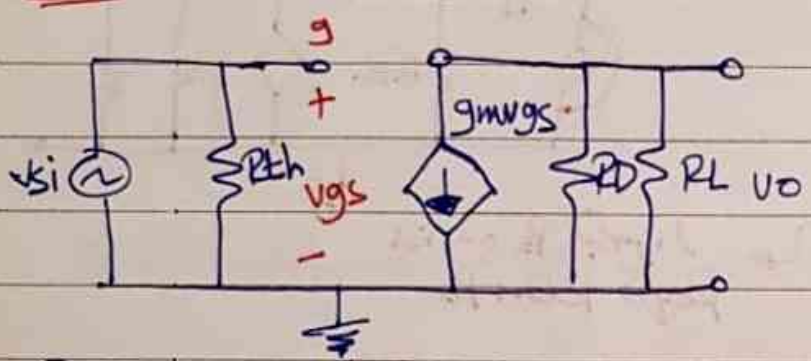
\Rightarrow

* Design the cct shown to have $f_L = 200 \text{ Hz}$
 $f_H = 500 \text{ kHz}$, $A_{vm} = 20 \text{ dB}$, $R_{in} = 50 \text{ k}\Omega$

Given $k_n = 1 \text{ mA/V}^2$, $I_D = 1 \text{ mA}$, $V_{TN} = 1$.

Sol:-

M.F.R



$\Rightarrow A_V = \frac{v_o}{v_{si}} = \frac{-g_m v_{gs} (R_D || R_L)}{v_{gs}} \Rightarrow A_V = -g_m (R_D || R_L)$

$\Rightarrow A_V (\text{dB}) = 20 \log A_V = 20 \text{ dB}$

$\therefore A_V = 10 = g_m (R_D || R_L)$, $g_m = 2\sqrt{k_n I_D} = 2 \text{ mA/V}$

$\Rightarrow R_D || R_L = 5 \text{ k}\Omega$ *no given*

$\Rightarrow R_D = \frac{5 \times 20}{20 - 5} = \frac{100}{15} \Rightarrow R_D = 6.66 \text{ k}\Omega$ ✓

$I_D = k_n (V_{GS} - V_{TN})^2$

$V_{GS} = V_{TN} \pm \sqrt{\frac{I_D}{k_n}} = 1 \pm 1 \Rightarrow 2 \text{ or } 0 \rightarrow V_{GS} = 2$ ✓

$\Rightarrow V_G = V_{GS} + V_S = 2 \text{ V}$ ✓ *o (and)*

$V_G = \frac{V_{DD} (R_2 + R_1)}{R_1 + R_2}$ *no Rin (given)*
 $\Rightarrow R_1 = \frac{10}{2} * 50 = 250 \text{ k}\Omega$ ✓

⇒

* Any cap. in parallel determine (FH)

* Any cap. in series \therefore (FL)

119

$$R_2 = \frac{250 \times 50}{250 - 50} = \frac{12500}{200} = 62.5 \text{ k}\Omega$$

* $C_1 = ??$

$\Rightarrow C_1 \rightarrow FL, CL \rightarrow FH$

$$FL = \frac{1}{2\pi C_1 R_{eq1}}$$

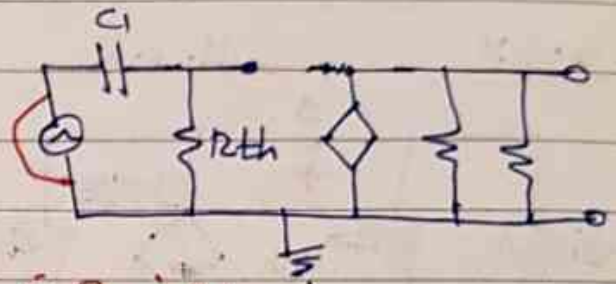
Seen by C_1

$$R_{eq1} = R_{th} = R_j = 50 \text{ k}\Omega$$

$$\Rightarrow C_1 = \frac{1}{2\pi f L R_{eq1}}$$

\Rightarrow $R_{eq} = R_{th} + R_s$

$$= \frac{1 \times 10^6}{2\pi \times 200 \times 50 \times 10^3} = \frac{1}{20\pi} \text{ MF} = 17 \text{ nF}$$

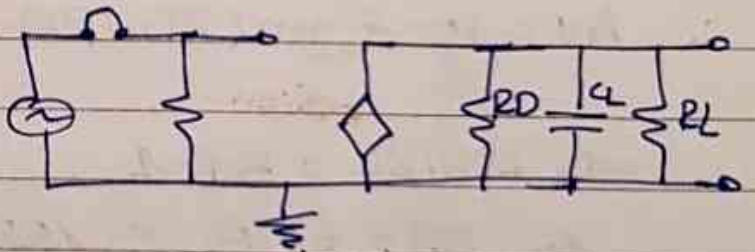


* $C_L = ??$

$$FH = \frac{1}{2\pi C_L R_{eq}}$$

seen by C_L

$$R_{eq} = R_D \parallel R_L = 5 \text{ k}\Omega$$



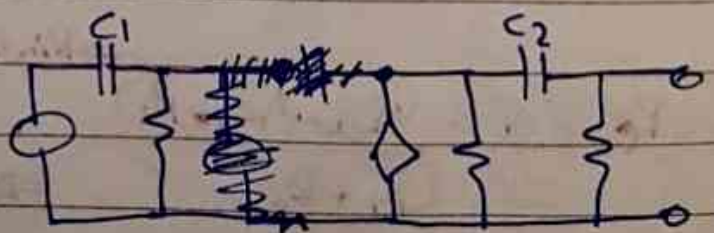
$$\Rightarrow C_L = \frac{1}{2\pi \times FH \times R_{eq}} = \frac{1}{2\pi \times 5 \times 10^5 \times 10^2} = \frac{10^{-8}}{50\pi} = \frac{10^{-8} \times 10^{12}}{50\pi}$$

$$C_L = 630 \text{ pF}$$

* if C_2 has a value

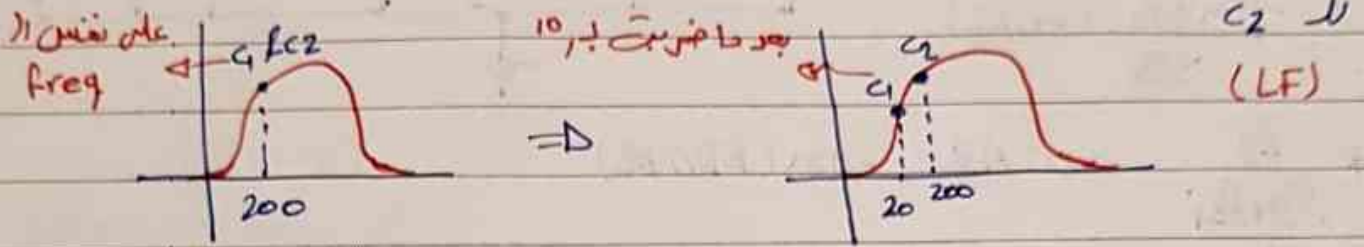
$$C_2 = \frac{1}{2\pi f L R_{eq2}}$$

$$R_{eq2} = R_D \parallel R_L$$

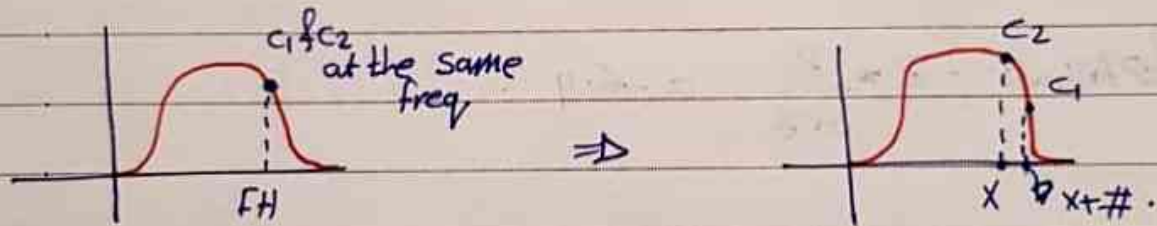


$$C_2 = \frac{10^6}{2\pi \times 200 \times 26.6 \times 10^3} = \frac{10^4}{106\pi} \approx 30\mu F$$

* تكون بدني اثنى ال (C2) و يضرب C1 بـ 10 و يترك ال FL تكون



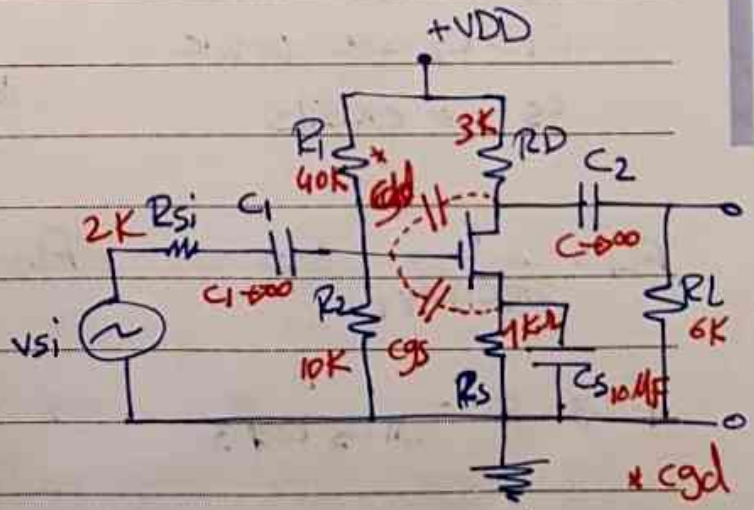
* ال (HF) بدني اثنى ال (C2) او ال cap بدني ال (LF) و يقسم ال الثانيه على ال 10
 ال ال HF تزيده لاني انا ال HF



* Freq. Resp. of Mosfet Amp.

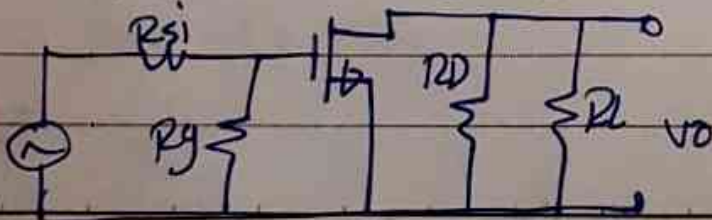
$I_D = 2mA, C_{gs} = 5PF, C_{gd} = 2PF$

- 1)- Draw M.F.S.S. eq cct & Find V_m
- 2)- " L.F.S.S. " " " " " F_L
- 3)- " H.F.S.S. " " " " " F_H
- 4)- Sketch Bode plot of Amp.



Sol:-

① $C_1, C_2, C_S \rightarrow S-C, C_{gd}, C_{gs} \rightarrow O-C$ $K_n = 2mA/V^2$

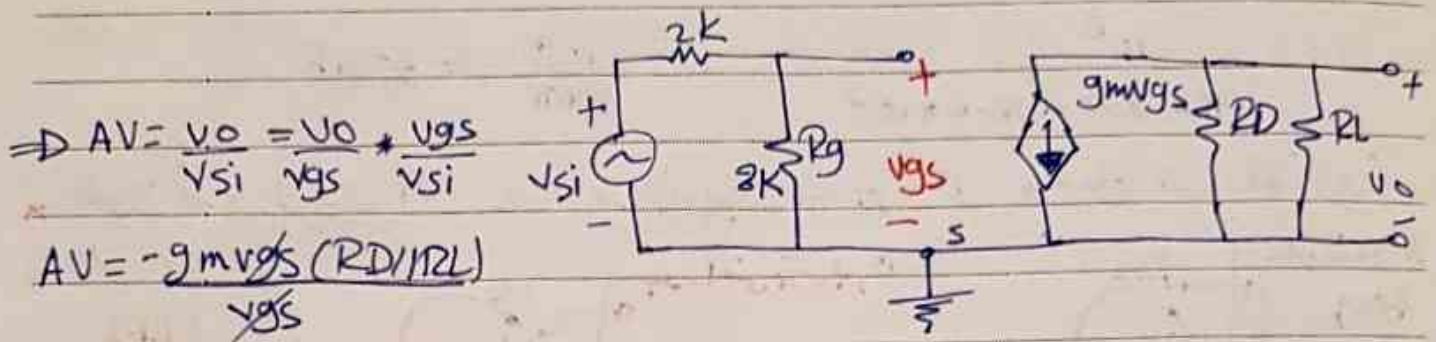


\Rightarrow

* $c_{gd} \rightarrow CM$

* $c_{gs} \rightarrow CII$

[12]



* $\frac{R_g}{R_g + R_{Si}} \Rightarrow AV = -g_m (R_D || R_L)$

* $g_m = 2\sqrt{knID} = 4 \frac{mA}{V^2}$

$\hookrightarrow \frac{V_O}{V_{GS}} [-(2\sqrt{knID})(3||6)] = -8$

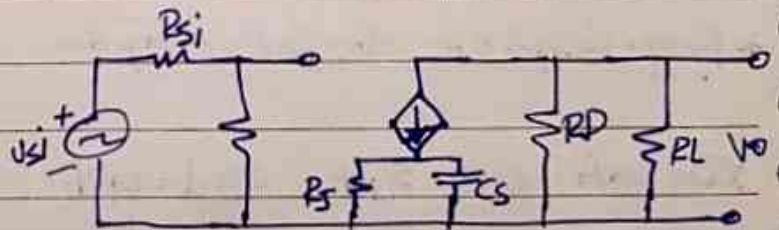
$\hookrightarrow AV_m = \frac{-8 * 8}{2+8} = -6.4$

② L.F.R

$\hookrightarrow c_{gd} = c_{gs} = 0 \Rightarrow DO.C$

$C_1 = C_2 = 0 \Rightarrow DSC$

C_s no exists



$FL_1 = \frac{1}{2\pi C_1 R_{eq1}} = 0$, $FL_2 = \frac{1}{2\pi C_2 R_{eq2}} = 0$

$FL_3 = \frac{1}{2\pi C_S R_{eq3}}$, $R_{eq3} :- R_{th}$ seen by C_S
 $R_{eq} = R_S$



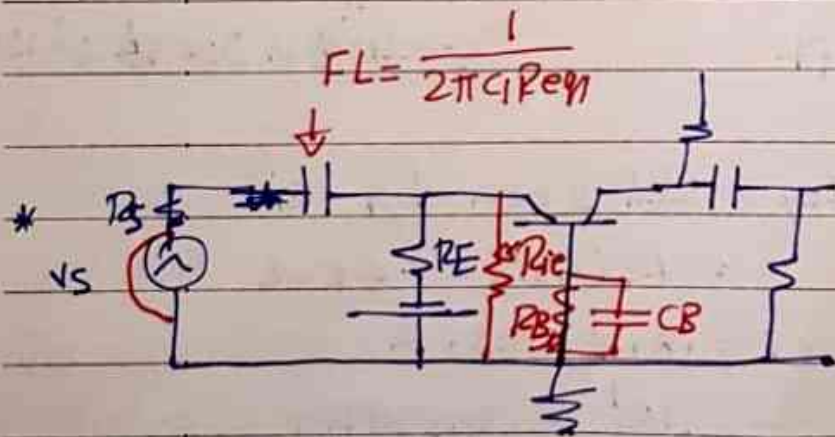
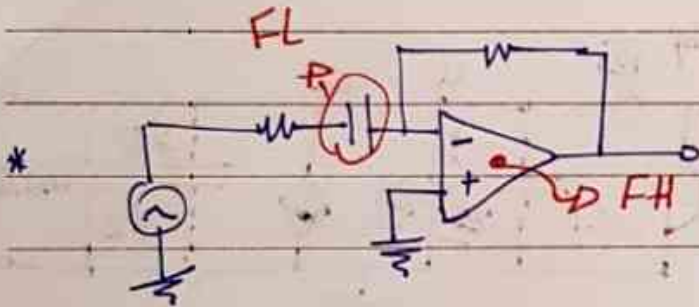
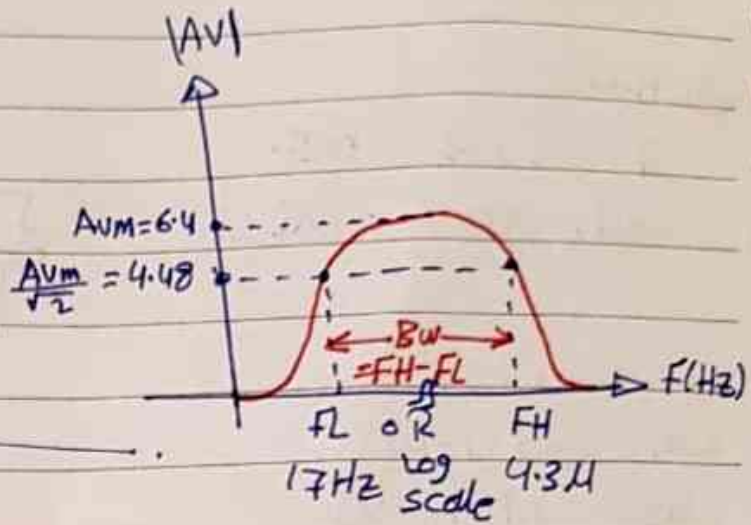
* any cap in parallel \Rightarrow High freq. (in Low & medium I consider it open ckt)

* frequency Response for C.S & C.E \rightarrow

no 03/6/21 *

123

(4)

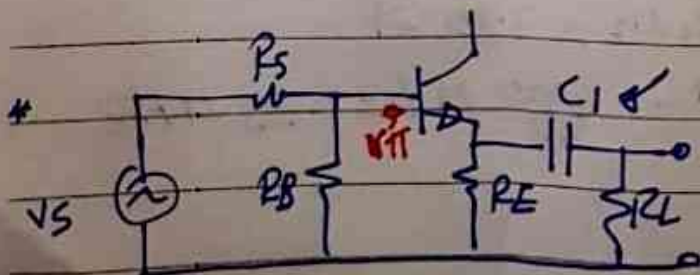


$R_{eq} = R_{ic} \parallel R_E + R_S$
 $R_{ic} = \frac{r_{\pi}}{\beta + 1}$

* if R_B & C_B exist.

$\Rightarrow FL_B = \frac{1}{2\pi C_B R_{eq}}$

$R_{eq} = (R_S \parallel R_E)(\beta + 1) \parallel r_{\pi} \parallel R_B$



$\Rightarrow R_{eq} = \left[\frac{(R_S \parallel R_B) + r_{\pi}}{\beta + 1} \parallel R_E \right] + R_L$