



تقدم لجنة EICoM الاكاديمية

دفتر لمادة:

الالكترونيات القوي

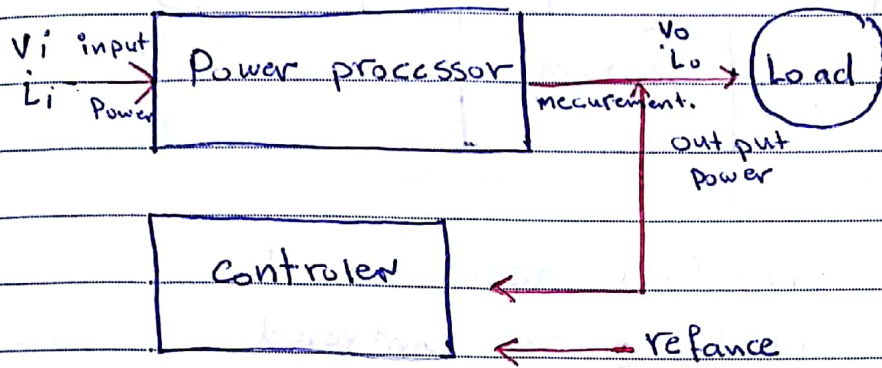
من شرح:

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جزيل الشكر للطالبة:

روند قطيشات





Block Diagram of PE System.

* power processor

1. dc (constant).

- (a) regulated magnitude.
- (b) adjustable "

2. Ac

- (a) constant frequency adjustable magnitude.
- (b) adjustable frequency, adjustable magnitude.

power Converters.

Inverter

rectifier.

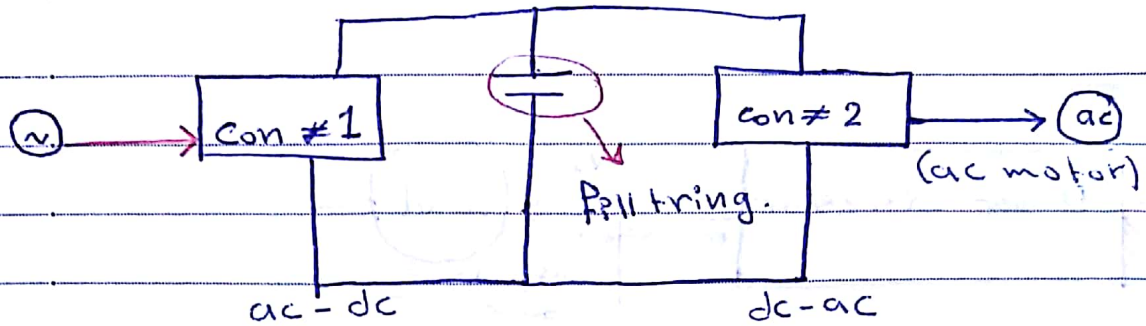
1- ac to dc \Rightarrow rectifier

2- dc to ac \Rightarrow inverter

3. dc to dc \Rightarrow converter

- \rightarrow set up
- \rightarrow set down
- \rightarrow set up - set down
- \rightarrow full bridge

4- ac to ac \Rightarrow rectifier + inverter.



* Converters are classified according to how the switches within it are controlled

1 - Line Frequency converter the switches within the converter are turned on and off at the line frequency (50 Hz) (Diode) \Rightarrow on and off by the nature of the input power.

2 - Switched (forced-commutated) converter :-
The switches within the converter are turned on and off at frequencies much higher than the line frequency (5 kHz - 25 kHz) using additional (external) control signal.

* Overview of power Semiconductor Switches :-

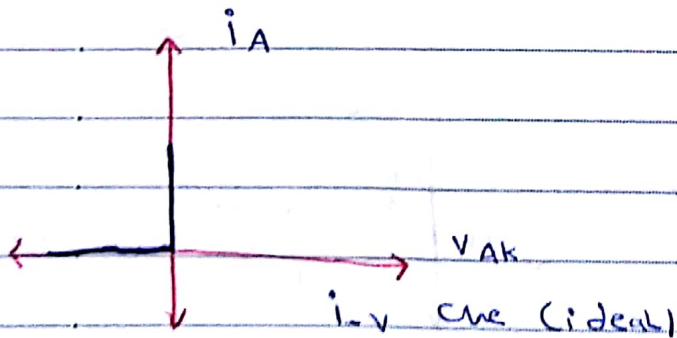
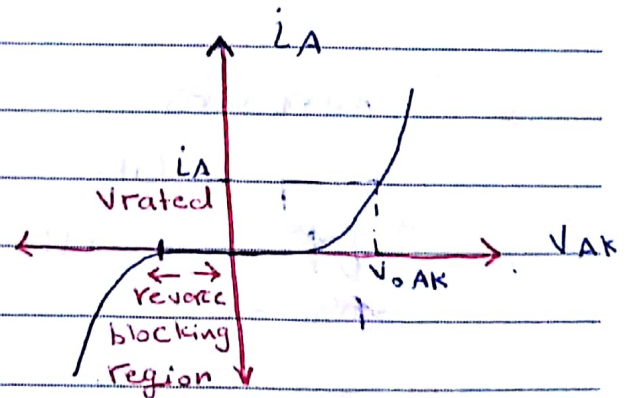
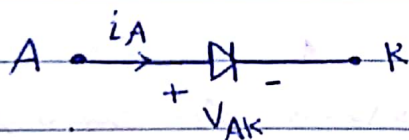
According to the degree of controllability, Power Semiconductor devices can be classification.

1- Diode :- on and off by the nature of the input voltage. (uncontrolled)

2- Thyristors :- on by additional ^{control} signal and off by the nature of the ~~input~~ ^{supply} source. (Semi-controlled)

3- controlled switches :- on and off by external (additional) signals (controlled).
(BJT, IGBT, MosFET, GTO).

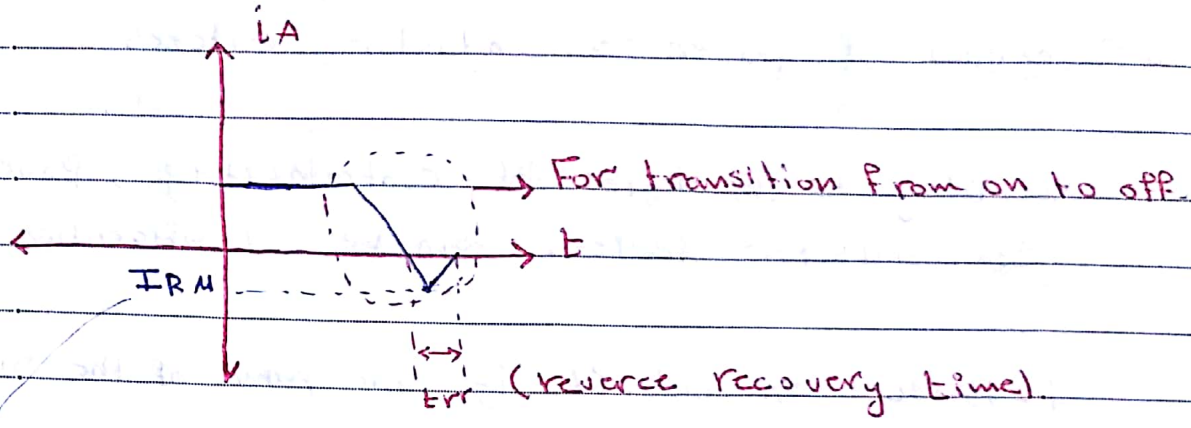
* Diodes :-



i-v char (partical)

$$R_D = \frac{V_{AK}}{i_A}$$

$$R_D = \frac{V_{AK}}{i_A} = \frac{0}{i_A} = 0$$

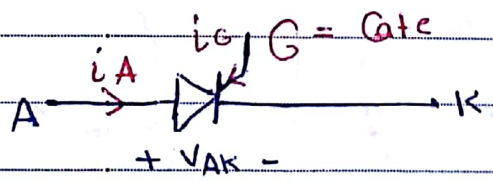


I_{RM} - Maximum reverse ~~current~~ value.

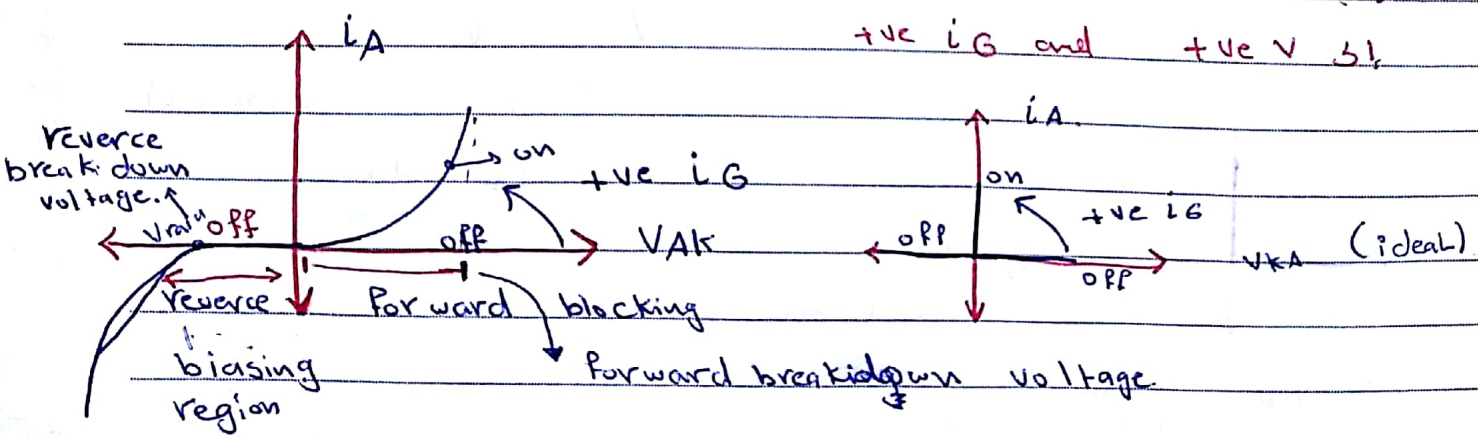
* ~~Schottky Diodes~~ Diodes * (Types Power Semiconductor Diodes) :-

- 1 - Schottky Diodes (50-100) V rated
 - 2 - Fast Recovery Diodes
 - 3 - Line Frequency
- check rated from the book.

* Thyristors :-



on and is Diode like ~~imp~~ *
 off \rightarrow on ~~with~~ *
 +ve i_G and +ve V_{AK}

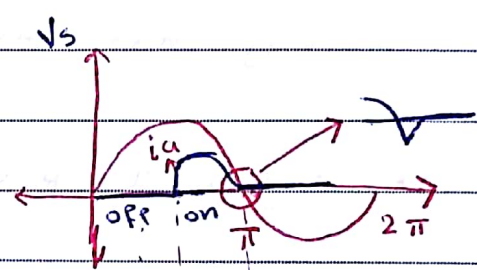
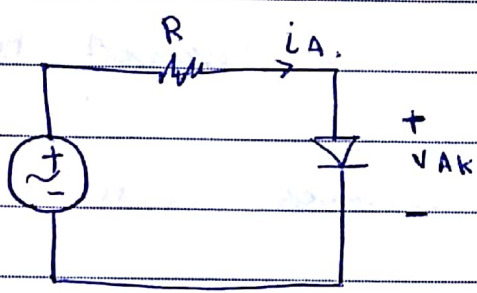


becomes off.

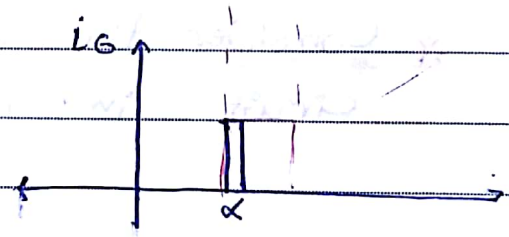
* The Thyristors (when the current tries to be negative.

* The Thyristors has the same chara of the Diode whiches reverse recovery time. (t_{rr}).

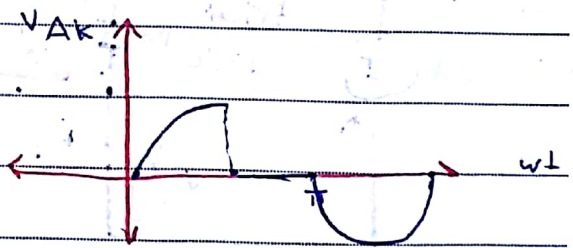
* The thyristor become on which α : +ve gate and +ve voltage are applied.



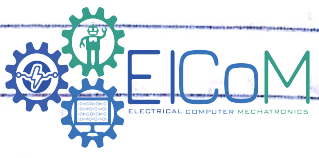
- $0 \rightarrow \alpha \Rightarrow \text{off}$
- $\alpha \rightarrow \pi \Rightarrow \text{on}$
- $\pi \rightarrow 2\pi \Rightarrow \text{off}$



$i_A = \frac{v_m \sin \omega t}{\omega L} \Rightarrow V_{AK} = \text{Zero.}$



Switched α \Rightarrow on
 on α \Rightarrow on
 off α \Rightarrow off
 Power low \Rightarrow on
 Power = 0 \Rightarrow off



* Desired characteristics of controllable switches (BJT) :-

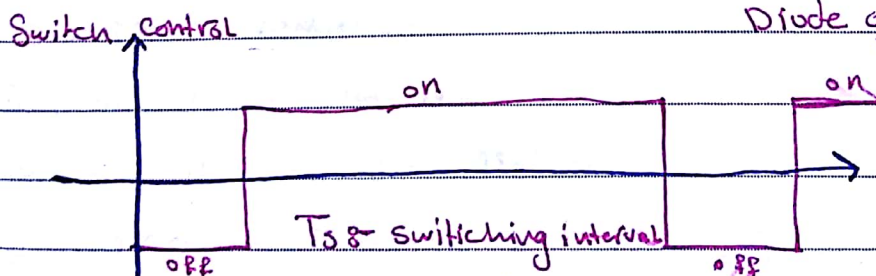
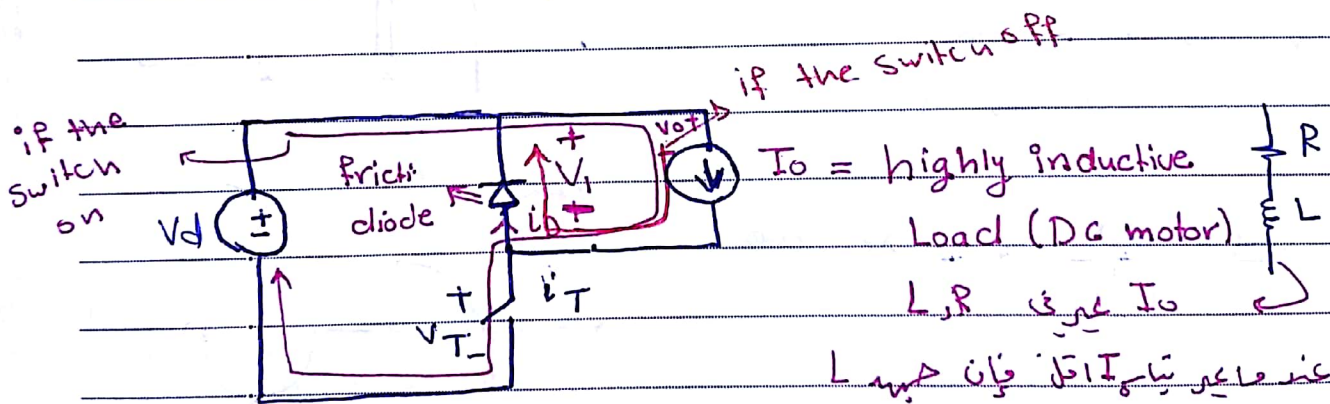
* Block large forward and reverse voltages with zero current when off.

* Conduct large current with zero voltage drop when on.

* Switching from on to off vice versa with very short interval, when triggered

* Very small power consumed by the control ckt

* Consider the following commonly encountered circuit in power electronics.



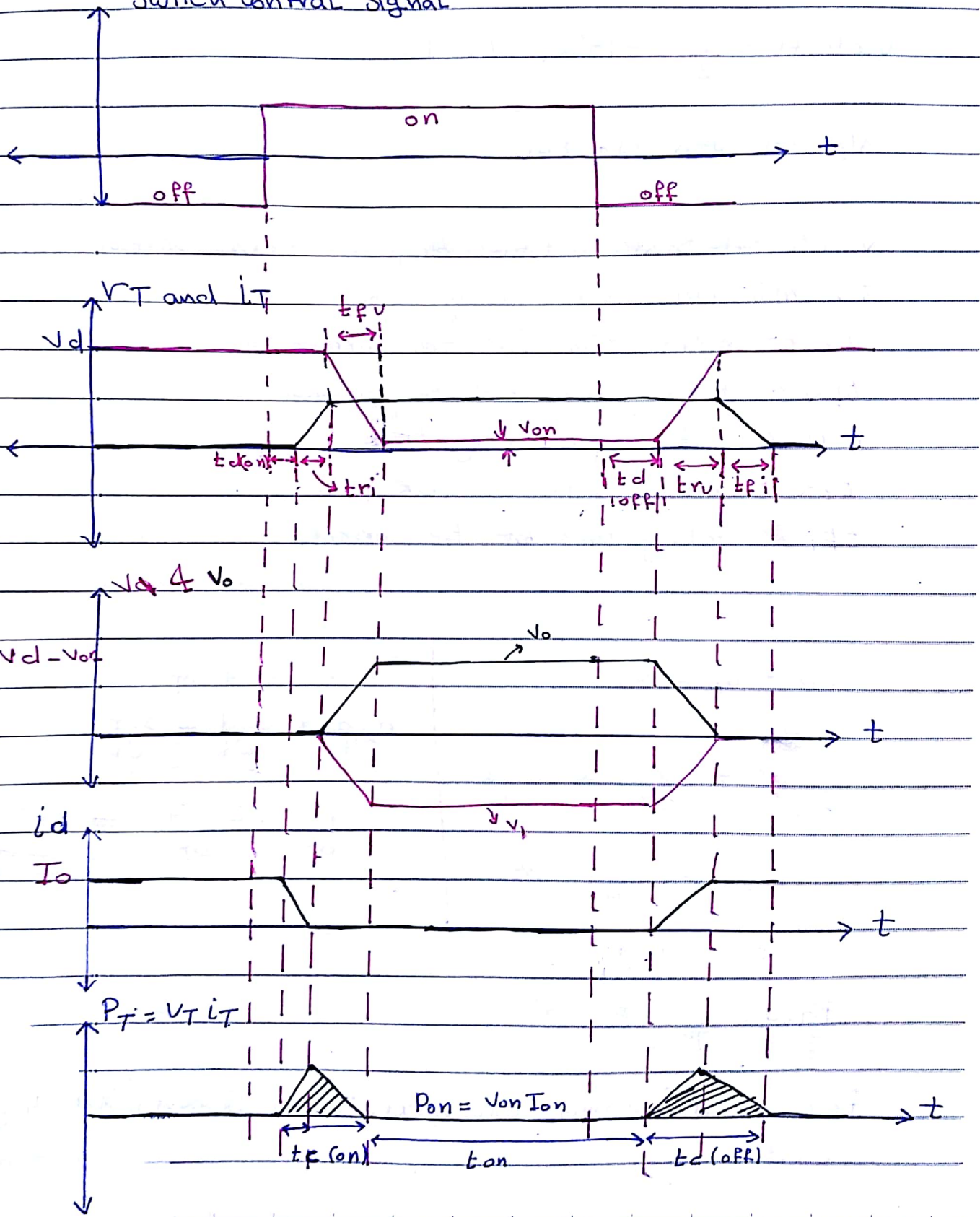
$$-V_d + V_o + V_T = 0$$

$$V_o + V_T = V_d \Rightarrow \frac{dV_o}{dt} + \frac{dV_T}{dt} = 0$$

$$\frac{dV_o}{dt} = -\frac{dV_T}{dt}$$

if the Switch on \Rightarrow Diode on (reverse).

Switch control signal



$$W_c(\text{on}) = \frac{1}{2} t_c(\text{on}) V_d I_o$$

$$W_c(\text{off}) = \frac{1}{2} t_c(\text{off}) V_d I_o$$

$$W_{\text{on}} = V_{\text{on}} I_o t_{\text{on}}$$

V_{on} :- on-state voltage drop across the switch

$t_d(\text{on})$:- on-state delay time

t_r :- rising time for the current

$t_f v$:- falling time for the voltage

$t_d(\text{off})$:- off-state delay time.

$t_{r v}$:- rising time for the voltage

$t_{f i}$:- falling time for the current

$$V_d = V_o + V_T$$

$$\frac{dV_d}{dt} = \frac{dV_o}{dt} + \frac{dV_T}{dt}$$

$$\frac{dV_o}{dt} = - \frac{dV_T}{dt} \neq$$

$$I_o = I_d + I_T$$

$$\frac{dI_o}{dt} = \frac{dI_d}{dt} + \frac{dI_T}{dt}$$

$$\frac{dI_d}{dt} = - \frac{dI_T}{dt} \neq$$

$$P_{\text{avg}} = \frac{1}{T} \int_0^T P(t) dt$$

P_s :- Power average consumed by the switch (switching power)

$$P_s = \frac{1}{2} v_d I_o \frac{1}{T_s} [t_c(\text{on}) + t_c(\text{off})]$$

$$= \frac{1}{2} v_d I_o f_s [t_c(\text{on}) + t_c(\text{off})]$$

$$P_{\text{on}} = \frac{v_{\text{on}} I_o t_{\text{on}}}{T_s} = v_{\text{on}} I_o t_{\text{on}} f_s, P_{\text{off}} = 0$$

$P_{\text{off}} = 0$, $i_T \Rightarrow 0$ during the off state.

$$P_{\text{total}} = P_s + P_{\text{on}} + \cancel{P_{\text{off}}}$$

$$P_{\text{total}} = P_s + P_{\text{on}}$$

* Desired characteristics of Controllable 8-

1. Small Leakage (Reversed) current in the off-state

~~2) Small time of change on to off:~~

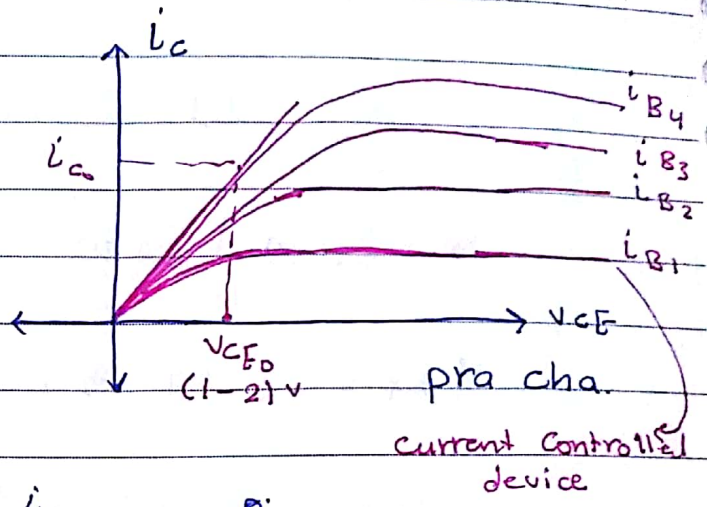
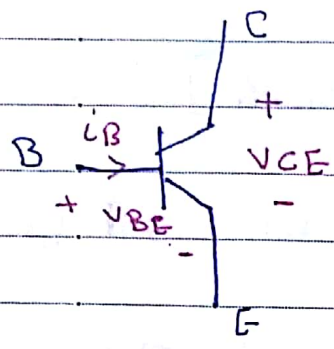
2. - Small on state voltage drop.

3) Small power consumed by the control CCT.

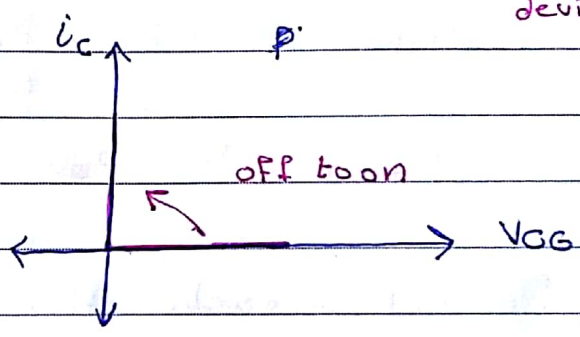
4) Short turn-on & off time intervals.

5) High on-state current rating.

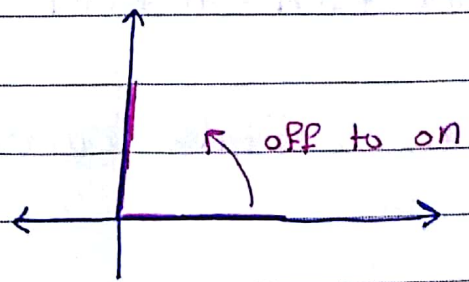
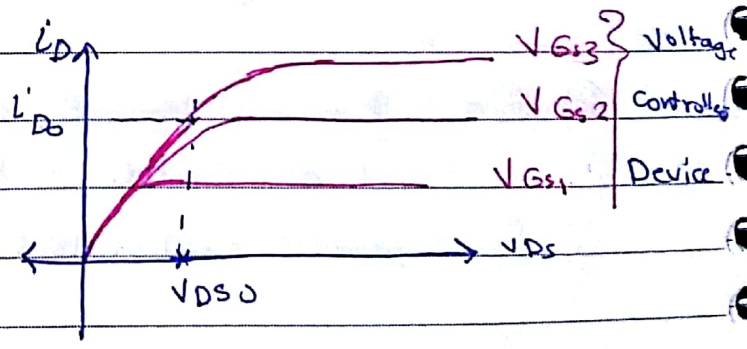
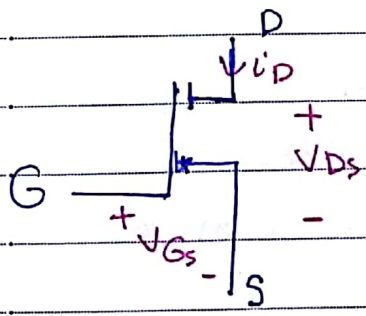
* BJT :-



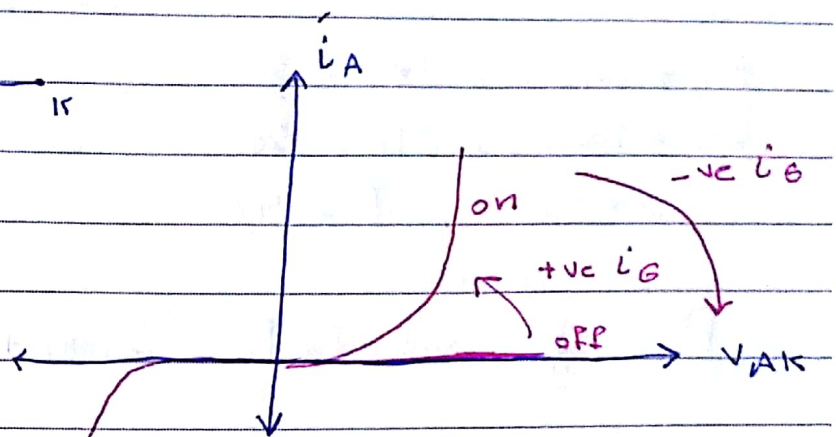
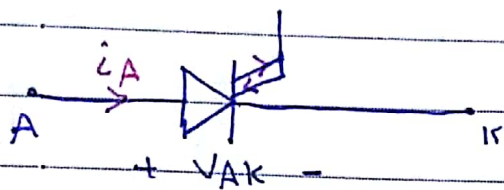
off $\sim 10^3$ }
 1400 V
 few hundred Amperes



* Mos Fet :-

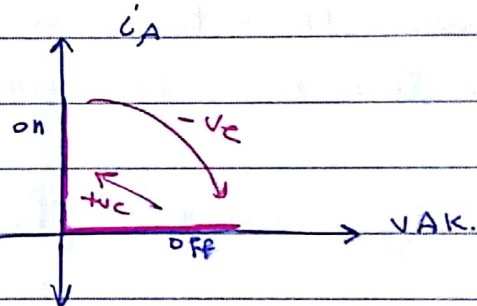


* GTO (Gate Turn off Thyristors) :-



Description :- Like the thyristor, GTO is turned on by +ve gate pulse.

unlike \rightarrow the thyristor, GTO is turned off by -ve gate pulse.



* Justifications of using idealized Cha of switches

* The switches will be treated in this course as ideal, because :-

1. on state voltage drop is very small compared with rated voltage. (0)

2. off state current is very small compared with rated current (Large resistance in off state).

3. Very small time required for switching.

*P(2-1) Page(32) 8-

$$t_{ri} = 100 \text{ ns}, \quad t_{fv} = 50 \text{ ns}$$

$$t_{rv} = 100 \text{ ns}, \quad t_{fi} = 200 \text{ ns}$$

$$V_d = 300, \quad I_o = 4 \text{ A.}$$

$$P_s = \frac{1}{2} V_d I_o f_s (t_{c(on)} + t_{c(off)})$$

$$t_{c(on)} = t_{ri} + t_{fv} = 100 + 50 = 150 \text{ ns.}$$

$$t_{c(off)} = t_{rv} + t_{fi} = 100 + 200 = 300 \text{ ns.}$$

$$P_s = \frac{1}{2} \times 300 \times 4 \times f_s [150 + 300] \times 10^{-9}$$

$$= 2.7 \times 10^{-4} f_s$$

$$\text{If } f_s = 25 \text{ KHz.} \quad \therefore P_s = 6.75 \text{ W}$$

$$\text{If } f_s = 100 \text{ KHz} \quad \therefore P_s = 27 \text{ W.}$$

$$P_{rated} = 300 \times 4 = 1200 \text{ W.}$$

* Idealized char of controllable switches

1 - Zero on-state voltage drop

2 - Zero reversed current in the off state

3 - Zero time duration for switching.

4 - Power required for the control CCT is zero

CH3: Review of basic Electrical circuit concepts

* Average power and rms current :-

$$P(t) = V(t) i(t).$$

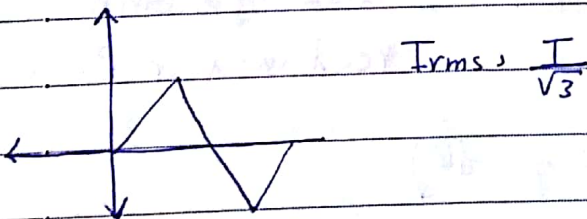
$$P_{avg} = \frac{1}{T} \int_0^T P(t) dt = \frac{1}{T} \int_0^T V(t) i(t) dt.$$

$$= \frac{1}{T} \int_0^T i^2(t) R dt =$$

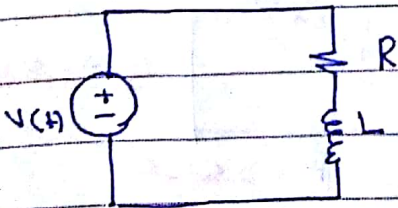
$$= \frac{R}{T} \int_0^T i^2(t) dt.$$

$$= R I^2 \quad \#$$

$$I = \sqrt{\frac{1}{T} \int_0^T i^2(t) dt} \rightarrow \text{rms value of } I.$$

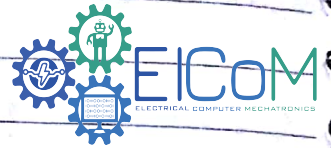
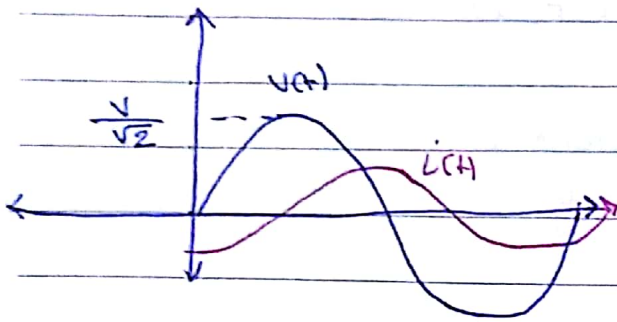


* Steady-state wave forms with sinusoidal voltages and currents.



$$V(t) = \sqrt{2} V \cos \omega t$$

$$i(t) = \sqrt{2} I \cos(\omega t - \theta).$$



$$\begin{aligned} \vec{V} &= V \angle 0 \\ \vec{I} &= I \angle -\phi \end{aligned}$$

$$\vec{V} = V e^{j0} \Rightarrow \text{exponential form}$$

$$\vec{I} = I e^{-j\phi} \Rightarrow \text{exponential form.}$$

$$\vec{Z} = \frac{\vec{V}}{\vec{I}} = \frac{V e^{j0}}{I e^{-j\phi}} = \frac{V}{I} \angle \phi$$

$$= \frac{V}{I} (\cos \phi + j \sin \phi) = Z \cos \phi + j Z \sin \phi$$

Rectangular form.

$$\vec{S} = \vec{V} \vec{I} = V e^{j0} (I e^{-j\phi})$$

↳ complex power.

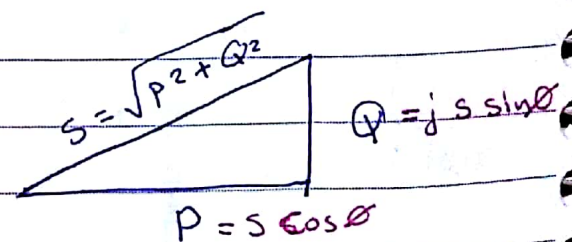
$$= V I e^{j\phi} = \underbrace{S \cos \phi}_{\text{active}} + j \underbrace{S \sin \phi}_{\text{reactive.}}$$

$S \Rightarrow$ apparent power

PF = 1 \Rightarrow pure R.

PF \Rightarrow Lagging \Rightarrow R and L or L

PF \Rightarrow Leading \Rightarrow R and C or C



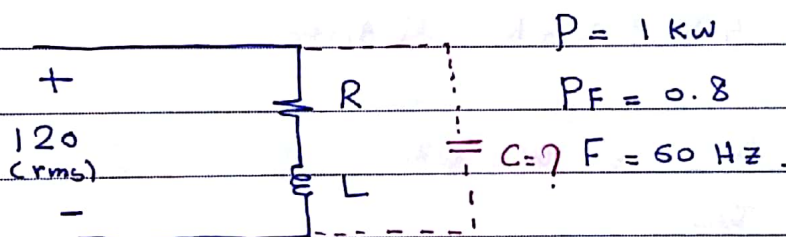
$$PF = \cos \phi = \frac{P}{S}$$

$$= \cos \left[\tan^{-1} \frac{Q}{P} \right] = \cos \left[\sin^{-1} \frac{Q}{S} \right]$$

$$PF \Rightarrow \text{Lagging} = R + j\omega L \text{ or } j\omega L$$

$$PF \Rightarrow \text{Leading} = R + \frac{1}{j\omega C} \text{ or } \frac{1}{j\omega C}$$

Ex 8-



PF combined = 0.95 Lagging.

~~PF~~ Before connecting C

$$PF = \frac{P}{S} \Rightarrow 0.8 = \frac{1000}{S}$$

$$S = 1250 \text{ VA}$$

$$Q = \sqrt{S^2 - P^2} = 750$$

$$\tilde{S} = 1000 + j750 \text{ VA}$$

After connecting C

$$P = 1000 \text{ W}$$

$$\text{P.F.} = \frac{P}{S} \Rightarrow 0.95 = \frac{1000}{S}$$

$$S = \sqrt{1000^2 + (750 - Q_c)^2}$$

$$0.95 = \frac{1000}{\sqrt{1000^2 + (750 - Q_c)^2}}$$

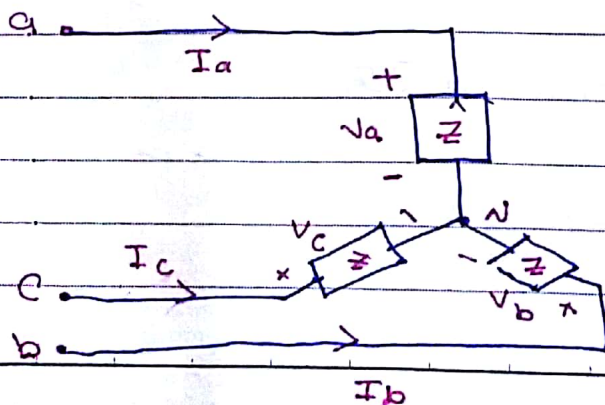
$$Q_c = 421.3 \text{ VAR } Q_{\text{After.}}$$

$$Q_c = \frac{V^2}{\frac{1}{\omega C}} = \omega C V^2$$

$$421.3 = (120)^2 (2\pi 60) C$$

$$C = 77.6 \text{ } \mu\text{F}$$

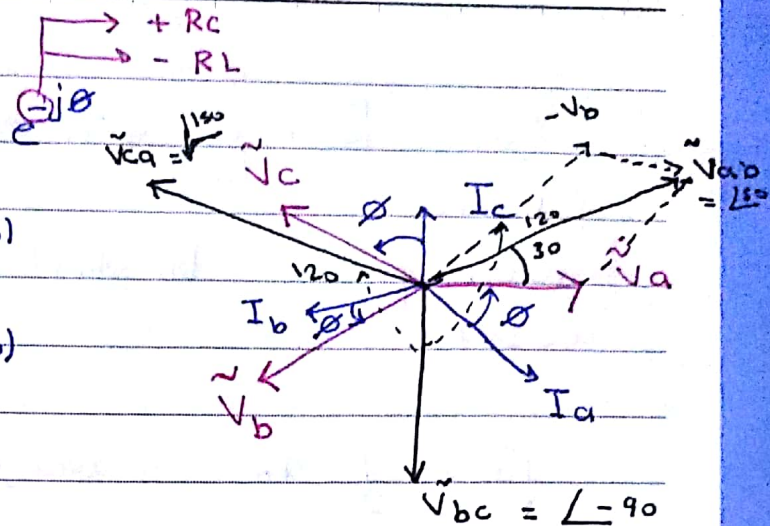
* Three-phase Circuits.



$$\tilde{I}_a = \frac{\tilde{V}_a}{Z} = \frac{V_a}{Z} e^{j\theta}$$

$$\tilde{I}_b = \frac{V_a}{Z} e^{-j(\theta - 120^\circ)}$$

$$\tilde{I}_c = \frac{V_a}{Z} e^{-j(\theta + 120^\circ)}$$



$$\begin{aligned} \tilde{V}_L = \tilde{V}_{L} &= \tilde{V}_a - \tilde{V}_b = V_a \angle 0^\circ - V_a \angle -120^\circ \\ &= \sqrt{3} V_a \angle 30^\circ \end{aligned}$$

$$\begin{aligned} * P &= \sqrt{3} V_L I_L \cos \theta \\ &= 3 V_\phi I_\phi \cos \theta \end{aligned}$$

$$\begin{aligned} * Q &= \sqrt{3} V_L I_L \sin \theta \\ &= 3 V_\phi I_\phi \sin \theta \end{aligned}$$

$$* S = \sqrt{3} V_L I_L = 3 V_\phi I_\phi$$

→ for both Δ or Y .

+ seq (abc)

- seq (acb)

* Non Sinusoidal waveforms in Steady-state :-

* The steady-state voltage and current in power Electronic are normally periodic but non sinusoidal.

* Fourier's Analysis of Repetitive waveforms :-

$$f(t) = F_0 + \sum_{h=1}^{\infty} F_h(t) = F_0 + \sum_{h=1}^{\infty} \left\{ a_n \cos(h\omega t) + b_n \sin(h\omega t) \right\}$$

Periodic Function $\omega = 2\pi f$

$$F_0 = \frac{1}{2} a_0 \Rightarrow \text{average value}$$

$$a_h = \frac{1}{\pi} \int_0^{2\pi} f(t) \cos(h\omega t) \frac{d\omega t}{\omega}, \quad h = 0, 1, 2, 3, \dots$$

$$b_h = \frac{1}{\pi} \int_0^{2\pi} f(t) \sin(h\omega t) \frac{d\omega t}{\omega}, \quad h = 1, 2, 3, \dots$$

if $h=0$

$$a_0 = \frac{1}{\pi} \int_0^{2\pi} f(t) \cos(0) d\omega t$$

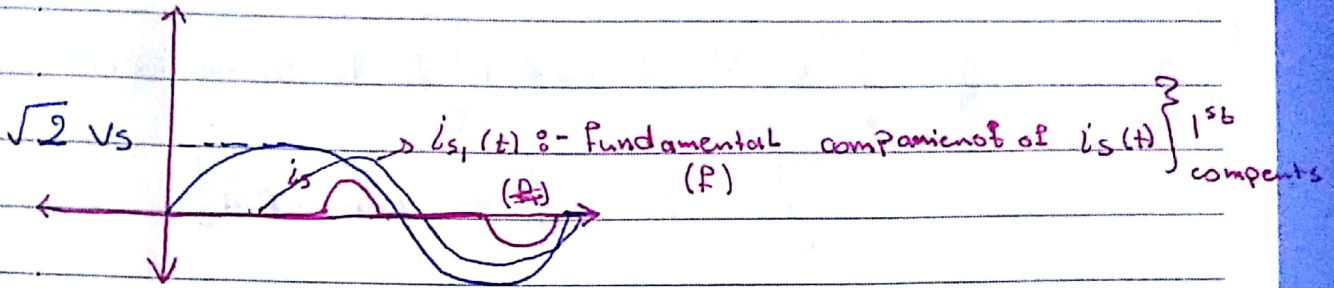
$$= \frac{1}{\pi} \int_0^{2\pi} f(t) d\omega t = 2F_0$$

* The rms value of $f(t)$ is.

$$F = \sqrt{F_0^2 + F_1^2 + \dots + F_n^2}$$

$$= \sqrt{\frac{1}{2\pi} \int_0^{2\pi} (f(t))^2 d\omega t}$$

* Line current Disturtion :-



$$i_s(t) = i_{s1}(t) + \sum_{h \neq 1}^{\infty} i_{sh}(t)$$

$i_{s1}(t)$ Fundamental component of $i_s(t)$.

i_{sh} :- the components at the h harmonic

$$f_h = hf_1$$

$$i_s(t) = \sqrt{2} I_{s1} \sin(\omega t - \phi_1) + \sum_{h \neq 1}^{\infty} \sqrt{2} I_{sh} \sin(\omega_h t - \phi_h)$$

\downarrow rms value of fundamental \downarrow the phase shift between v_s & i_{s1} \rightarrow rms of the h component

* $THD\% = \sqrt{\frac{I_s^2 - I_{s1}^2}{I_{s1}^2}} * 100\% \Rightarrow$ Total harmonic Disturtion

$THD = 0$ Signal sin ωt ل \sin مع مقدار بعد \times

$$P_i = \frac{1}{T} \int_0^T P(t) dt$$

$$= \frac{1}{T} \int_0^T v_s(t) i_s(t) dt$$

$$P_1 = \frac{1}{T_1} \int_0^{T_1} v_s(t) i_s(t) dt.$$

$$P_1 = \frac{1}{T_1} \int_0^{T_1} \sqrt{2} V_s \sin(\omega_1 t) * \left[\sqrt{2} I_{s1} \sin(\omega_1 t - \phi_1) + \sum_{n \neq 1}^{\infty} \sqrt{2} I_{sn} \sin(\omega_n t - \phi_n) \right]$$

$$= V_s I_{s1} \cos(\phi_1)$$

$$\int_0^{2\pi} \sin \theta \sin 2\theta d\theta = 0 \quad \text{--- } \int \sin \theta \cos \theta d\theta$$

* Conclusion
 The ~~interaction~~ of the current components at harmonic frequencies of average value of the power with pure sinusoidal voltage is zero.

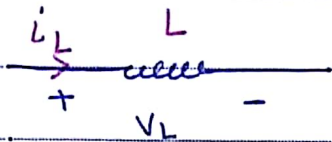
$$* S = V_s I_s$$

$$PF = \frac{P}{S} = \frac{V_s I_{s1} \cos(\phi_1)}{V_s I_s}$$

$$= \frac{I_{s1}}{I_s} \cos(\phi_1) \quad \left[\begin{array}{l} V_s \Rightarrow \sin t \text{ is by law} \\ I \Rightarrow \text{not } \sin t \end{array} \right]$$

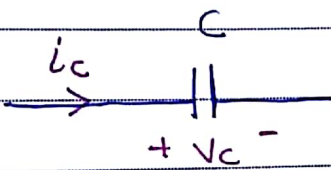
↓
 D.P.F. : Displacement power factor.

* Inductor and capacitor Responses.



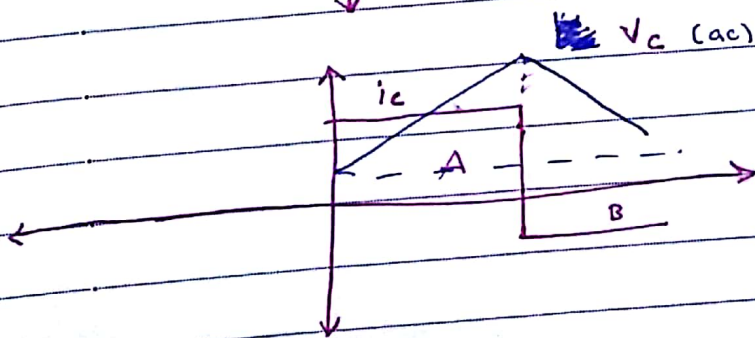
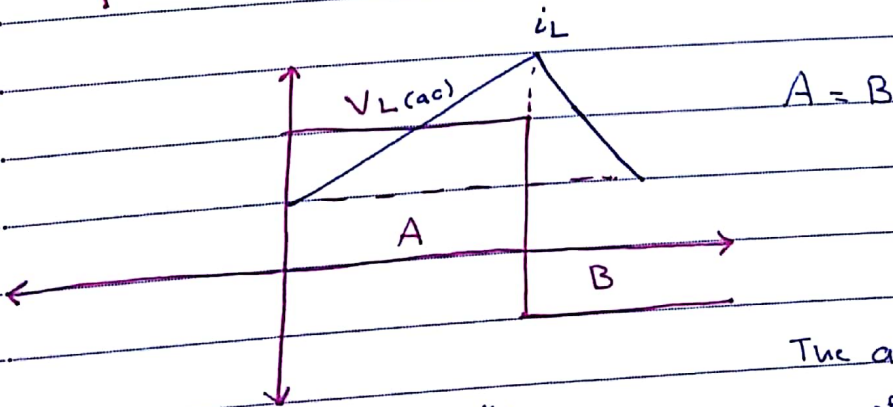
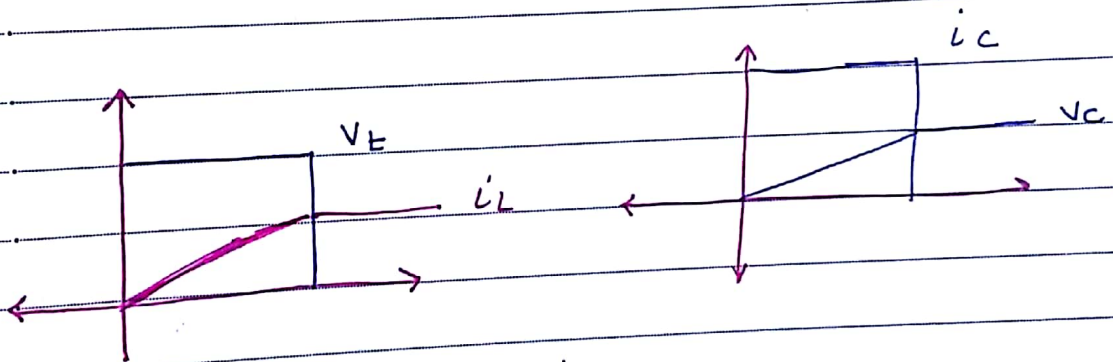
$$V_L = L \frac{di_L(t)}{dt}$$

$$i_L(t) = \frac{1}{L} \int V_L(t) dt + k$$



$$i_C = C \frac{dV_C(t)}{dt}$$

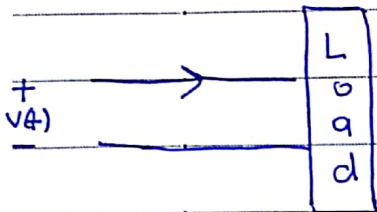
$$V_C = \frac{1}{C} \int i_C dt + k$$



The average value of voltage across inductor in steady state = zero.

The average value of current through the capacitor at steady state = zero.

3-6 pp (58) :-

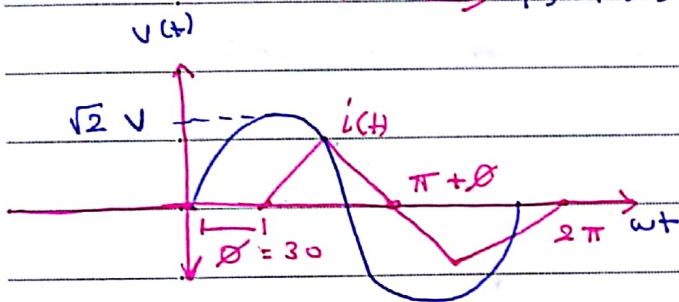


* $v(t) = \sqrt{2} V \sin(\omega t)$, $V = 120$

* $i(t)$ is a triangular wave with an amplitude $A = 10 A$

* $i(t)$ lags $v(t)$ by 30° ($\phi = 30^\circ$)

Find \Rightarrow P, DPF, THD, PF = ??



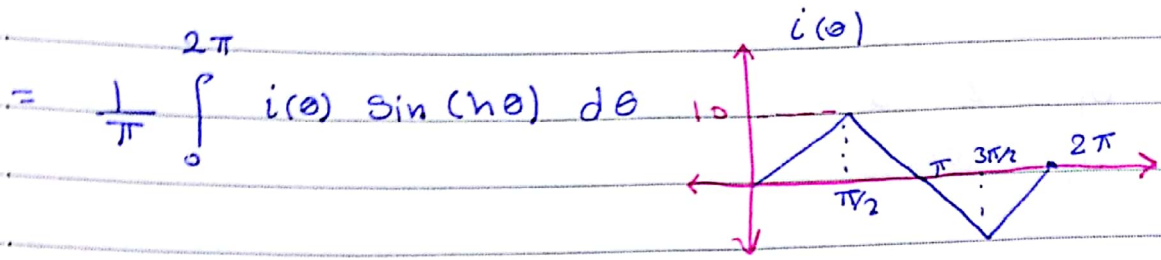
$$P = V I_1 \cos \phi$$

$$I_1 = \frac{I_1(t)}{\sqrt{2}}, \quad * i(t) \text{ is symmetric on the } x\text{-axis}$$

$a_n = 0$, $b_n = 0$ for even numbers of n
 b_1, b_3, b_5, \dots

$$I_1 = \frac{b_1}{\sqrt{2}}$$

$$b_n = \frac{1}{\pi} \int_0^{2\pi} i(t) \sin(n\omega t) d\omega t$$



$$i(\theta) = \begin{cases} \frac{20}{\pi} \theta, & 0 < \theta < \frac{\pi}{2} \\ -\frac{20}{\pi} \theta + 20, & \frac{\pi}{2} < \theta < \frac{3\pi}{2} \\ \frac{20\theta}{\pi} - 40, & \frac{3\pi}{2} < \theta < 2\pi \end{cases}$$

$$-\frac{20}{\pi} \theta + 20, \quad \frac{\pi}{2} < \theta < \frac{3\pi}{2}$$

$$\frac{20\theta}{\pi} - 40, \quad \frac{3\pi}{2} < \theta < 2\pi$$

$$\rightarrow \left(\frac{\pi}{2}, 10\right), (\pi, 0)$$

$$y - 0 = \frac{10 - 0}{\frac{\pi}{2} - \pi} \cdot \left(\theta - \pi\right) = \frac{10}{-\frac{\pi}{2}} \cdot (\theta - \pi)$$

$$y - 0 = -\frac{20}{\pi} (\theta - \pi)$$

$$y = -\frac{20}{\pi} \theta + 20$$

~~$$b_n = \frac{1}{\pi} \left[\int_0^{\frac{\pi}{2}} \frac{20\theta}{\pi} d\theta + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (20 - \frac{20\theta}{\pi}) d\theta + \int_{\frac{3\pi}{2}}^{2\pi} (\frac{20\theta}{\pi} - 40) d\theta \right]$$~~

$$b_n = \frac{1}{\pi} \left[\int_0^{\frac{\pi}{2}} \frac{20\theta}{\pi} \sin(n\theta) d\theta + \int_{\frac{\pi}{2}}^{\frac{3\pi}{2}} (20 - \frac{20\theta}{\pi}) \sin(n\theta) d\theta + \int_{\frac{3\pi}{2}}^{2\pi} (\frac{20\theta}{\pi} - 40) \sin(n\theta) d\theta \right]$$

$$b_1 = 8.106$$

$$b_3 = -0.9006$$

$$1 - P = V I_1 \cos \theta = 120 \times \frac{8.106}{\sqrt{2}} \cos 30$$

$$= 596 \text{ W}$$

$$2 - \text{D}_{\text{PF}} = \cos \theta = \cos 30 = 0.866$$

$$3 - \text{THD} = \frac{\sqrt{I^2 - I_1^2}}{I_1} \times 100$$

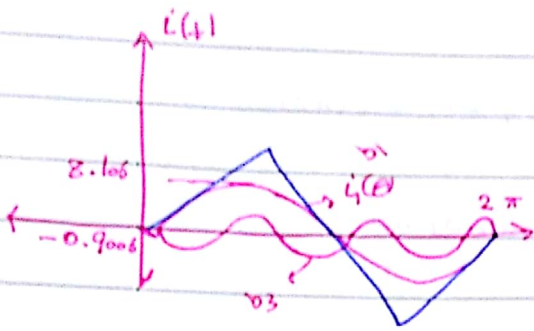
$$I = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} [i(\theta)]^2 d\theta}$$

$$I = \sqrt{\frac{1}{2\pi} \left[\int_0^{\pi/2} \left(\frac{20\theta}{\pi}\right)^2 d\theta + \int_{\pi/2}^{\frac{3\pi}{2}} \left[20 - \frac{20\theta}{\pi}\right]^2 d\theta + \int_{\frac{3\pi}{2}}^{2\pi} \left(\frac{20\theta}{\pi} - 40\right)^2 d\theta \right]}$$

$$I = 5.7736$$

$$\text{THD} = \frac{\sqrt{(5.7736)^2 - \left(\frac{8.106}{\sqrt{2}}\right)^2}}{\frac{8.106}{\sqrt{2}}} \times 100\% = 12.1\%$$

$$\text{PF} = \frac{I_1}{I} \cos \theta = \frac{8.106}{\sqrt{2} \times 5.7736} \cos(30) =$$



* How to Integration Symbolically MATLAB :-

⇒ Syms a x

⇒ A = int(a * sin(x), x)

⇒ A =

$$-a * \cos(x)$$

⇒ B = int(a * sin(x), a)

⇒ B =

$$(1/2) * a^2 * \sin(x)$$

⇒ C = int(a * sin(x), x, 0, pi) $\rightarrow \int_0^{\pi} a \sin x dx$
 . عدد تكامل

⇒ C =

$$2*a$$

⇒ F = a^2 * exp(x).

⇒ D = int(F, x, 1, 2)

⇒ D =

$$a^2 \exp(2) - a^2 \exp(1).$$

Variable
Precision
automatic.

⇒ vpa(D, 5)

$$= 4.6708 * a^2.$$

د جواب D مقبول 5 digit.

$$b_h = \frac{1}{\pi} \left[\int_0^{\pi/2} \frac{20\theta}{\pi} \sin(h\theta) d\theta + \int_{\pi/2}^{3\pi/2} \left(\frac{-20\theta}{\pi} + 20 \right) \sin(h\theta) d\theta \right. \\ \left. + \int_{3\pi/2}^{2\pi} \left(\frac{20\theta}{\pi} - 40 \right) \sin(h\theta) d\theta \right]$$

>> Sym 5 h th

$$\gg F_1 = \text{Int} \left[\left(\frac{20 * th}{\pi} \right) * \sin(h * th), th, 0, (\pi/2) \right]$$

$$\gg F_1 =$$

$$\gg F_2 = \text{Int} \left[\left(\frac{-20 * th}{\pi} \right) * \sin(h * th), th, (\pi/2), (3\pi/2) \right]$$

$$\gg F_2 =$$

$$\gg F_3 =$$

$$\gg F_3 =$$

$$\gg b_h = (1/\pi) [F_1 + F_2 + F_3]$$

=

$$\gg b_1 = \text{Subs}(b_h, h, 1)$$

$$b_1 = 8.106$$

$$\gg b_2 = \text{Subs}(b_h, h, 2)$$

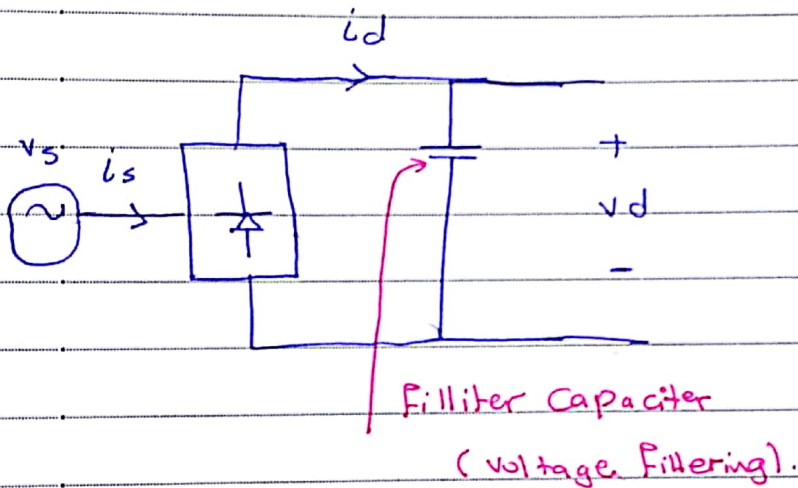
$$b_2 = 1.6 * 10^{-19}$$

$\gg b_3 = \text{subs} (b_n, h, 3)$

$b_3 = 0.9006$

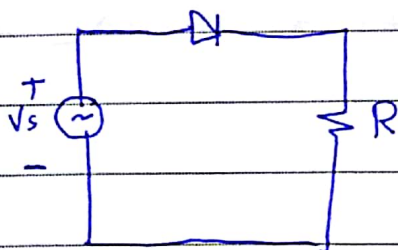
* Line Frequency Diode ^{uncontrolled} Rectifiers.

Line Frequency = 50 or 60 Hz.



* Basic Rectifier concept

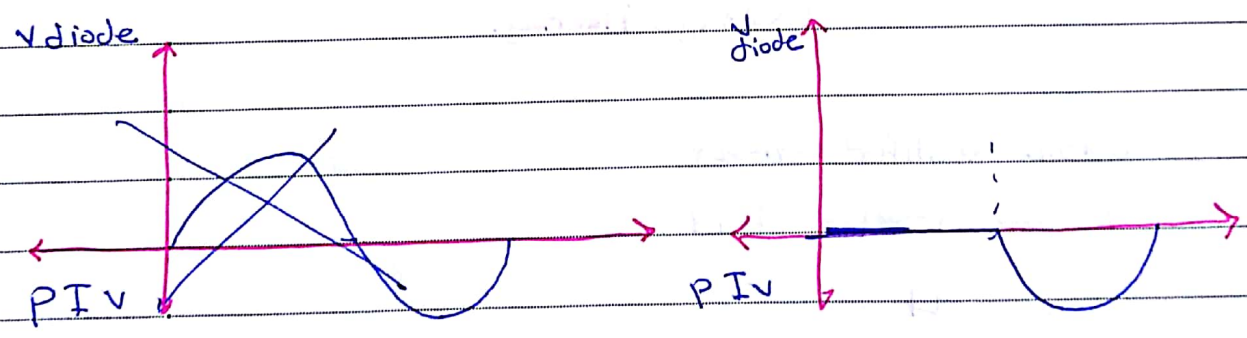
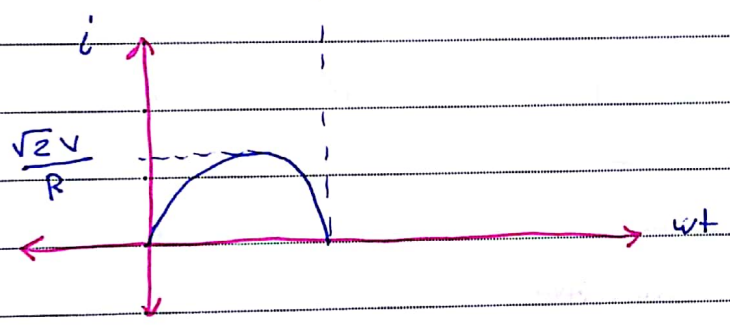
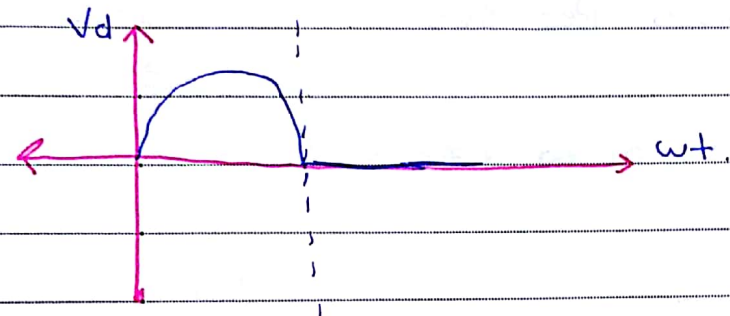
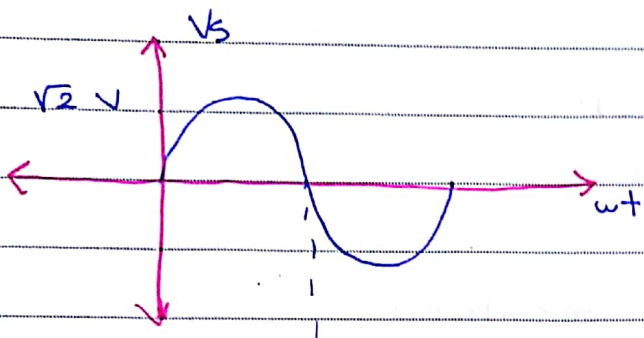
— pure resistive load



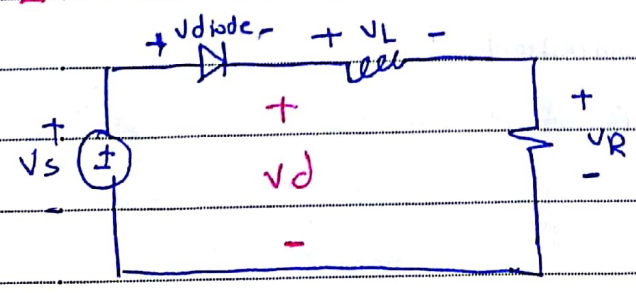
Half - ~~wave~~ wave uncontrolled

rectifier ~~with~~ pure resistive load.

with



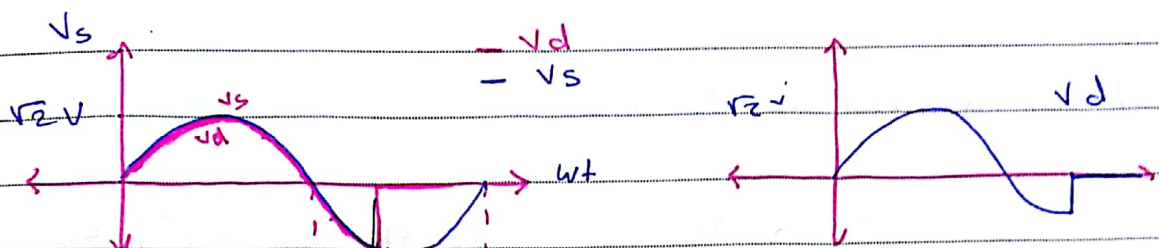
2 - Inductive Load



$$-V_s(t) + L \frac{di}{dt} + Ri = 0$$

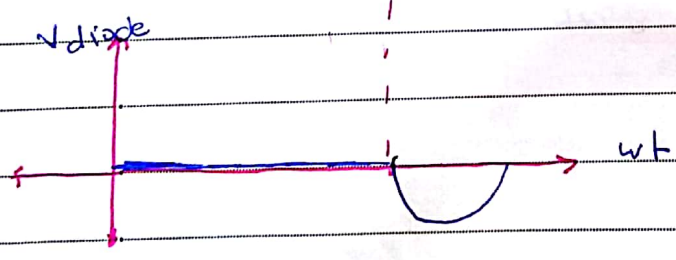
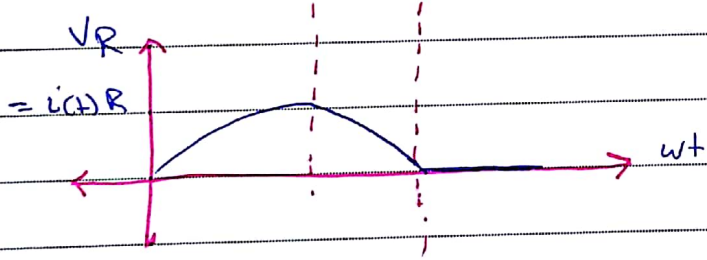
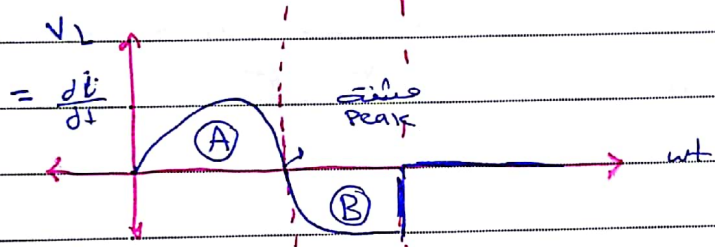
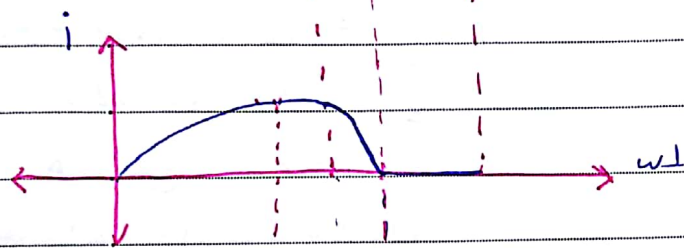
$$L \frac{di}{dt} = \sqrt{2} V \sin \omega t - Ri(t)$$

$i(t)$ is not pure sinusoidal.



Billiter S jzu Inductance

current j
current j
current j



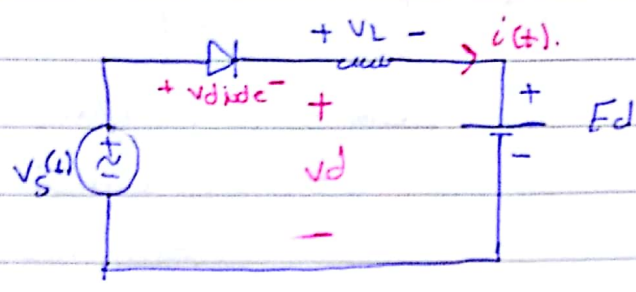
Diode on

$$v_d = v_s$$

Diode off

$$v_d = 0$$

② Load with an internal dc voltage.

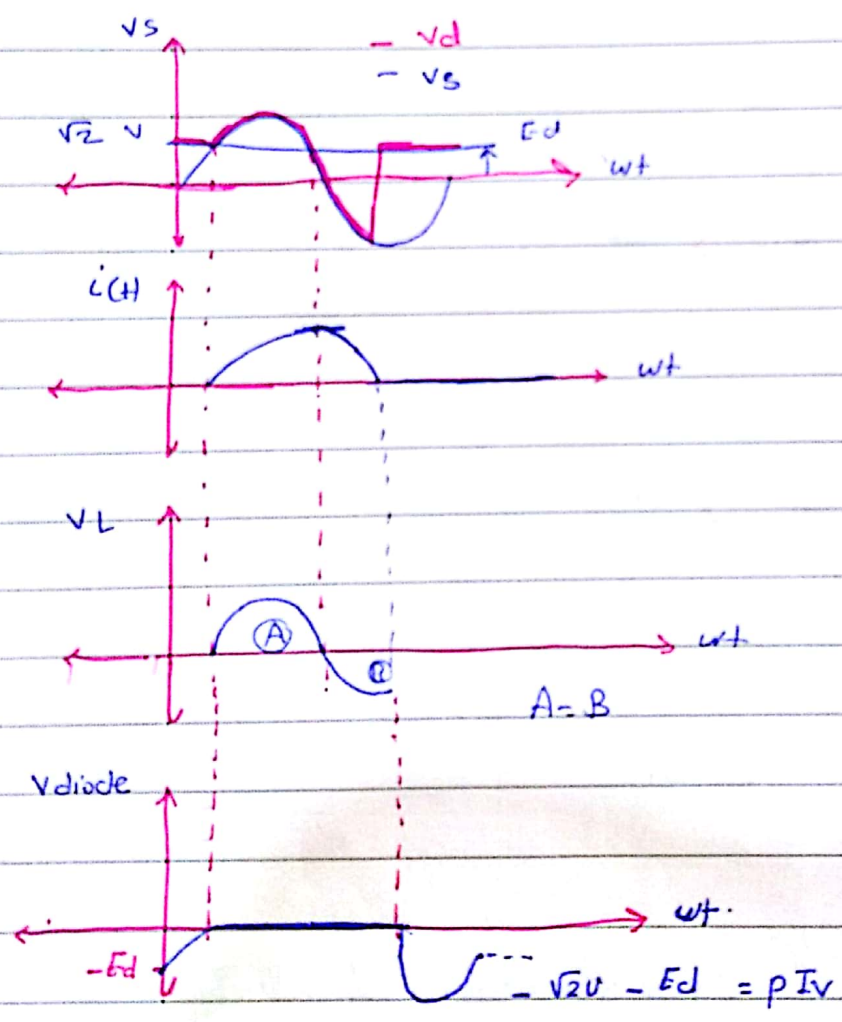


$$-v_s(t) + L \frac{di}{dt} + E_d = 0$$

$$L \frac{di}{dt} = \sqrt{2} v \sin \omega t - E_d$$

$$i = \text{peak}$$

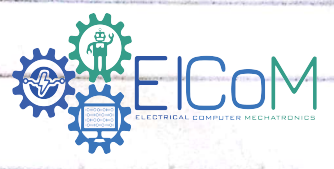
مقدار پیک جریان در لحظه
 عبور از بار است که در آن
 $v_s = E_d$



Diode on $v_d = 0$ (ideal), $v_d = v_s$

off $\Rightarrow -v_s(t) + v_{diode} + v_L + E_d = 0$

$$v_d = v_s - E_d$$

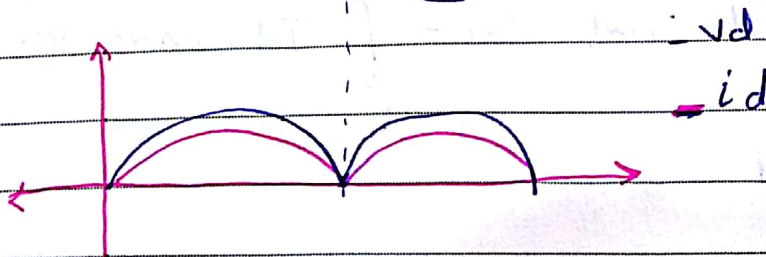
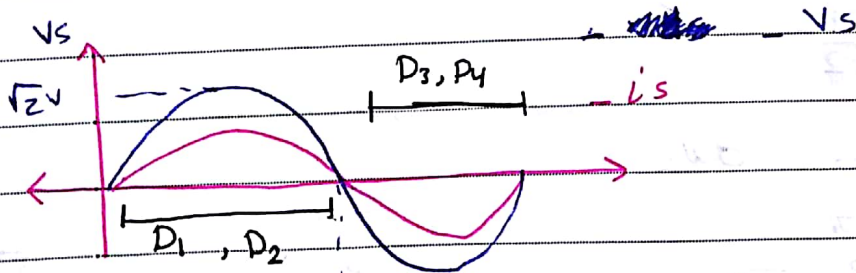
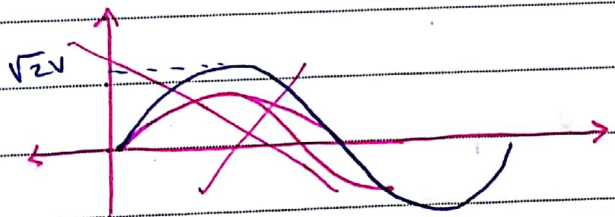
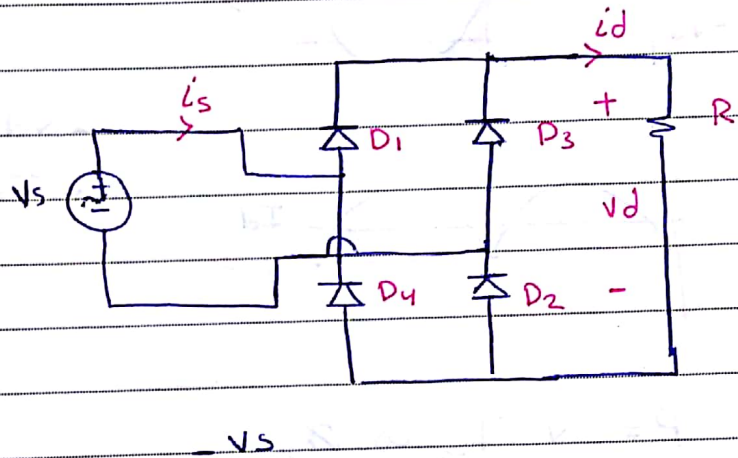


Diode off = $v_d = E_d$

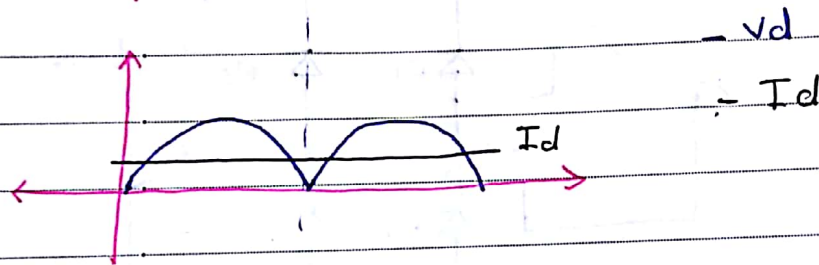
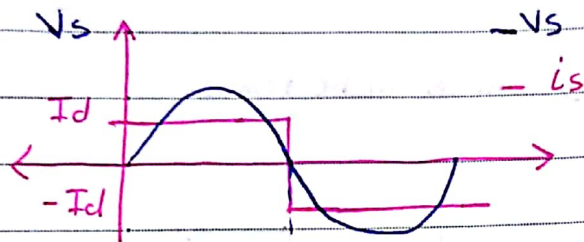
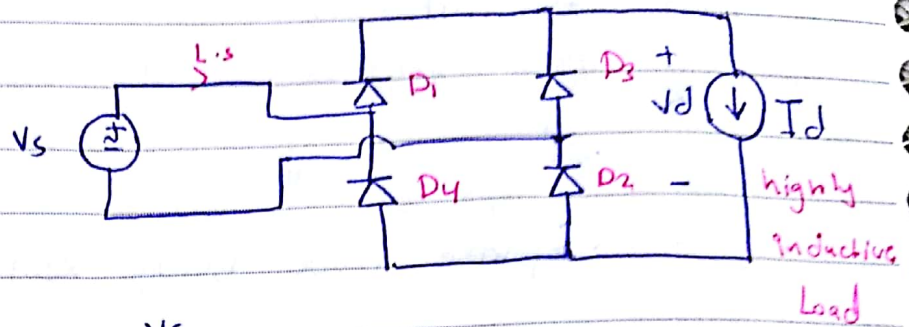
Diode on = $v_d = v_s$

* Single phase Diode Bridge Rectifiers.

1. Idealized case ($L_s = 0$). \Rightarrow Source inductance.



$$V_s = \sqrt{2} V \sin \omega t$$



$$P = V I_{s1} \cos \theta_1$$

$$= V I_{s1} \cos(0) = V I_{s1}$$

$$= V \frac{b_1}{\sqrt{2}}$$

$$b_n = \frac{1}{\pi} \int_0^{\pi} \dots d\omega$$

$$b_n = \frac{1}{\pi} \left[\int_0^{\pi} I_d \sin \omega t \, d\omega t - \int_0^{2\pi} I_d \sin \omega t \, d\omega t \right]$$

$$b_1 = \sqrt{2} \cdot 0.9 I_d$$

$$P_{ac} = V \times \frac{\sqrt{2} \cdot 0.9 I_d}{\sqrt{2}} = 0.9 V I_d$$

$$P_{dc} = \frac{1}{2\pi} \int_0^{2\pi} v_d(\theta) i_d(\theta) d\theta \Rightarrow \text{قانون الحساب البسيط}$$

. dc , ac

$$= 2 \times \frac{1}{2\pi} \left[\int_0^{\pi} \sqrt{2} \times v \times \sin\theta I_{dd} d\theta \right]$$

$$= \frac{1}{\pi} I_d \sqrt{2} \times v \cos\theta \Big|_0^{\pi}$$

$$= \frac{I_d}{\pi} \times \sqrt{2} \times v \times 2$$

$$= \frac{2\sqrt{2}}{\pi} v I_d = 0.9 v I_d$$

$$P_{ac} = P_{dc}$$

$$THD\% = \sqrt{\frac{I_s - I_{s1}}{I_{s1}}} \times 100\%$$

$$I_s = \sqrt{\frac{1}{2\pi} \int_0^{2\pi} I(\theta)^2 d\theta}$$

$$= \sqrt{\frac{1}{2\pi} \left[\int_0^{\pi} I_d^2 d\theta + \int_{\pi}^{2\pi} (-I_d)^2 d\theta \right]}$$

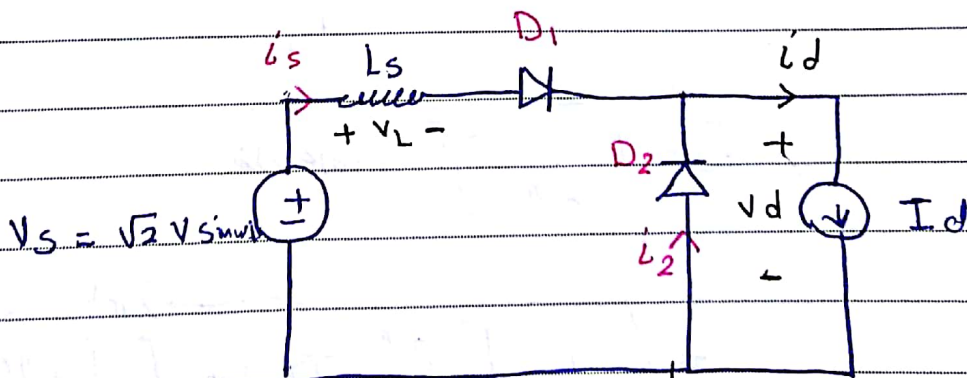
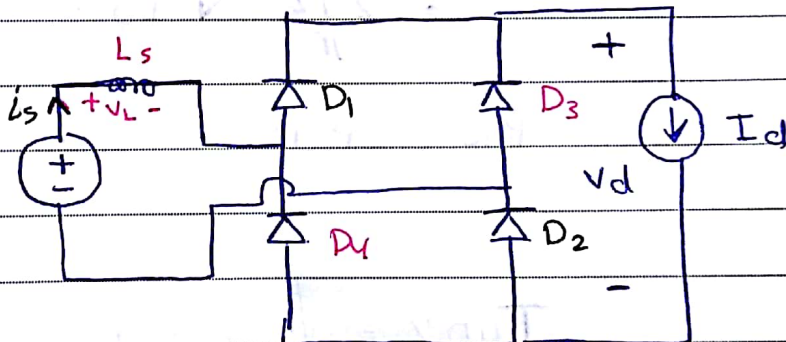
$$I_s = I_d$$

$$THD\% = \sqrt{\frac{(I_d)^2 - (0.9 I_d)^2}{(0.9 I_d)^2}} \times 100\% = 48.43\%$$

$$DPF = 1, \quad \cos(\phi) = 1 \Rightarrow \phi = 0$$

$$PF = \frac{I_{s1}}{I_s} DPF = \frac{0.9 I_d}{I_d} (1) = 0.9 \neq$$

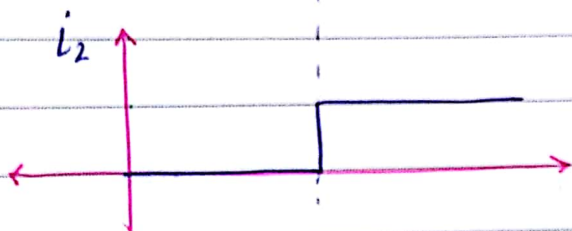
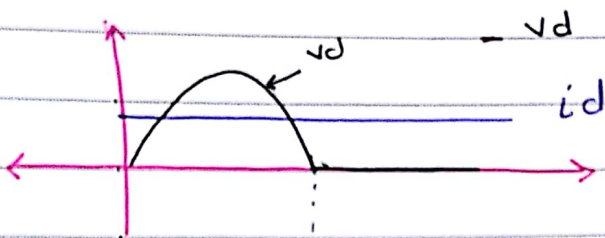
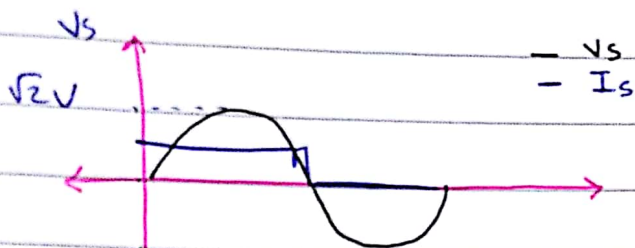
2. Effect of Source Inductance on Current Commutation.



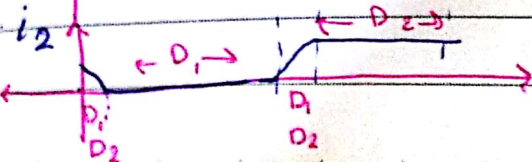
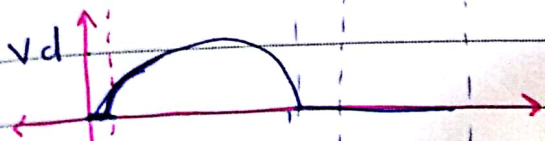
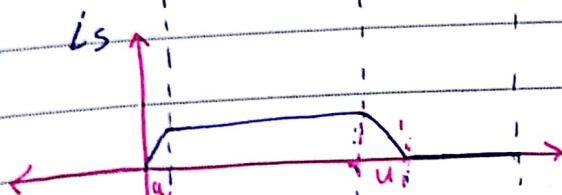
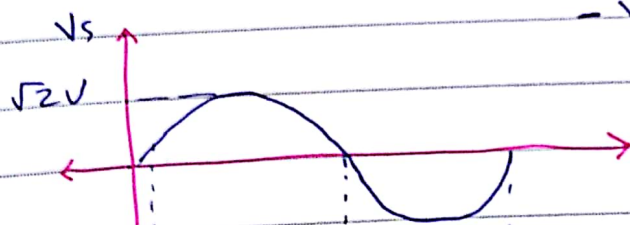
* If $L_s = 0$

Free wheeling Diode.

* $I_p L_s = 0$ ($\omega < \omega_{sw}$)



* with $L_s \neq 0$



یا i_s و i_d و i_2

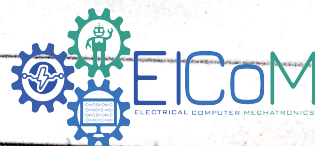
$v_d = 0 \leftarrow D_2 = 1$ on i_s

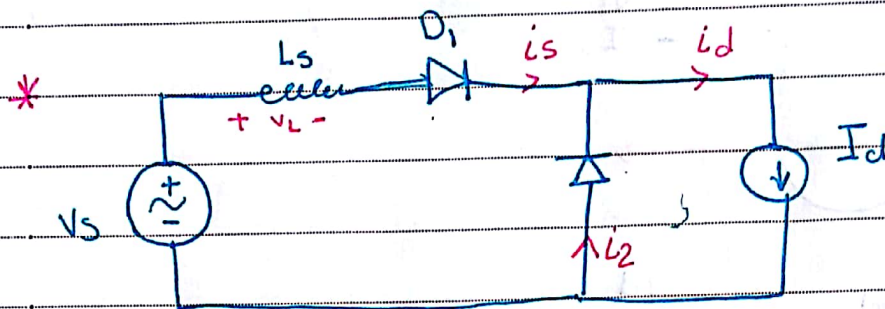
$$-i_s + i_d + i_2 = 0$$

$$-\frac{di_s}{dt} + \frac{di_d}{dt} - \frac{di_2}{dt} = 0$$

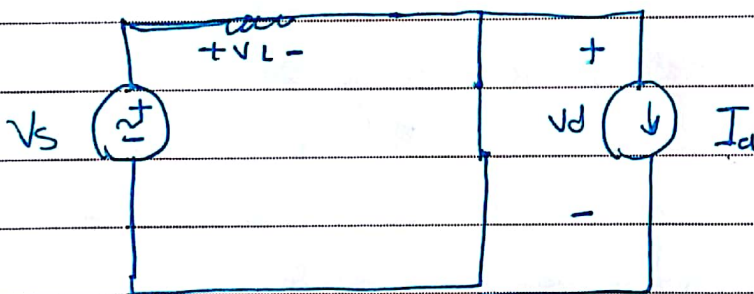
$$\frac{di_s}{dt} = -\frac{di_2}{dt}$$

$$v_d = v_{d2}$$





$$V_L = L \frac{di_s}{dt}$$



$0 < \omega t < \pi$ (two Diode on).

* During Commutation :-

$$V_L = V_s$$

$$L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t$$

$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t$$

$$\omega L_s \int_0^{\pi} di_s = \int_0^{\pi} \sqrt{2} V \sin \omega t \, d\omega t$$

$$\omega L_s I_d = \sqrt{2} V \cos \omega t \Big|_0^{\pi}$$

$$\omega L_s I_d = \sqrt{2} V [1 - \cos u]$$

$$\cos u = 1 - \frac{\omega L_s I_d}{\sqrt{2} V}$$

$$u = \cos^{-1} \left[\frac{1 - \omega L_s I_d}{\sqrt{2} V} \right]$$

* If $L_s = 0$

$$u = \cos^{-1}(1) = 0$$

$$V_d = \frac{1}{2\pi} \int_0^{2\pi} v_d(\theta) d\theta$$

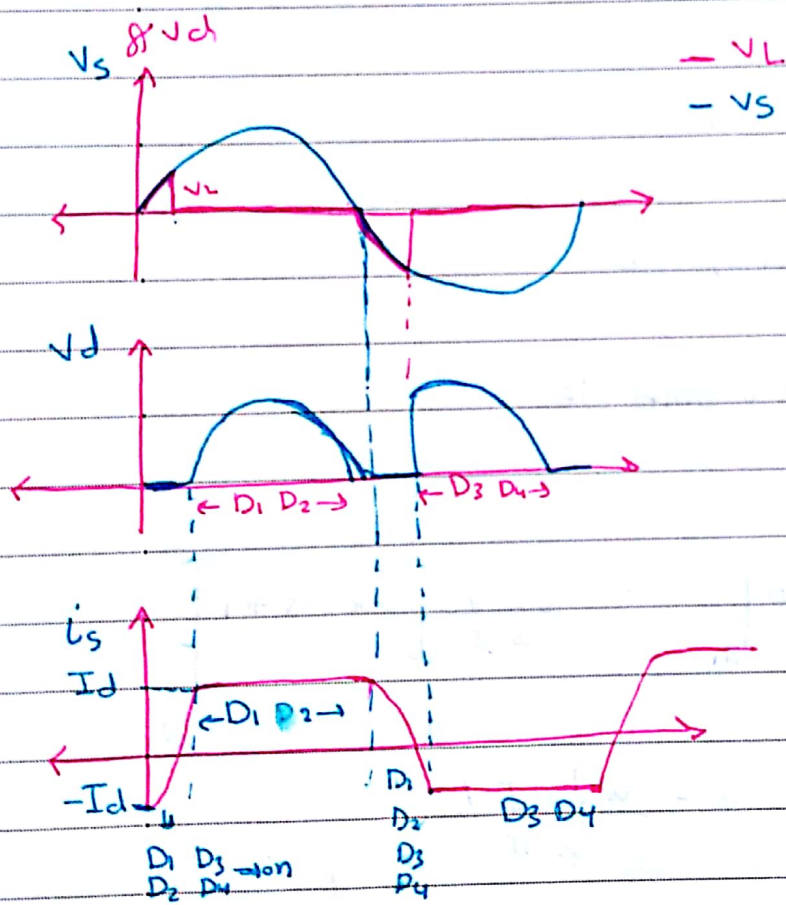
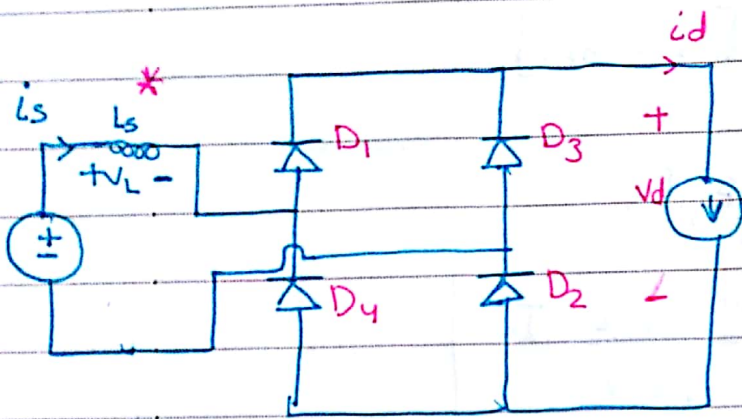
$$= \frac{1}{2\pi} \int_u^{\pi} \sqrt{2} V \sin \theta d\theta$$

$$= \frac{\sqrt{2} V}{2\pi} \left[\cos \theta \right]_u^{\pi} = \frac{\sqrt{2} V}{2\pi} [\cos u + 1]$$

$$V_d = 0.45 V - \frac{\omega L_s I_d}{2\pi}$$

$$\text{If } L_s = 0, V_d = 0.45 V$$

$$P_d = V_d I_d$$



* During Commutation :-

$$V_L = V_s$$

$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t$$

$$\omega L_s \int_{-I_d}^{I_d} di_s = \sqrt{2} V \int_0^u \sin \omega t$$

$$2 \omega L_s I_d = \sqrt{2} V \cos \omega t \Big|_u^0$$

$$2 \omega L_s I_d = \sqrt{2} V [1 - \cos u]$$

$$\cos u = 1 - \frac{2 \omega L_s I_d}{\sqrt{2} V} \quad \neq$$

$$* V_d = \frac{1}{2\pi} \int_0^{2\pi} v_d(\theta) d\theta$$

$$= \frac{2}{2\pi} \int_u^\pi \sqrt{2} V \sin \theta d\theta$$

$$= \frac{\sqrt{2} V}{\pi} \cos \theta \Big|_\pi^u = \frac{\sqrt{2} V}{\pi} [\cos u + 1]$$

$$V_d = 0.9 V - \frac{2 \omega L_s I_d}{\pi} \quad \neq$$

at highly
inductive load

constant
current.

interduced u

+ inductive

* ووجود L_s

تقل V_d , P_d , u

During commutation

$$V_L = V_s.$$

$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t.$$

$$\omega L_s \int di_s = \sqrt{2} V \int \sin \omega t \dots (+K)$$

↓ $i_s(0) = -I_d$

$$\omega L_s i(\theta) = \sqrt{2} V \cos \omega t + K$$

$$P = V I_1 \quad (\text{a.c.})$$

$$I_1 = \frac{b_1}{\sqrt{2}}$$

$$i(\theta) = \begin{cases} I_d & 0 < \theta < \mu \\ I_d & \mu < \theta < \pi \\ -I_d & \pi < \theta < \pi + \mu \\ -I_d & \pi + \mu < \theta < 2\pi \end{cases}$$

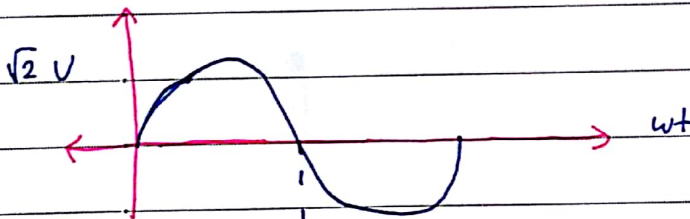
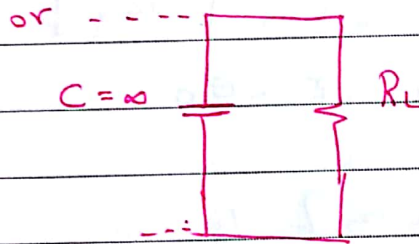
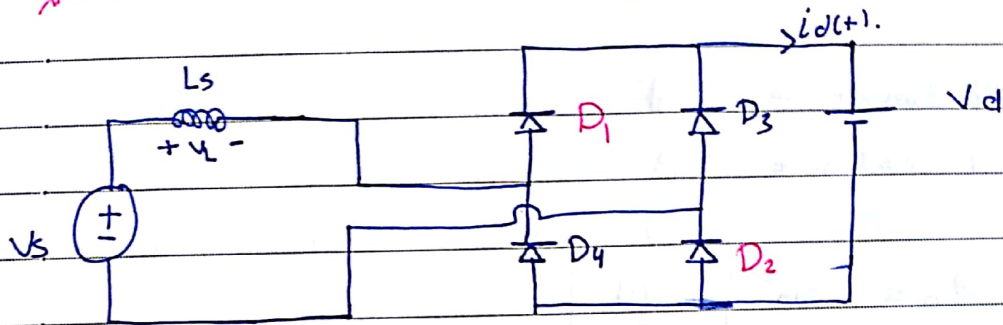
≈ a.c. side.

* Power (d.c.) :-

$$P_d = V_d I_d$$

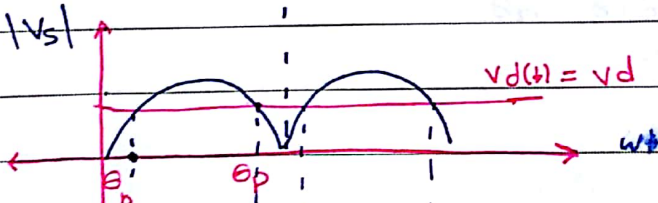
$$P_d = P.$$

* Constant dc-side voltage $v_d(t) = V_d$.



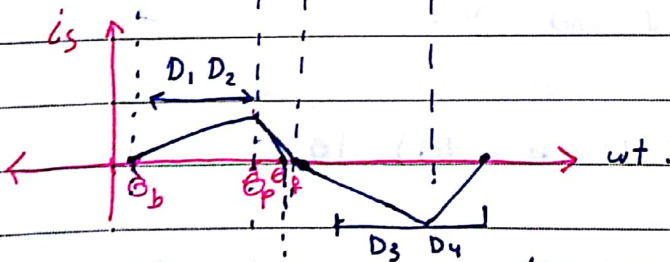
D_1 and D_2 (on) :-

$$-v_s(t) + L_s \frac{di_s}{dt} + v_d = 0$$



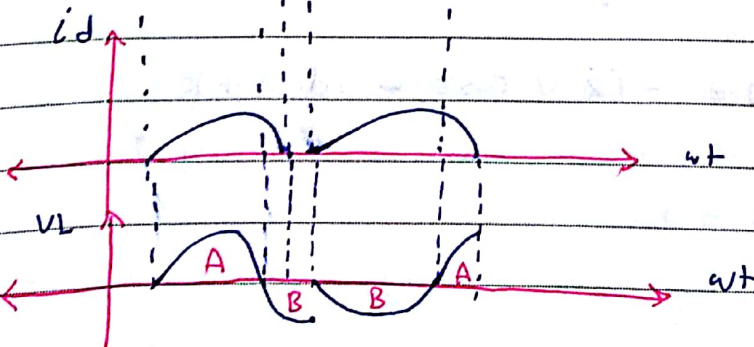
$$\omega L_s \frac{di_s}{dt} = \sqrt{2} v_s \sin \omega t - v_d$$

↳ $\int \dots$



$$\theta_p = \pi - \theta_b$$

Peak value Current $i_s \Rightarrow v_d = v_s$.



$$V_s = V_d.$$

$$\sqrt{2} V \sin \omega t = V_d$$

$$\sqrt{2} V \sin \theta_b = V_d$$

$$\theta_b = \sin^{-1} \left[\frac{V_d}{\sqrt{2} V} \right]$$

$$\theta_p = \pi - \theta_b.$$

$$\theta_f = ?$$

$$I_d = \frac{2}{2\pi} \int_{\theta_b}^{\theta_f} i_d(\theta) d\theta$$

For $i_d(\theta) \Rightarrow$

$$\omega L_s \frac{di_d}{d\theta} = \sqrt{2} V \sin \theta - V_d.$$

$$\omega L_s di_d(\theta) = (\sqrt{2} V \sin \theta - V_d) d\theta$$

$$\omega L_s \int di_d(\theta) = \int \sqrt{2} V \sin \theta - V_d d\theta + K$$

$$\omega L_s i_d(\theta) = -\sqrt{2} V \cos \theta + V_d \theta + K$$

$$i_d(\theta_b) = 0$$

$$\omega L_s i_d(\theta_b) = -\sqrt{2} V \cos \theta_b - v_d \theta_b + K.$$

$$0 = -\sqrt{2} V \cos(\theta_b) - v_d \theta_b + K.$$

$$K = \sqrt{2} V \cos(\theta_b) + v_d \theta_b.$$

$$i_d(\theta) = \frac{1}{\omega L_s} \left[-\sqrt{2} V \cos \theta - v_d \theta + \sqrt{2} V \cos \theta_b + v_d \theta_b \right]$$

$$i_d(\theta_f) = 0 = \frac{1}{\omega L_s} \left[-\sqrt{2} \cos(\theta_f) - v_d \theta_f + \underbrace{\sqrt{2} V \cos \theta_b + v_d \theta_b}_{\text{constant}} \right]$$

non linear algebraic equation.

⇓

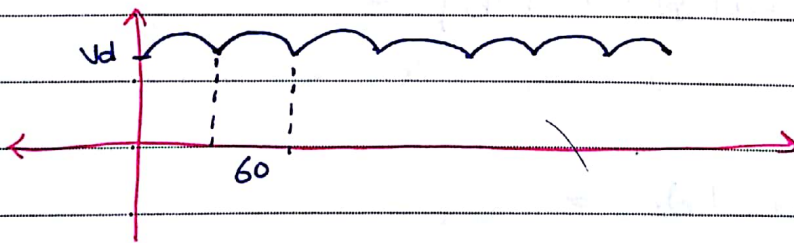
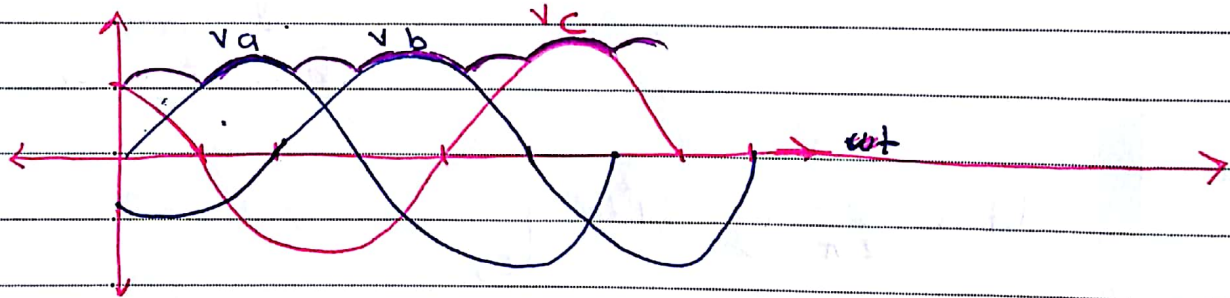
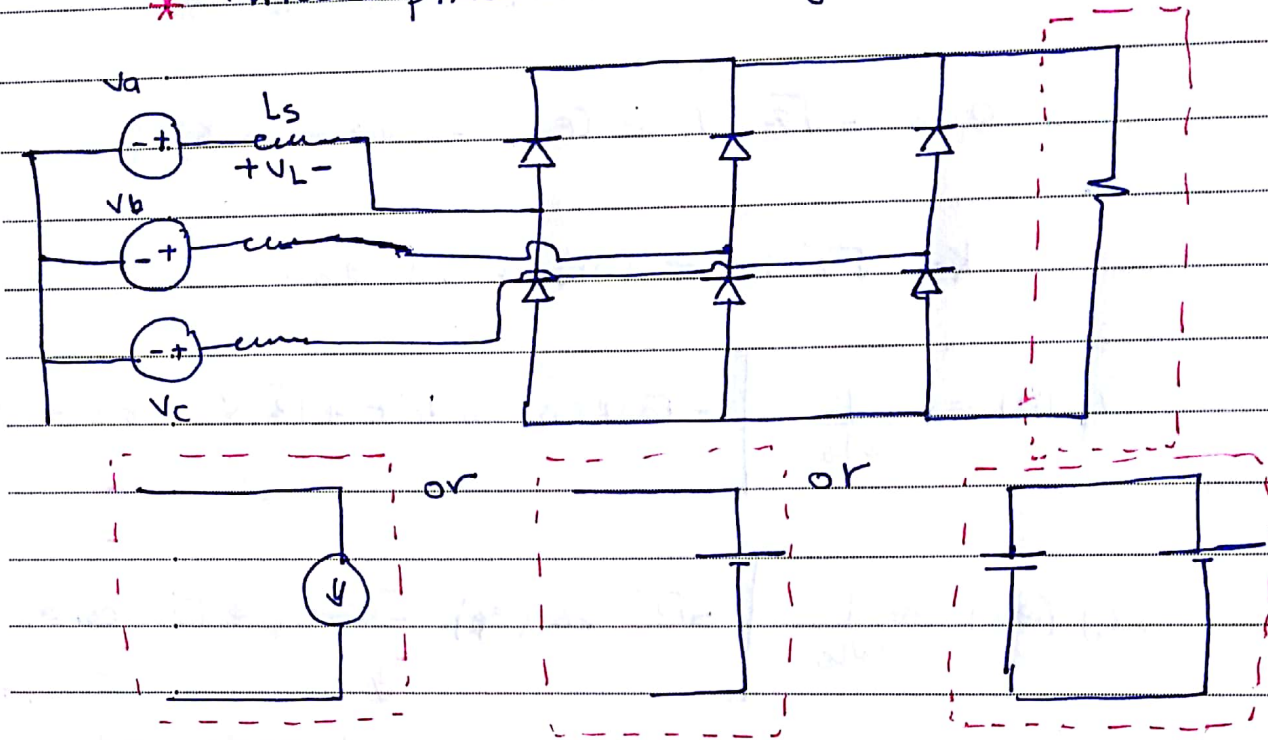
Trial & Error

$$I_d = \frac{2}{2\pi} \times \frac{1}{2} \int_{\theta_b}^{\theta_f} i_d^2(\theta) d\theta$$

$$= \frac{1}{2\pi} \left[i_d^2(\theta_f) - i_d^2(\theta_b) \right] =$$

$$P = I_d v_d =$$

* Three-phase Full-Bridge Rectifier.



- 1- Smoother output voltage (lower ripple).
- 2- Higher power.

$$V_d = 1.35 V_L \rightarrow \text{rms.}$$

$$v_a(t) = \sqrt{2} V \sin(\omega t)$$

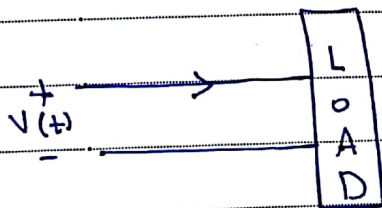
$$v_b(t) = \sqrt{2} V \sin(\omega t - 120^\circ)$$

$$v_c(t) = \sqrt{2} V \sin(\omega t + 120^\circ)$$

$$V_{LL} = \sqrt{3} V$$

$$V_d = 1.35 V_{LL} = 1.33 \times \overset{1.73}{\uparrow} \sqrt{3} V$$

5-3 pp. 114 8-



$$v(t) = V_d + \sqrt{2} V_1 \cos(\omega_1 t) + \sqrt{2} V_1 \sin(\omega_1 t) + \sqrt{2} V_3 \cos(\omega_3 t)$$

$$i(t) = I_d + \sqrt{2} I_1 \cos(\omega_1 t) + \sqrt{2} I_3 \cos(\underbrace{\omega_3 t - \phi_3}_{3\omega_1})$$

(a) $P = ?$

$$P = \frac{1}{T_1} \int_0^{T_1} v(t) i(t) dt$$

$$= \frac{1}{T_1} \int_0^{T_1} [V_d + \sqrt{2} V_1 \cos(\omega_1 t) + \sqrt{2} V_1 \sin(\omega_1 t)$$

$$+ \sqrt{2} V_3 \cos(\omega_3 t)] [I_d + \sqrt{2} I_1 \cos(\omega_1 t) + \sqrt{2} I_3 \cos(\omega_3 t - \phi_3)] dt =$$

$$= V_d I_d + V_1 I_1 + V_3 I_3 \cos \phi_3$$

$$\int \sin x \cdot \sin x = 0$$

$$\int \cos x \cdot \cos 3x = 0$$

حرف = Power given $\sin \times \cos$ ①

حرف = $\sin \times \sin 3x$ ②

9. وقتی Phase shift = Power given ①

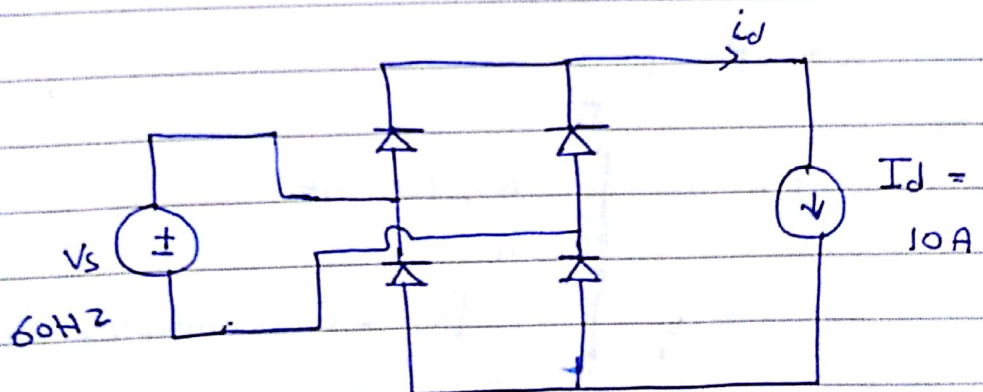
$$V_{rms} = \sqrt{V_d^2 + V_1^2 + V_1^2 + V_3^2}$$

$$I_{rms} = \sqrt{I_d^2 + I_1^2 + I_3^2}$$

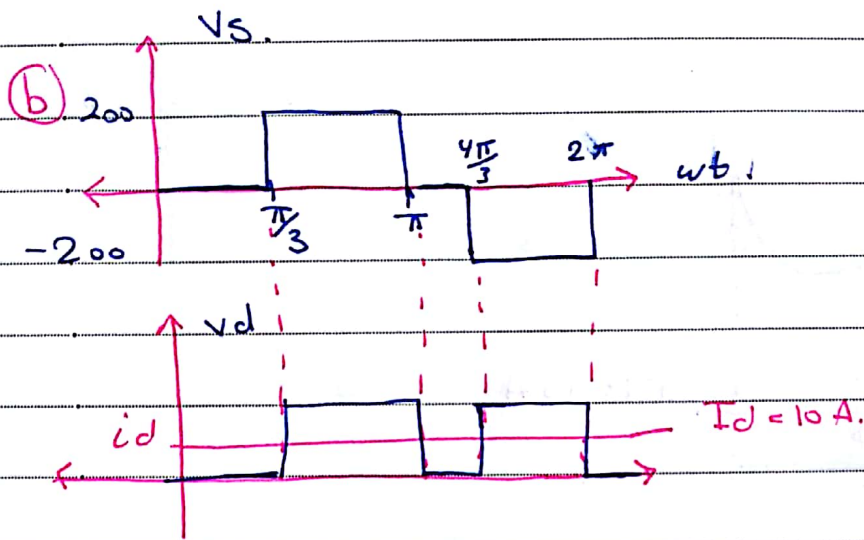
c) $S = \frac{V}{rms} \frac{I}{rms} =$

d) $PF = \frac{P}{S} = \frac{V_d I_d + V_1 I_1 + V_3 I_3 \cos \phi_3}{S}$

5-4)



a) IP Vs is sinusoidal with $V = 120V$.

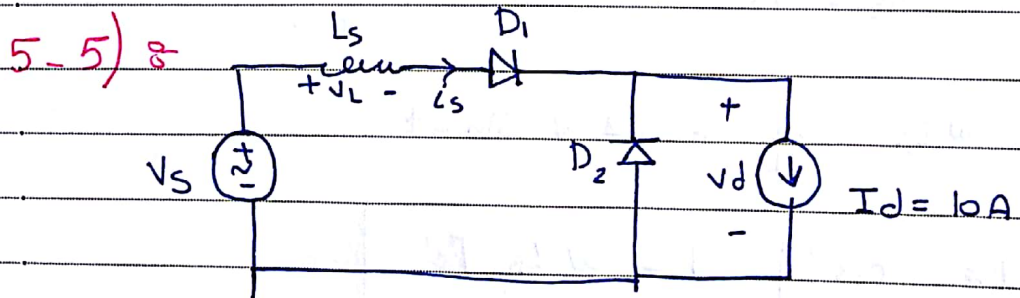


$$P = \frac{1}{2\pi} \int_0^{2\pi} v(\theta) i(\theta) d\theta.$$

$$= \frac{2}{2\pi} \int_{\pi/3}^{\pi} (200)(10) d\theta.$$

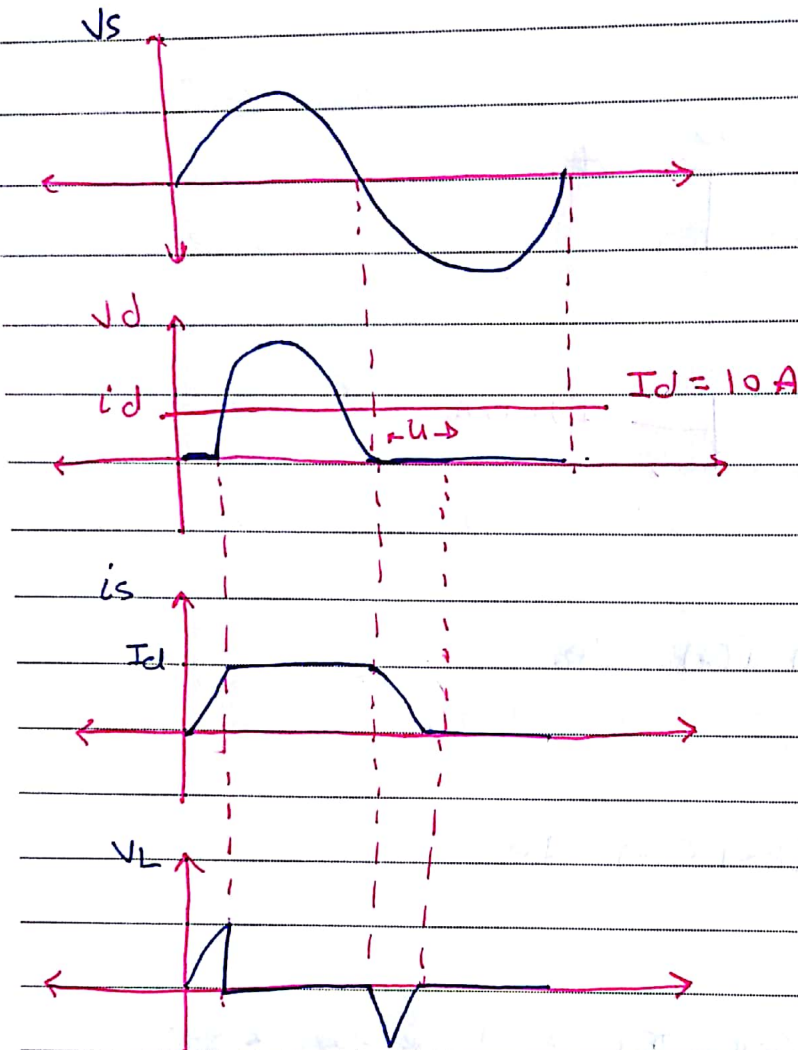
$$= \frac{1}{\pi} \times 2000 \left(\frac{3\pi}{3} - \frac{\pi}{3} \right) = \frac{1}{\pi} \times 2000 \times \frac{2\pi}{3}$$

$$= 1333.33 \text{ w.}$$



$$L_s = 5\text{mH} \cdot 60\text{Hz} \cdot u, v_d, P_d ?$$

$$V = 120.$$



During commutation.

$$V_L = V_s$$

$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t$$

$$u = \cos^{-1} \left[1 - \frac{\omega L_s I_d}{\sqrt{2} V} \right]$$

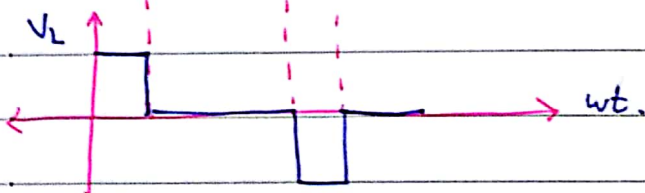
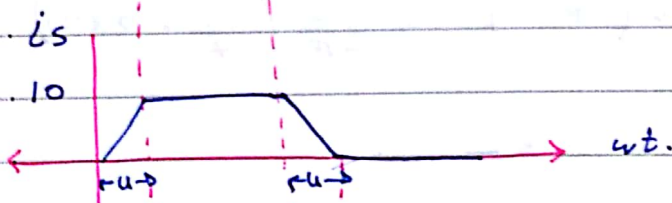
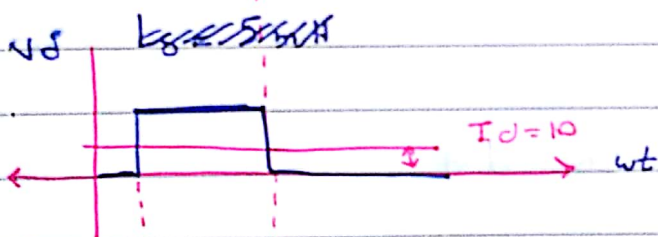
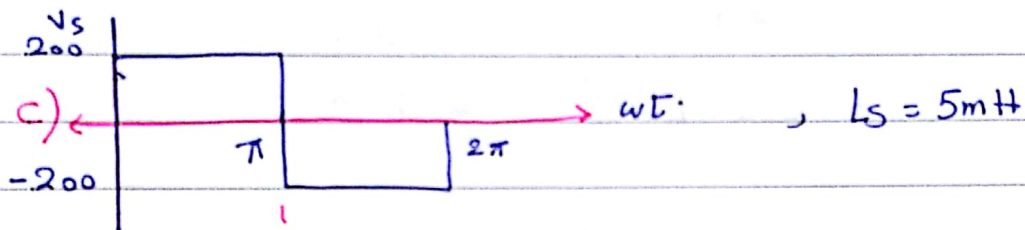
$$= \cos^{-1} \left[1 - \frac{2\pi f (5 \times 10^{-3}) \times 10}{\sqrt{2} \times 120} \right] = \cos^{-1}(0.8886)$$

$$V_d = 0.45 V - \frac{\omega L_s I_d}{2\pi}$$

$$= 0.45 * 120 - \frac{(2\pi * 60) * 5 * 10^{-3} * 10}{2\pi}$$

=

$$P_d = V_d I_d = V_d * 10 =$$



During commutation.

$$v_L = v_s$$

$$\omega L_s \frac{di_s}{dt} = 200$$

$$\omega L_s \int_0^u di_s = \int_0^u 200 dt$$

$$\omega L_s I_d = 200u$$

$$u = \frac{\omega L_s I_d}{200} = \frac{(2\pi 60) 5 \times 10^{-3} \times 10}{200}$$

$$= 0.094 \text{ rad} = 5.4^\circ$$

$$= 0.094 \times \frac{180}{\pi} = 5.4^\circ$$

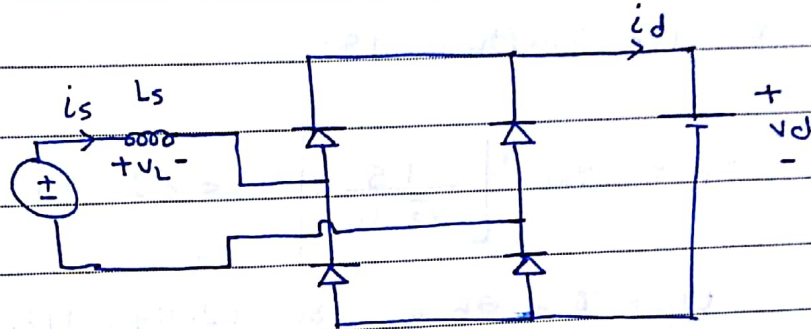
$$v_d = \frac{1}{2\pi} \int_u^\pi 200 dt$$

$$= \frac{1}{2\pi} 200 (\pi - u) = \frac{200}{2\pi} \left(\frac{22}{7} - 0.094 \right)$$

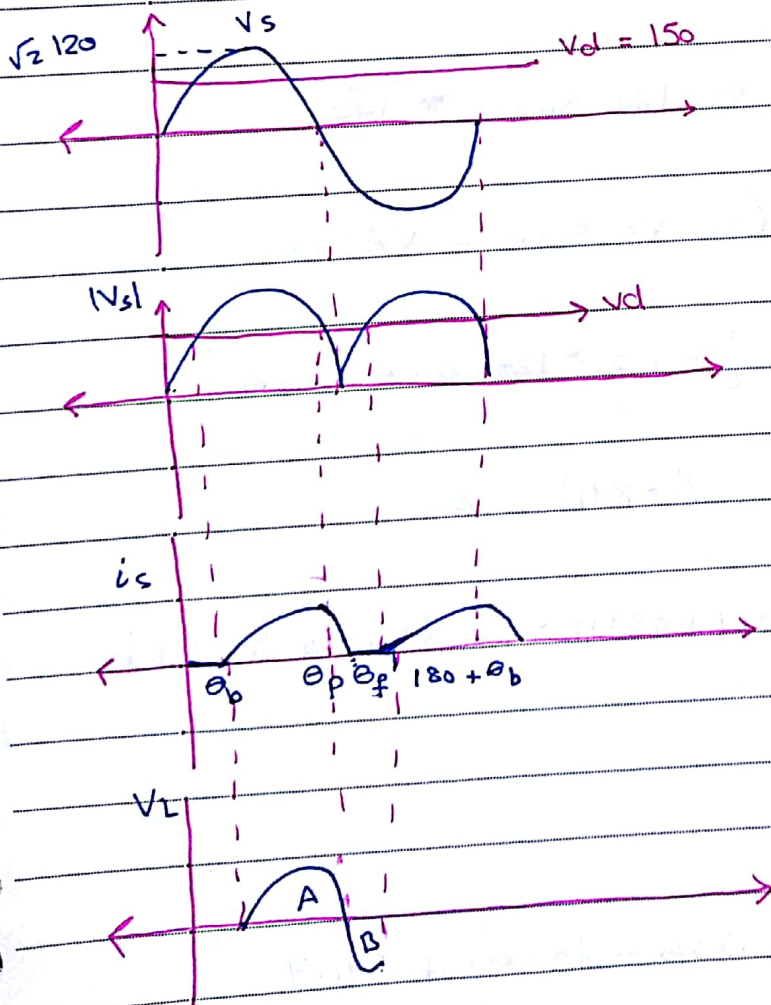
~~$$= \frac{200}{2\pi} \left(\frac{22}{7} - 0.094 \right)$$~~

$$P_d = v_d I_d$$

* P(5-11) PP (115).



$V_s = 120$, 60Hz , $L_s = 1\text{mH}$, $v_d = 50\text{V}$
 i_d , θ_b , ϕ , $I_d \text{ peak}$, $I_d = ??$



$$V_s = v_d$$

$$\sqrt{2} 120 \sin \theta_b = 150$$

$$\theta_b = \sin^{-1} \left[\frac{150}{\sqrt{2} 120} \right] = 62.114^\circ = (1.0841 \text{ rad})$$

$$\begin{aligned} \theta_p = \pi - \theta_b &= 180 - 62.114 = 117.89. \\ &= 2.0575 \text{ rad}. \end{aligned}$$

$$-V_s + L_s \frac{d i_s}{dt} + v_d = 0$$

$$\omega L_s \frac{d i_d}{dt} = \sqrt{2} 120 \sin \omega t + 150.$$

$$\omega L_s d i_d = (\sqrt{2} V_s \sin \theta - v_d) d \theta$$

$$i_d(\theta) = \frac{1}{\omega L_s} \left[-\sqrt{2} * 120 \cos \theta - v_d \theta \right]$$

$$i_d(\theta_b) = i_d(1.0841) = 0$$

$$\frac{1}{\omega L_s} \left[-\sqrt{2} V_s \cos(1.0841) - (150)(1.0841) \right] + K.$$

$$K = 641.9.$$

$$i_d(\theta) = 2.65 \left[-169.7 \cos \theta - 150 \theta \right] + 641.9$$

* Peak value i_d when θ_p .

$$i_d(\theta_p) = i_d(2.0575) = 2.65 \left[-169.7 \cos(2.0575) - 150 \times 2.0575 \right] + 641.9$$

$$* I_d = \frac{2}{2\pi} \int_{\theta_b}^{\theta_f} i_d(\theta) d\theta.$$

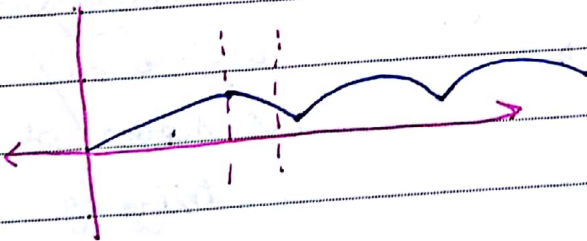
$$= \frac{1}{\pi} \int_{1.0841}^{\theta_f} 2.65 \left[-169.7 \cos(\theta) - 150\theta \right] + 641.9 d\theta.$$

$$\theta_f = ?$$

$$i_d(\theta_f) = 0 = 2.65 \left[-169.7 \cos(\theta_f) - 150\theta_f \right] + 641.9$$

بالتعويض نجد θ_f من (130-140)

لوكات θ_f اكبر $\pi + \theta_b$ مع بقاء ripple في صورة θ_f

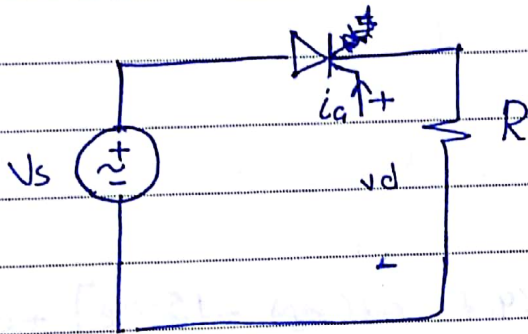


Ch 6 :-

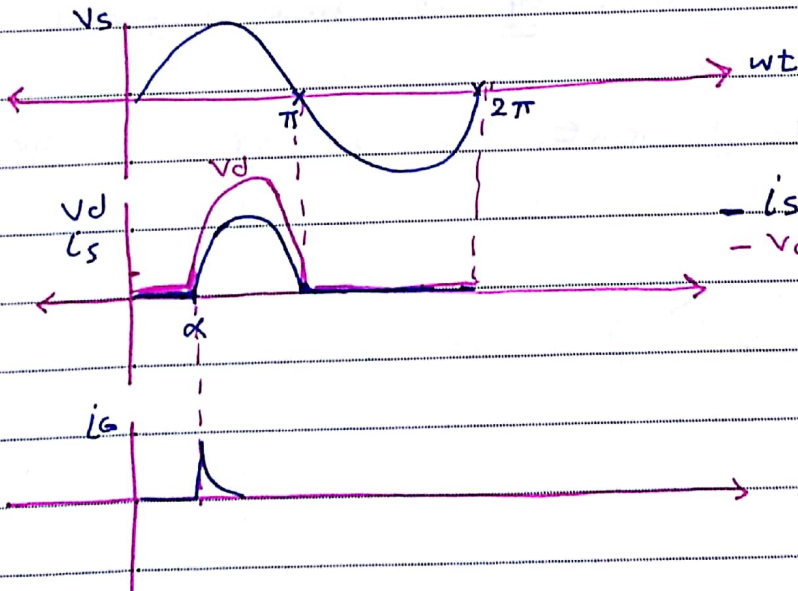
Line frequency phase - controlled Rectifiers and Inverters :-

Line frequency ac \Rightarrow Controlled dc
Thyristors.

* Basic Thyristors Circuits.



Half-wave controlled Rectifier Circuit with Pure resistive Load



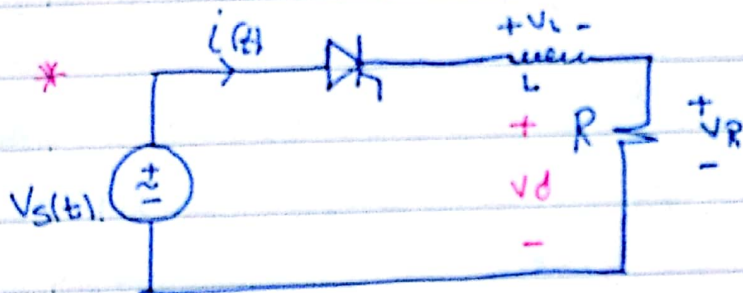
α is firing angle
 $\alpha = \omega t_0$
 t_0 - instant of triggering.

α Fri
 $\alpha = \omega t$
 t_0 instant of triggering

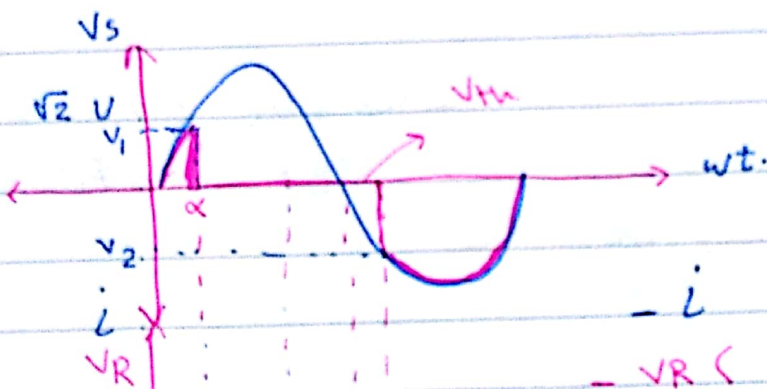
$$V_d = \frac{1}{2\pi} \int_{\alpha}^{\pi} \sqrt{2} V_s \sin \theta d\theta$$

$$= \frac{\sqrt{2} V}{2\pi} \left[\cos \theta \right]_{\alpha}^{\pi}$$

$$= \frac{\sqrt{2} V}{2\pi} [\cos \alpha + 1]$$

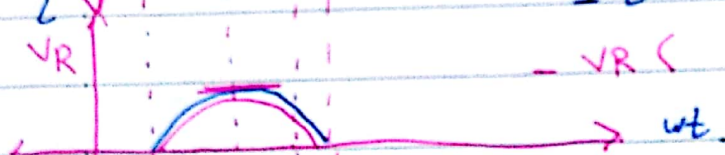


$$-\sqrt{2} V \sin \omega t + L \frac{di}{dt} + Ri = 0$$

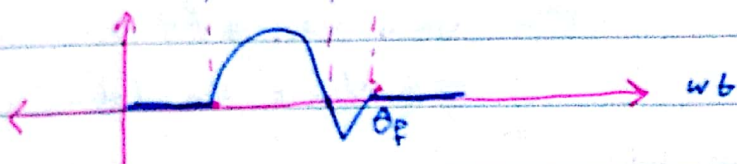
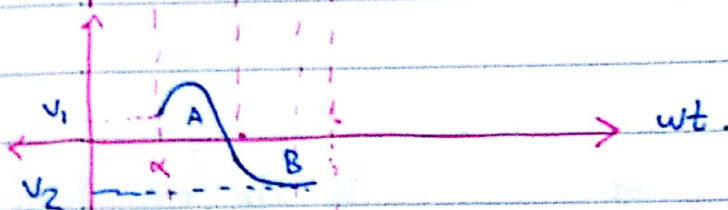


$$V_L = \sqrt{2} V \sin \omega t - Ri$$

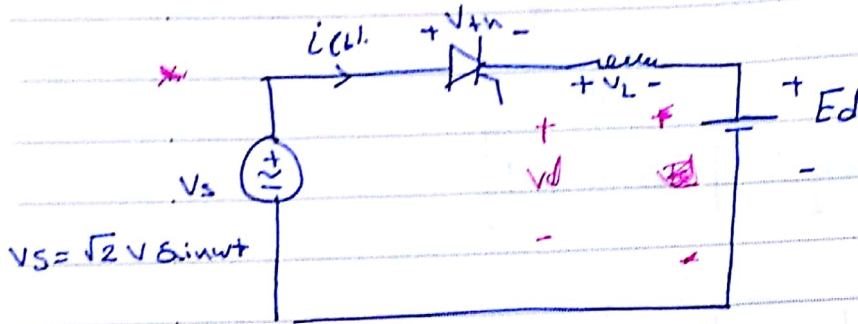
V_L always goes negative
 v_s only zero



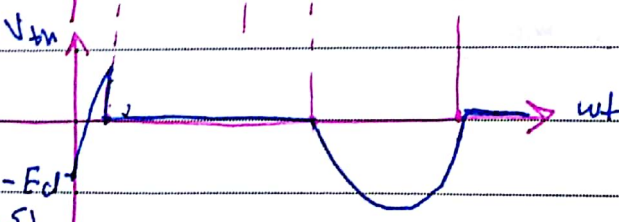
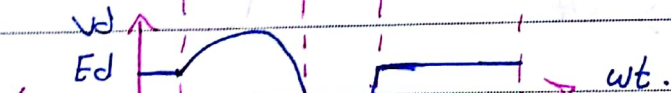
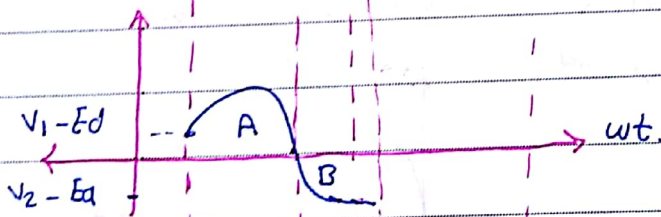
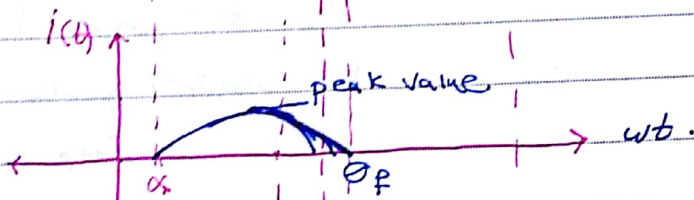
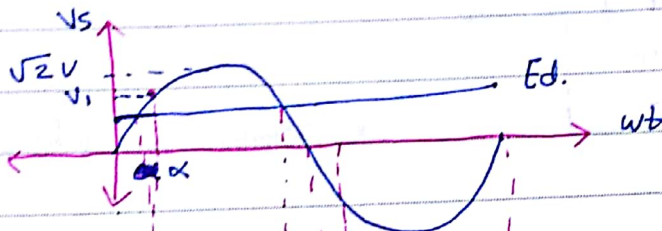
آب لایه آبی



$$V_d = \frac{1}{2\pi} \int_{\alpha}^{\theta_f} \sqrt{2} V \sin \omega t \, d\omega t$$



The (on) \Rightarrow V_s \geq E_d
 - V_s \geq E_d \Rightarrow V_s \geq E_d
 - $V_s < E_d$ \Rightarrow $V_s < E_d$



$$-V_s + V_L + E_d = 0$$

$$V_L = V_s - E_d$$

if the the off \Rightarrow

$$-V_s + V_{th} + E_d = 0$$

$$V_{th} = V_s - E_d$$

negative voltage
 The cycle

$$V_L = V_s - E_d.$$

$$\omega L \frac{di}{dt} = \sqrt{2} V \sin \omega t - E_d.$$

$$\omega L di = (\sqrt{2} V \sin \omega t - E_d) dt.$$

$$\omega L i(\theta) = -\sqrt{2} V \cos(\theta) - E_d \theta + k.$$

$$i(\alpha) = 0 \Rightarrow k = ??$$

α is known.

$$V_L = L \frac{di(\theta)}{d\theta}.$$

$$i(\theta_p) = 0 \Rightarrow \theta_p.$$

$$V_d = \frac{1}{2\pi} \int_0^{2\pi} v_d(\theta) d\theta$$

$$= \frac{1}{2\pi} \left[\int_0^{\alpha} E_d d\theta + \int_{\alpha}^{\theta_p} \sqrt{2} V \sin \theta d\theta + \int_{\theta_p}^{2\pi} E_d d\theta \right]$$

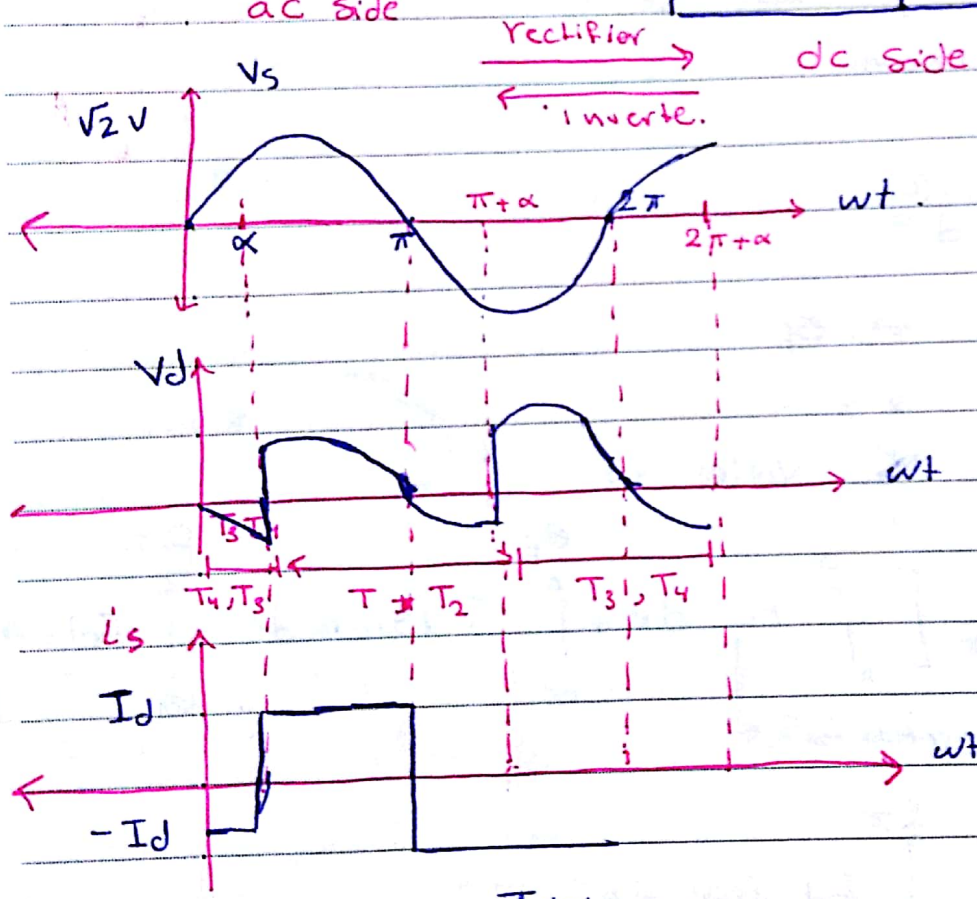
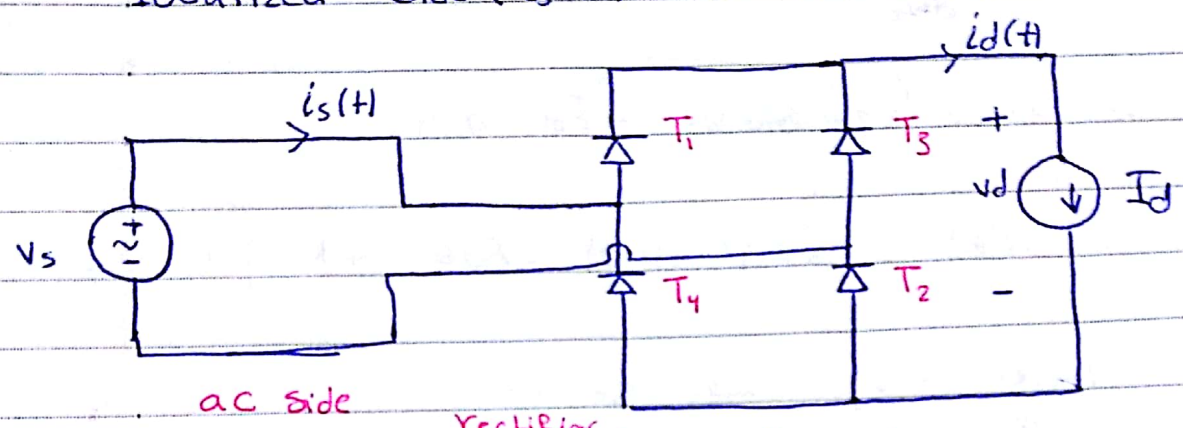
. $\int_0^{\alpha} E_d d\theta$ is the area under the curve.

$$P_d = \frac{1}{2\pi} \int_0^{2\pi} E_d i(\theta) d\theta.$$

$$P_d = \frac{E_d}{2\pi} \int_{\alpha}^{\theta_p} i(\theta) d\theta \Rightarrow \omega.$$

* Single-phase converter.

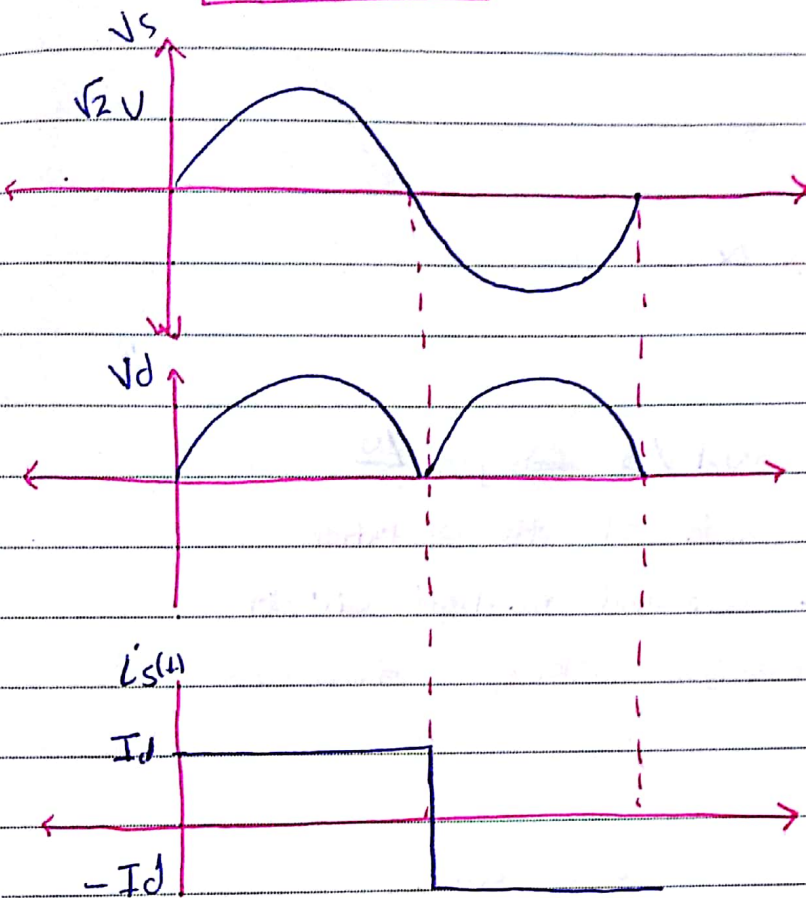
Idealized case ($L_s = 0$) and $i_d(t) = I_d$.



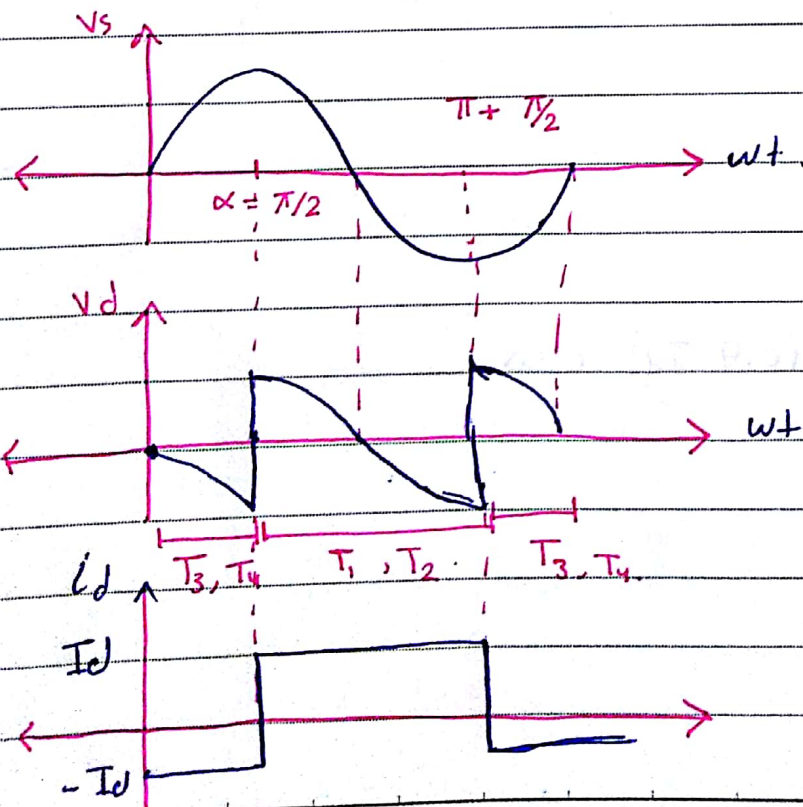
$$V_d = \frac{1}{2\pi} \int_{\alpha}^{\pi+\alpha} \sqrt{2} V \sin \theta d\theta = \frac{\sqrt{2} V \cos \theta}{\pi} \Big|_{\pi+\alpha}^{\alpha}$$

$$= \frac{\sqrt{2} V}{\pi} [\cos \alpha - \cos(\pi + \alpha)] = 0.9 V \cos(\alpha)$$

2. if $\alpha = 0$

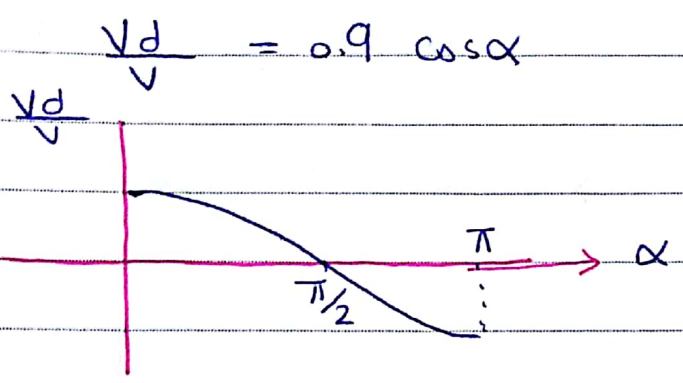


3. if $\alpha = \pi/2$



* انا كانت زاوية اكبوت
يخرج كله اوج ببالب





$\pi/2 < \alpha < \pi \quad V_d < 0 \Rightarrow \text{pd. } \neq 0$

inverter mode of ~~the~~ operation
of the controlled rectifier circuit.

~~reg. operation~~ Regenerative braking on DC side



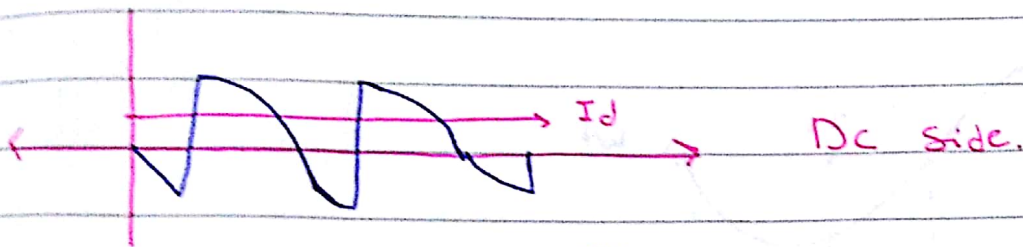
$$P = V I_{s1} \cos \theta_1$$

$$\theta_1 = \alpha$$

rms
value of fundamental
components.

$$I_{s1} = 0.9 I_d$$

$$P = V (0.9 I_d) \cos \alpha$$



$$P_{dc} = V_d I_d$$

$$THD = \sqrt{\frac{I_s^2 - I_{s1}^2}{I_s^2}} \times 100\%$$

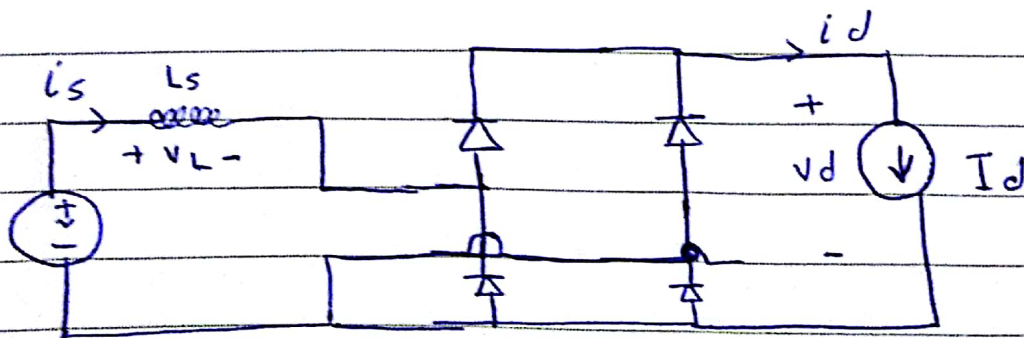
$$I_s = I_d$$

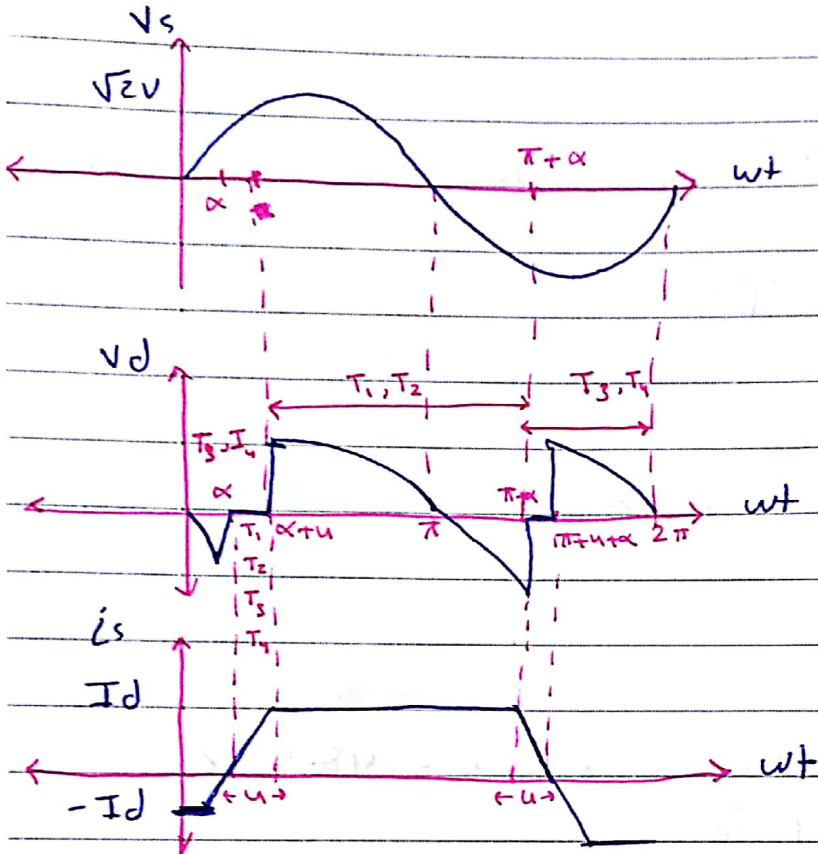
$$= \sqrt{\frac{I_d^2 - (0.9 I_d)^2}{I_d^2}} \times 100\% = 48.43\%$$

$$D_p F = \cos \phi = \cos \alpha$$

$$P F = \frac{I_{s1}}{I_d} \cos \alpha = 0.9 \cos \alpha$$

* Effect of Source inductance ($L_s \neq 0$).





$$V_d = \frac{2}{2\pi} \int_{\alpha+u}^{\pi+\alpha} \sqrt{2} V \sin \theta d\theta$$

$$= \frac{\sqrt{2} V}{\pi} \cos \theta \Big|_{\pi+\alpha}^{\alpha+u} = \frac{\sqrt{2} V}{\pi} [\cos(\alpha+u) - \cos(\pi+\alpha)]$$

$$V_d = 0.9 V \cos \alpha - \frac{2 \omega L_s I_d}{\pi}$$

دوره اولی از سلف سلفی است
 زیرا که در آن زمان

During commutation.

$$V_L = V_s$$

$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \theta$$

$$\omega L_s \frac{di_s}{d\theta} = \sqrt{2} V \sin \theta$$

$$\omega L_s \int_{-I_d}^{I_d} di_s = \int_{\alpha}^{\alpha+\mu} \sqrt{2} V \sin \theta d\theta$$

$$2\omega L_s I_d = \sqrt{2} V \cos \theta \Big|_{\alpha+\mu}^{\alpha}$$

$$2\omega L_s I_d = \sqrt{2} V [\cos(\alpha) - \cos(\alpha+\mu)]$$

*

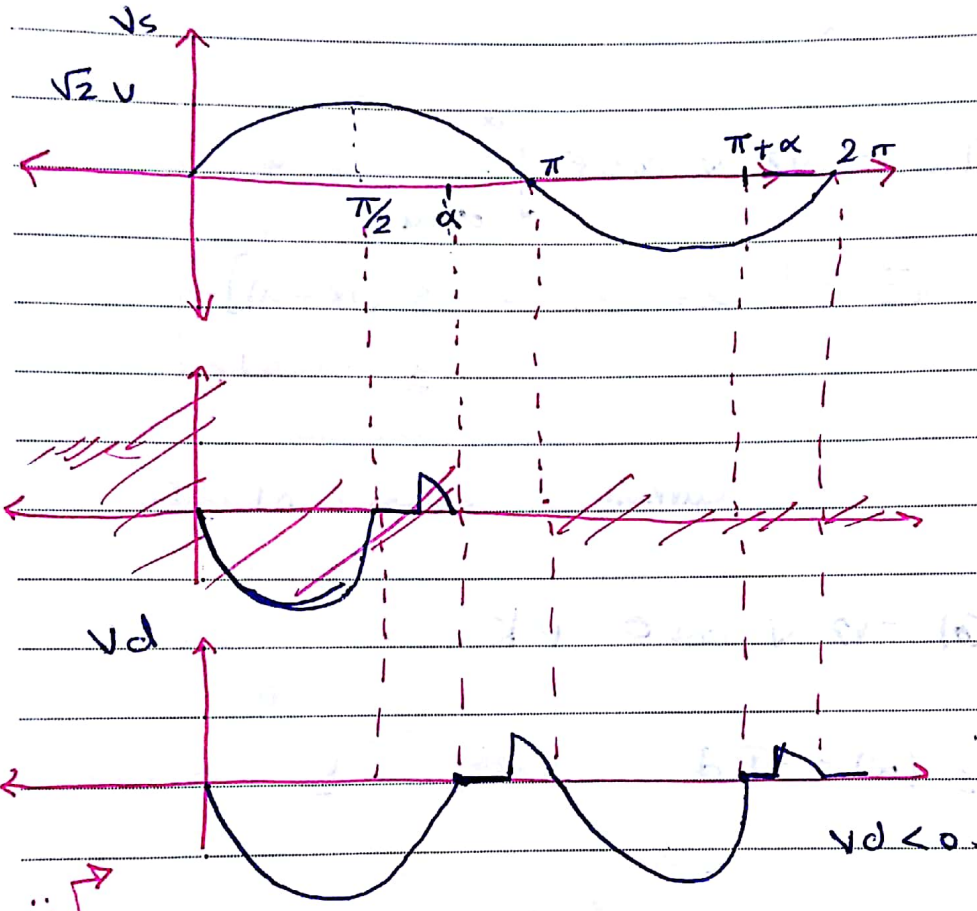
Currents also equal i_{sc}

$$\omega L_s I(\theta) = -\sqrt{2} V \cos \theta + K$$

$$i_s(\alpha) = -I_d \Rightarrow K = \text{constant}$$

* Inverter mode of operation.

① $v_d < 0 \Rightarrow$ if $L_s = 0 \quad \alpha > 90^\circ$

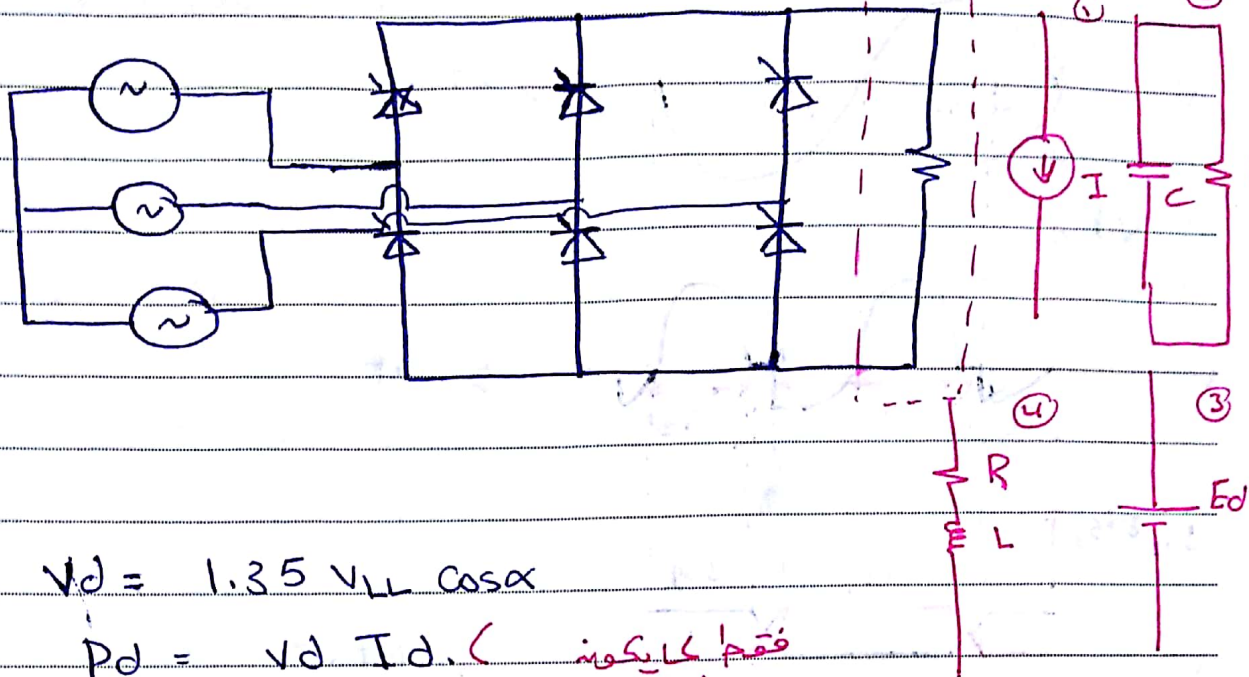


تيار
المصدر

② Source in ^{the} load or energy storage device.

*

* Three-phase Converters 8-



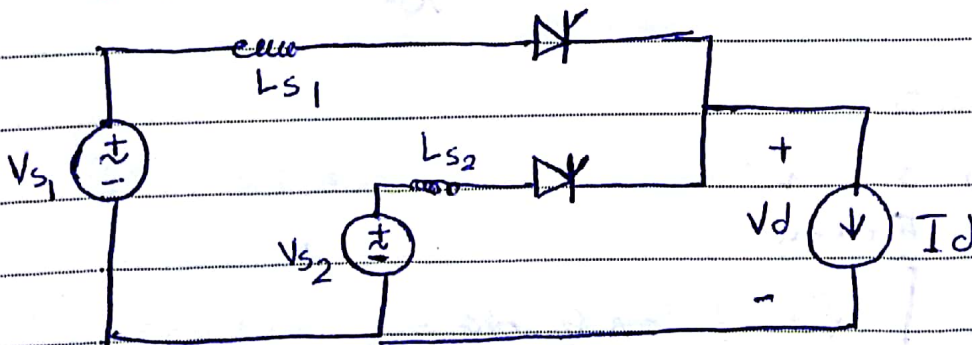
$$V_d = 1.35 V_{LL} \cos \alpha$$

$$P_d = V_d I_d \quad (\text{فقد الطاقة في } I_d \text{ في } \odot)$$

$$P = \underbrace{V I}_{\text{non sin or cos}} \cos \phi$$

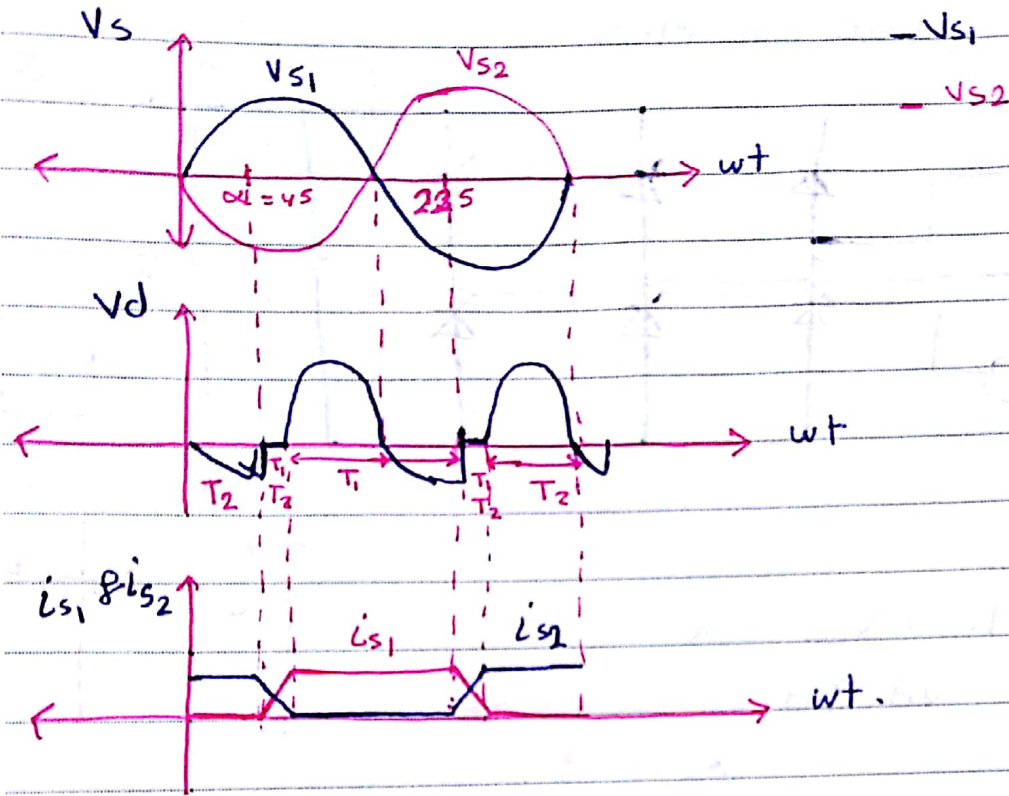
$$P = \frac{1}{2\pi} \int_0^{2\pi} v_d(\omega) i_d(\omega) d\omega$$

* Problem 6-1



$$V_{s1} = V_{s2} = 120 \text{ (rms) out of phase } 180$$

$$L_s = 5 \text{ mH}, \quad I_d = 10 \text{ A } 60 \text{ Hz}, \quad \alpha = 45^\circ$$



* During commutation. B-

$$-V_{s1} + L_s \frac{di_{s1}}{dt} + v_d = 0 \quad \dots (1)$$

$$+ -V_{s2} + L_s \frac{di_{s2}}{dt} + v_d = 0 \quad \dots (2)$$

$$-V_{s1} + L_s \frac{di_{s1}}{dt} + v_d - V_{s2} + L_s \frac{di_{s2}}{dt} + v_d = 0$$

لم عكس V_{s2}
في الإشارة
و قسارين
في مقدار.

$$2v_d = 0$$

$$v_d = 0 \quad \checkmark$$

$$V_d = \frac{2}{2\pi} \int_{\alpha + \mu}^{\pi + \alpha + \mu} \sqrt{2} V \sin \theta \, d\theta =$$

During Commutation :-

u u u

$$V_{L1} = V_{s1}$$

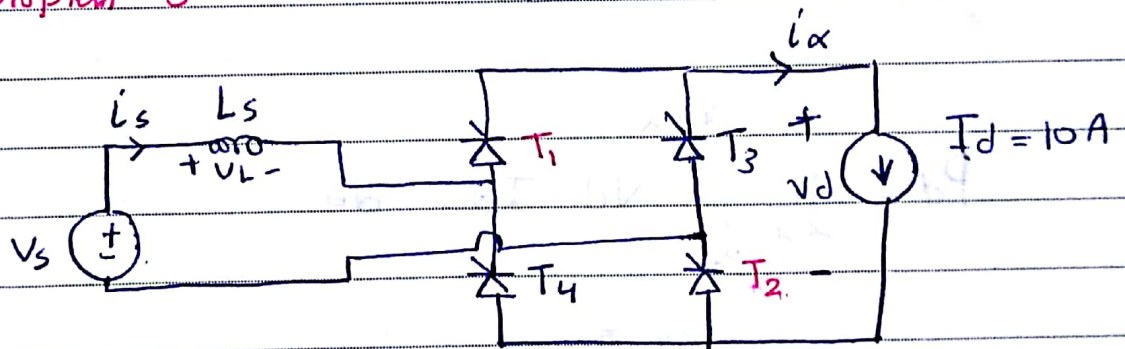
$$\omega L_s \frac{di_s}{dt} = \sqrt{2} V \sin \omega t$$

inverter 5 J2

$$\omega L_s \int_0^{\alpha + \mu} di_s = \int_{\alpha}^{\alpha + \mu} \sqrt{2} V \sin \theta \cdot d\theta$$

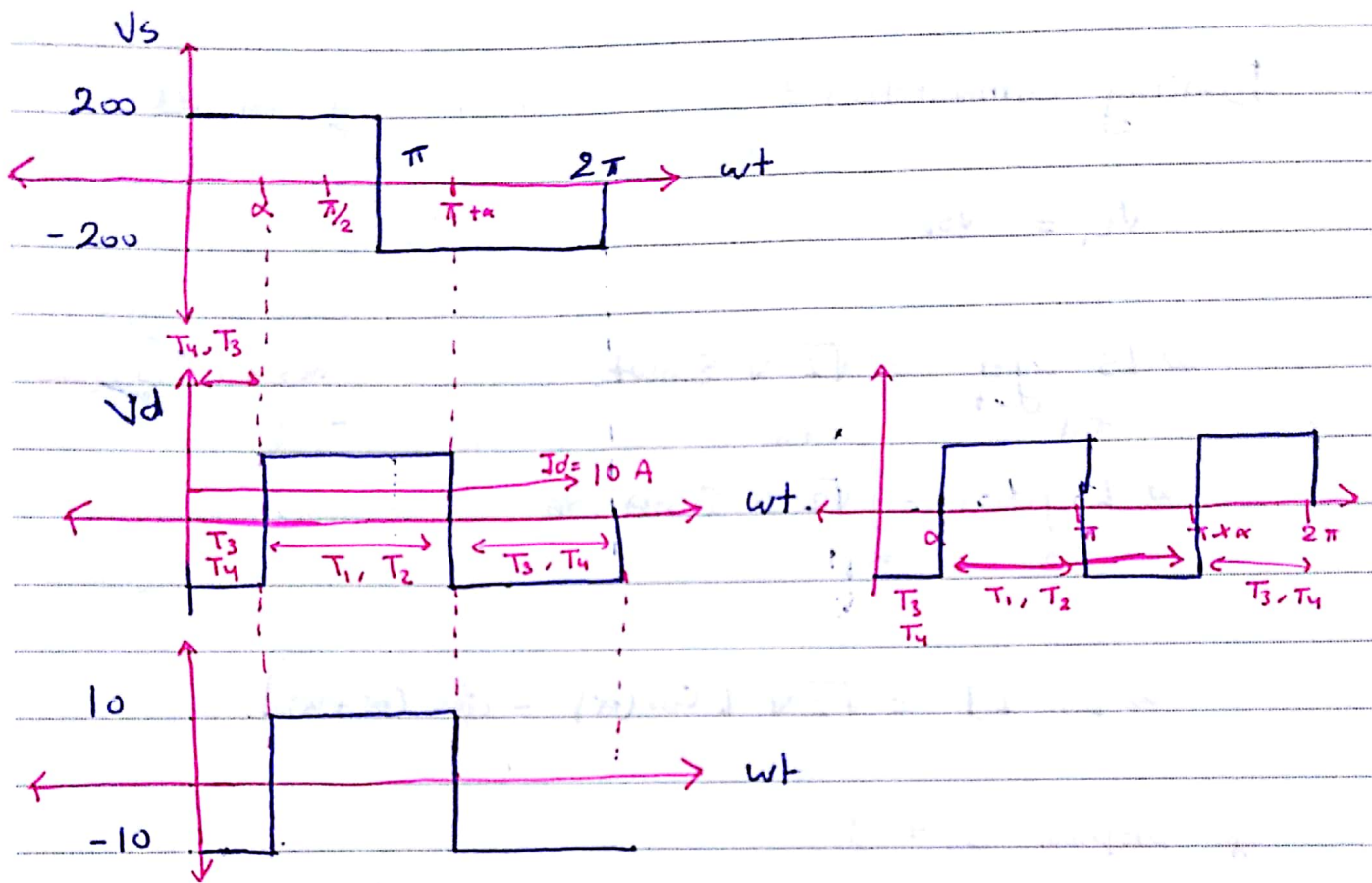
$$\omega L_s I_d = \sqrt{2} V [\cos(\alpha) - \cos(\alpha + \mu)]$$

* problem 6-4 :-



V_s is a square wave with amplitude of 200 V , 60 Hz ; $L_s = 3 \text{ mH}$; $\alpha = 45^\circ$.

(a) If $L_s = 0$.



$$P_d' = \frac{2}{2\pi} \int_{\alpha}^{\pi+\alpha} V_d I_d d\theta$$

$$= \frac{1}{\pi} \int_{\alpha}^{\alpha+\pi} 200 * 10 d\theta$$

$$= \frac{2000}{\pi} (\alpha + \pi - \alpha) = 2000 \text{ watt.}$$

~~$V_d = \frac{2}{2\pi} \int_{\alpha}^{\pi} 200 d\theta = 200 \text{ volt.}$~~

$$V_d = \frac{2}{2\pi} \left[\int_{\alpha}^{\pi} 200 d\theta + \int_{\pi}^{\pi+\alpha} -200 d\theta \right]$$

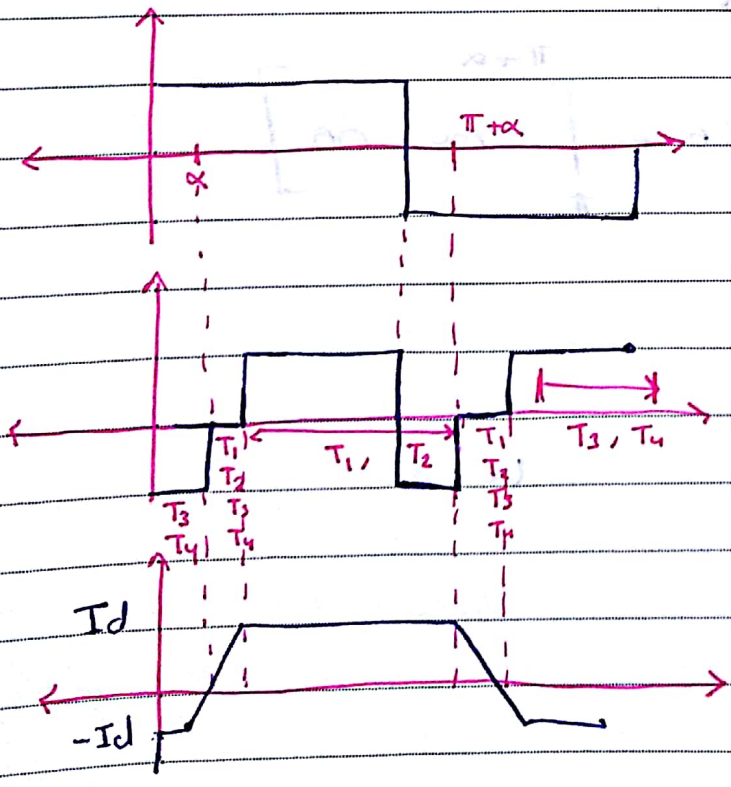
$$P_d = \frac{1}{\pi} \left[\int_{\alpha}^{\pi} 200 \times (10) d\theta + \int_{\pi}^{\pi+\alpha} (-200)(10) d\theta \right]$$

↘ D.c Side

* a.c side

$$P_{ac} = \frac{1}{2\pi} \left[\int_0^{\alpha} 200^2 (-10) d\theta + \int_{\alpha}^{\pi} 200 \times 10 d\theta \right. \\ \left. + \int_{\pi}^{\pi+\alpha} -200 \times 10 d\theta + \int_{\pi+\alpha}^{2\pi} -200 \times -10 d\theta \right]$$

b) If $L_s = 3mH$.



During commutation

$$V_L = V_S.$$

$$\omega L_s \frac{di_s}{dt} = 200$$

$$\omega L_s \int_{-I_d}^{I_d} di_s = \int_{\alpha}^{\alpha+\mu} 200 d\theta$$

$$2\omega L_s I_d = 200(\alpha + \mu - \alpha)$$

$$(2)(2\pi f)(3 \times 10^{-3})(10) = 200\mu$$

$$\mu = 0.11 \text{ rad.}$$

$$= 6.48^\circ.$$

$$V_d = \frac{2}{2\pi} \left[\int_{\alpha+\mu}^{\pi} 200 d\theta + \int_{\pi}^{\pi+\alpha} -200 d\theta \right]$$

=

$$P_d = V_d I_d = \quad W.$$

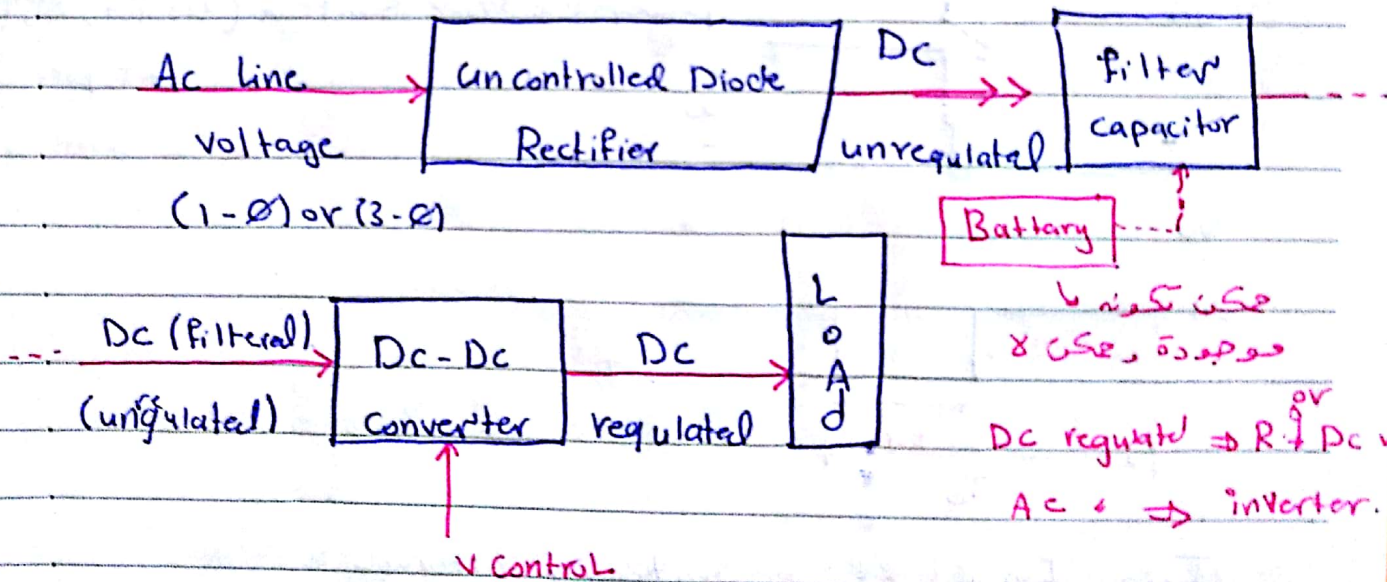
CH 7. dc - dc Switch mode converter :-

* Applications.

- 1- dc motor drive system.
- 2- Regulated power supplies
- 3- Renewable energy system.

* Based on the value of the output voltage compared with the input :-

- 1- step - down converter (Buck)
- 2- Step - up converter (boost)
- 3- Step-up step down (buck - boost).
- 4- Full bridge




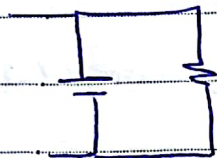
entral Block diagram.

The cct

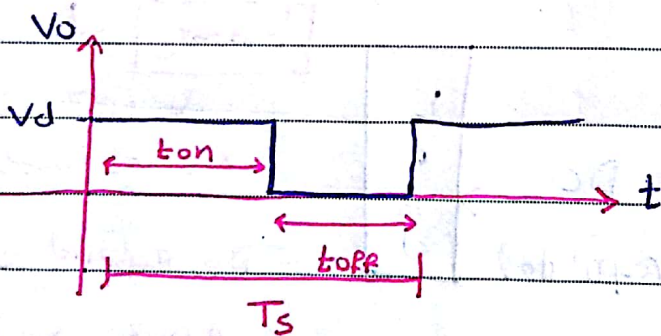
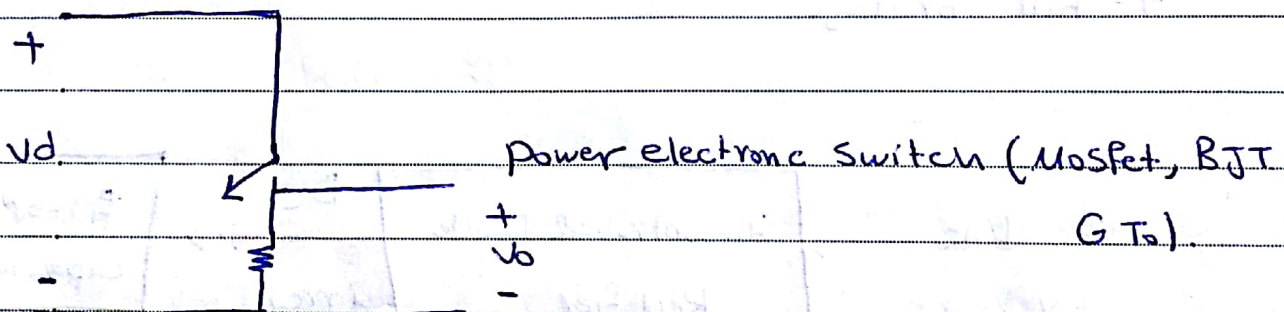
*

1. The cct.
2. The Switch are ideal
3. The capacitor and inductor

 \rightarrow ideal L , $R=0$

 \rightarrow ideal C , $R = \infty$

* Control of dc-dc converters.



$$T_s = t_{on} + t_{off} \equiv \text{Switching Interval.}$$

$$f_s = \frac{1}{T_s} \equiv \text{Switching Frequency. (1 kHz} \rightarrow \text{25 kHz).}$$

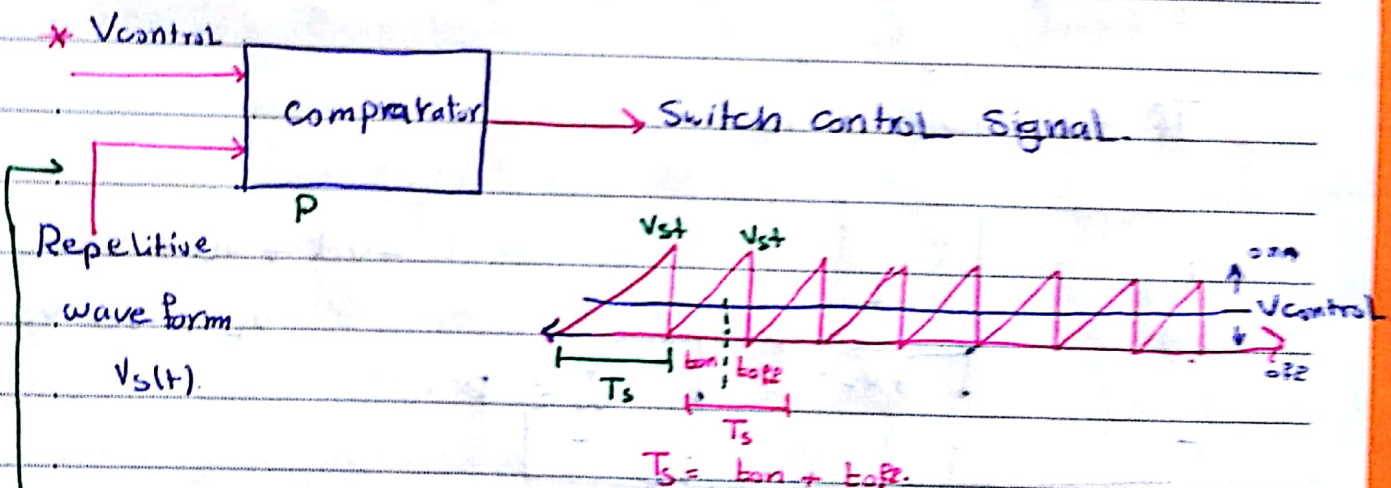
$$V_o = \frac{1}{T_s} \int_0^{T_s} v_o(t) dt$$

$$= \frac{1}{T_s} \int_0^{t_{on}} v_d dt = v_d \frac{t_{on}}{T_s} = v_d D$$

$D \rightarrow$ duty cycle.

To change the average output voltage: either ~~change~~ change t_{on} or T_s

طريقة متبعة في t_{on} و T_s دلتيمت



$V_{control} < v_{st} \Rightarrow$ signal off

$V_{control} > v_{st} \Rightarrow$ on.

~~power~~ * PWM technique for controlling the switches of DC-DC converters.

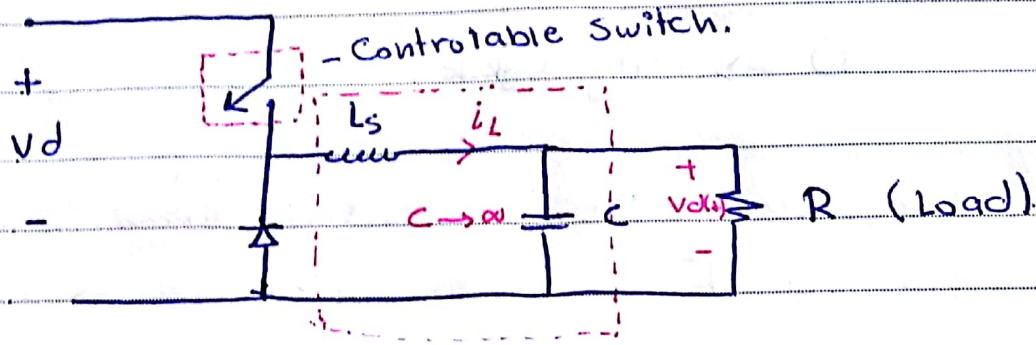
* DC to DC convert Run in to mode

1: Continuous ~~and~~ current conduction mode.

2. dis continuous current conduction.

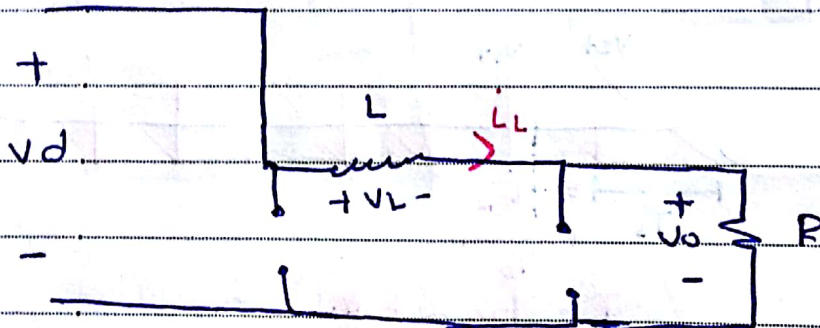
Application: Jall case

* Step down (Buck) converter



$C \rightarrow \infty$ such that $V_o(t) \approx V_o$.

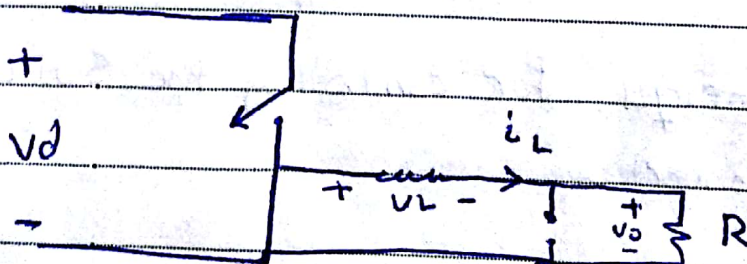
* If the switch is on



$$-V_d + V_L + V_o = 0$$

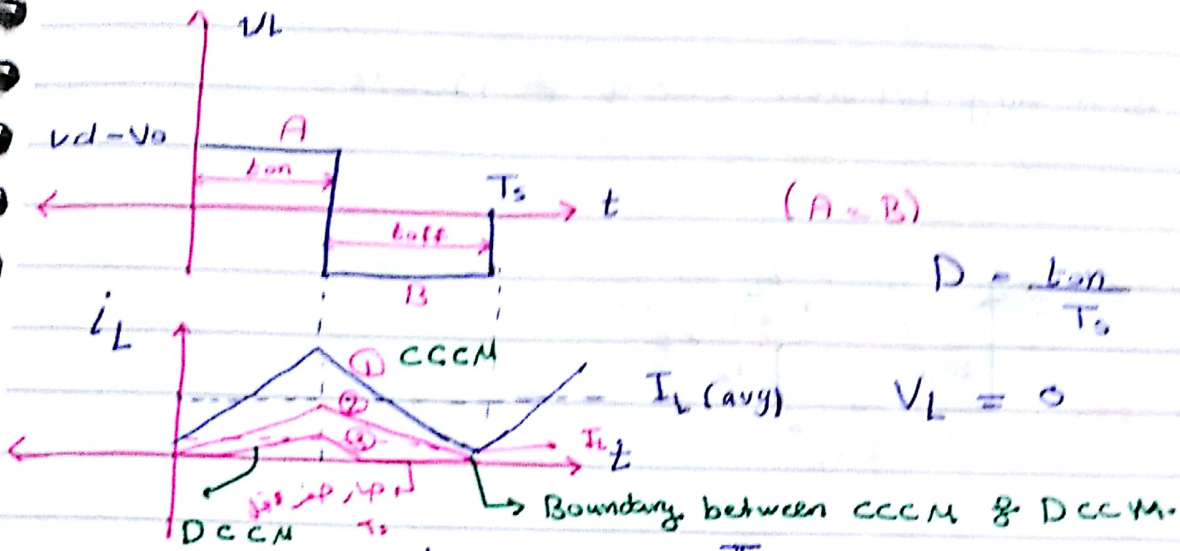
$$V_L = V_d - V_o$$

* If the switch is off



$$V_L + V_o = 0$$

$$V_L = -V_o$$



$$V_L = \int_0^{t_{on}} (v_d - v_o) dt + \int_{t_{on}}^{T_s} -v_o dt = 0$$

$$\Rightarrow (v_d - v_o)(t_{on}) + -v_o(T_s - t_{on}) = 0$$

$$v_d t_{on} - v_o t_{on} - v_o T_s + v_o t_{on} = 0 \quad \text{① CCM}$$

$$v_d t_{on} = v_o T_s$$

$$\frac{v_o}{v_d} = \frac{t_{on}}{T_s} = D$$

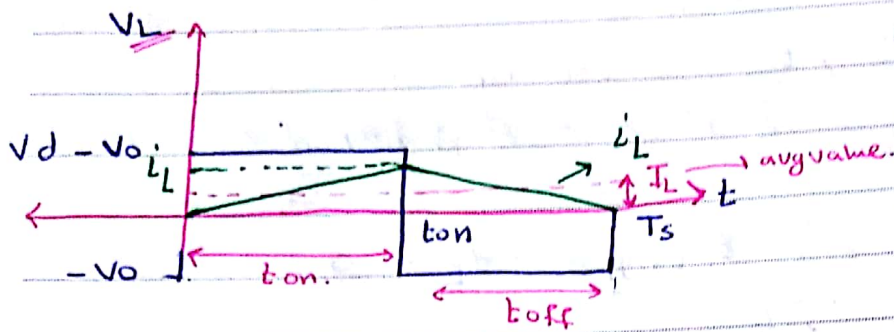
$$v_o = D v_d, \quad D = 0 \rightarrow 1, \quad \frac{I_o}{I_d} = \frac{1}{D}$$

$$v_o I_o = v_d I_d$$

$v_o < v_d \Rightarrow$ Step down convert.

* على Load مع current عالية كبرية .
* Load صغيره كبرية مع current قليلة كبرية .

* Boundary between CCM & DCCM



$$I_{LB} = \frac{1}{2} i_{L peak}$$

$$I_{LB} = \frac{1}{T_s} \left[\frac{1}{2} t_{on} i_{L peak} + \frac{1}{2} t_{off} i_{L peak} \right]$$

$$= \frac{1}{2} i_{L peak} \left[\frac{t_{on} + t_{off}}{T_s} \right]$$

$$= \frac{1}{2} i_{L peak}$$

$$i_{L peak} = \frac{1}{L} (V_d - V_o) t_{on}$$

$$i_L = \frac{1}{L} \int (V_d - V_o) dt$$

$$i_L = \frac{1}{L} (V_d - V_o) t + K \quad \left. \begin{array}{l} i_L(0) = 0 \\ K = 0 \end{array} \right\}$$

$$i_{L peak} = \frac{1}{L} (V_d - V_o) t_{on}$$

$$* I_{LB} = \frac{1}{2} \frac{1}{L} (v_d - v_o) t_{on}$$

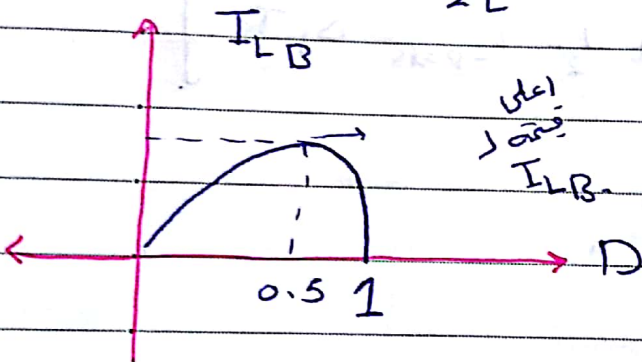
$$= \frac{t_{on}}{2L} (v_d - v_o)$$

$$D = \frac{t_{on}}{T_s} \Rightarrow t_{on} = D T_s$$

$$I_{LB} = \frac{D T_s}{2L} (v_d - v_o)$$

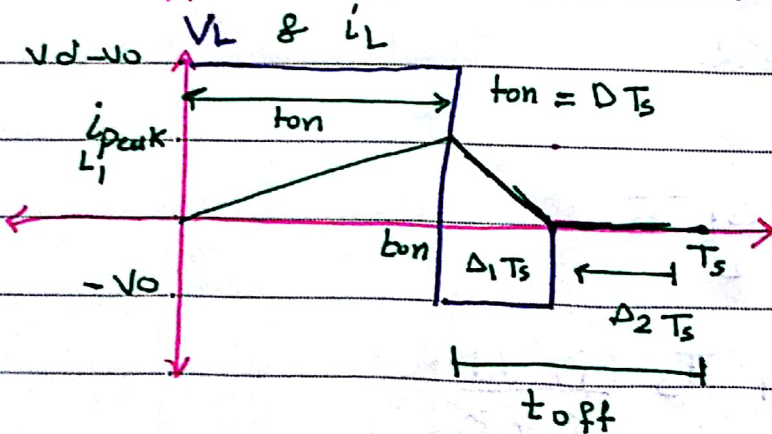
$$= \frac{D T_s}{2L} (v_d - D v_d)$$

$$= \frac{D T_s}{2L} v_d - \frac{D^2 T_s}{2L} v_d$$



$$I_{LB} \Big|_{D=0.5} = \frac{T_s v_d}{8L}$$

* Discontinuous conduction Mode.



$$V_L = 0 \Rightarrow A = B$$

$$(V_d - V_o) k_{on} = V_o \Delta_1 T_s$$

$$(V_d - V_o) D T_s = V_o \Delta_1 T_s$$

$$V_d D T_s - V_o D T_s = V_o \Delta_1 T_s$$

$$\frac{V_o}{V_d} = \frac{D}{D + \Delta_1} \rightarrow ?$$

$$I_L = \frac{1}{T_s} \left[\frac{1}{2} i_{L, \text{peak}} D T_s + \frac{1}{2} i_{L, \text{peak}} \Delta_1 T_s \right]$$

$$= i_{L, \text{peak}} \left(\frac{D + \Delta_1}{2} \right)$$

$$(V_d - V_o) D T_s = V_o D T_s$$

$$i_{L, \text{peak}} = \frac{V_o \Delta_1 T_s}{L}$$

$$I_L = \frac{(D + \Delta_1)}{2} i_{L, \text{peak}}$$

$$= \frac{(D + \Delta_1)}{2} \frac{V_o \Delta_1 T_s}{L}$$

$$= \frac{(D + \Delta_1)}{2} \frac{1}{L} \Delta_1 T_s \frac{D V_d}{D + \Delta_1}$$

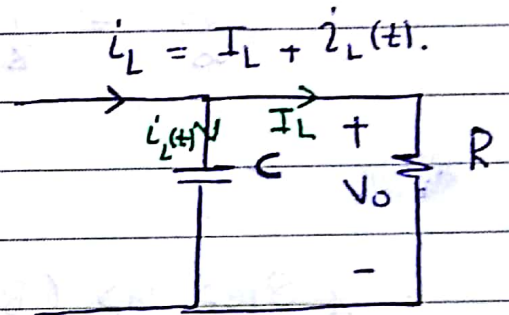
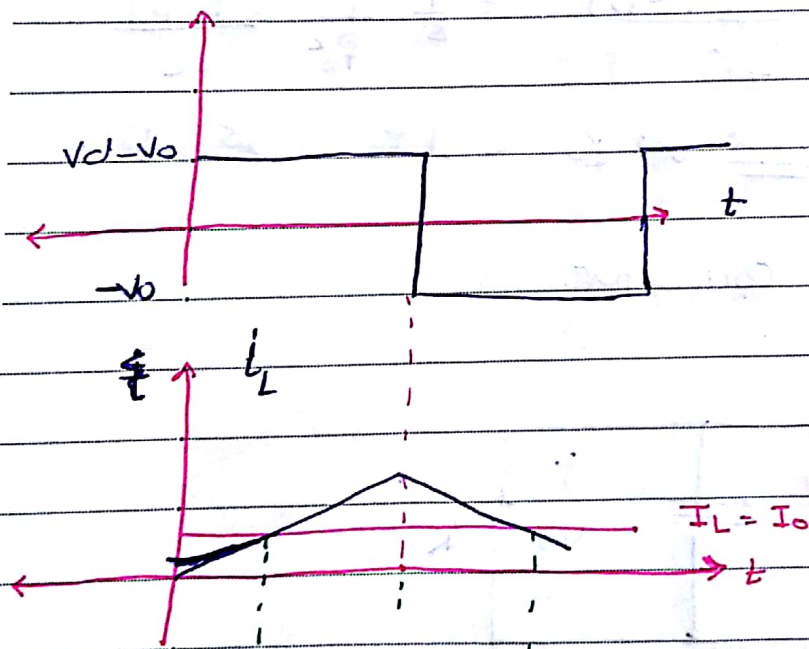
$$I_L = \frac{1}{2L} \Delta I T_s D v_d$$

$$\Delta I = \frac{2L I_L}{D T_s v_d}$$

$$\frac{V_o}{v_d} = \frac{D}{D + \frac{2L I_L}{D T_s v_d}}$$

given (I_L) (D T_s v_d) given

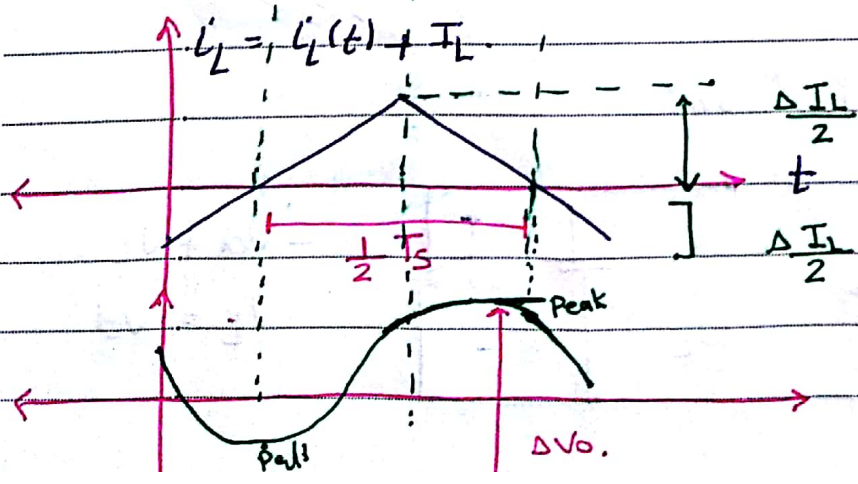
* output voltage Ripple :-



$$X_C = \frac{1}{\omega C} \rightarrow 0$$

$$i_C = C \frac{dv_C}{dt}$$

$$i_L(t) = C \frac{dv_o}{dt}$$



مسئله
الثاني

$$\Delta V_o = \frac{\Delta Q}{C} = \frac{1}{C} \cdot \frac{1}{2} \cdot \frac{1}{2} T_s \Delta I_L = \frac{1}{4C} T_s \frac{\Delta I_L}{2}$$

$$Q = \int i_L(t) dt = \frac{1}{8C} T_s \Delta I_L$$

$$\Delta I_L = \frac{V_o}{L} (1-D) T_s$$

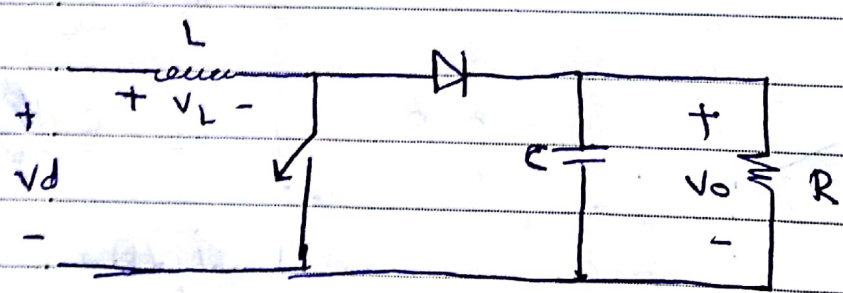
$$i_L = \frac{1}{L} \int v_L dt \dots$$

$$\Delta V_o = \frac{1}{8C} T_s \frac{V_o}{L} (1-D) T_s$$

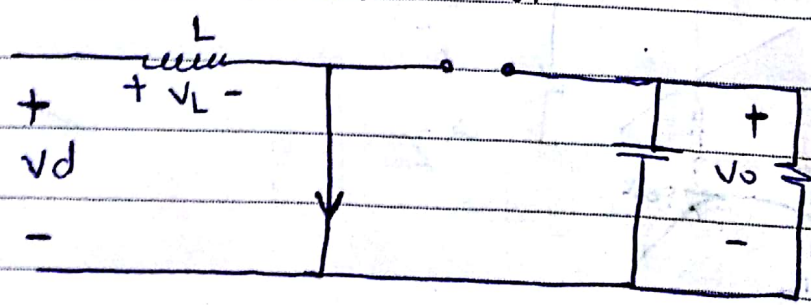
$$\frac{\Delta V_o}{V_o} = \frac{1}{8} \frac{T_s^2 (1-D)}{LC} = \frac{1}{8} \frac{1}{\frac{f_s^2}{LC} (1-D)}$$

ripple الج c, f_s و D

* Step up (Boost) converter.



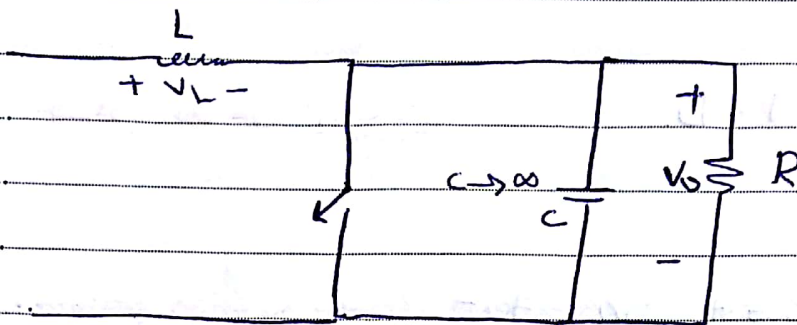
If the switch is "on"



$$-v_d + v_L = 0$$

$$v_L = v_d$$

* IF the switch is "OFF "

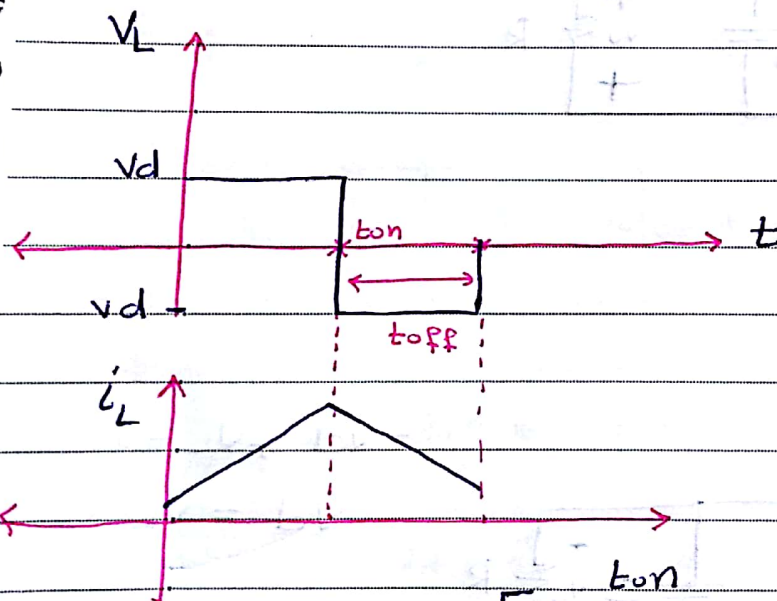


C → ∞

$$-V_d + V_L + V_o = 0$$

DC

$$V_L = V_d - V_o$$



$$V_L = 0 = \left[\int_0^{t_{on}} V_d dt + \int_{t_{on}}^{t_{off}} (V_d - V_o) dt \right]$$

~~XXXXXXXXXXXXXXXXXXXXXXXXXXXX~~

$$V_d t_{on} + V_d T_s - V_d t_{on} - V_o T_s + V_o t_{on} = 0$$

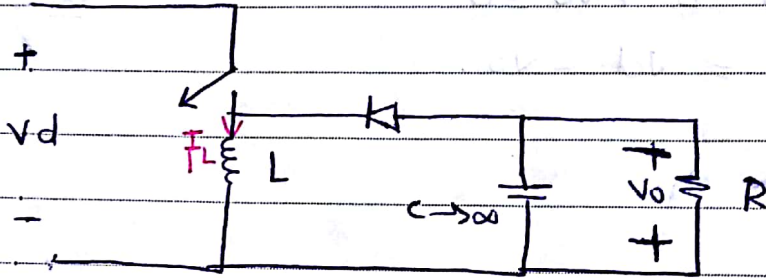
$$V_d T_s = V_o (T_s - t_{on})$$

$$\frac{V_o}{V_d} = \frac{T_s}{T_s - t_{on}} = \frac{T_s}{T_s - D T_s} = \frac{1}{1-D}$$

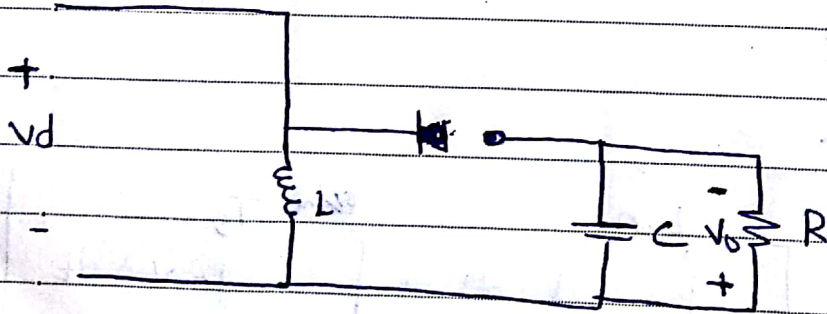
$$\frac{I_o}{I_d} = 1 - D$$

حظاوي مناسب CCCM

* Buck - Boost converter. (step up - step down)



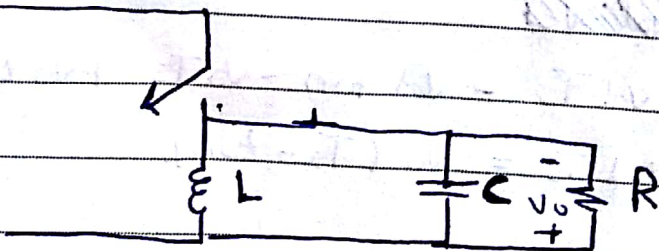
* "on" the switch.



$$-V_d + V_L = 0$$

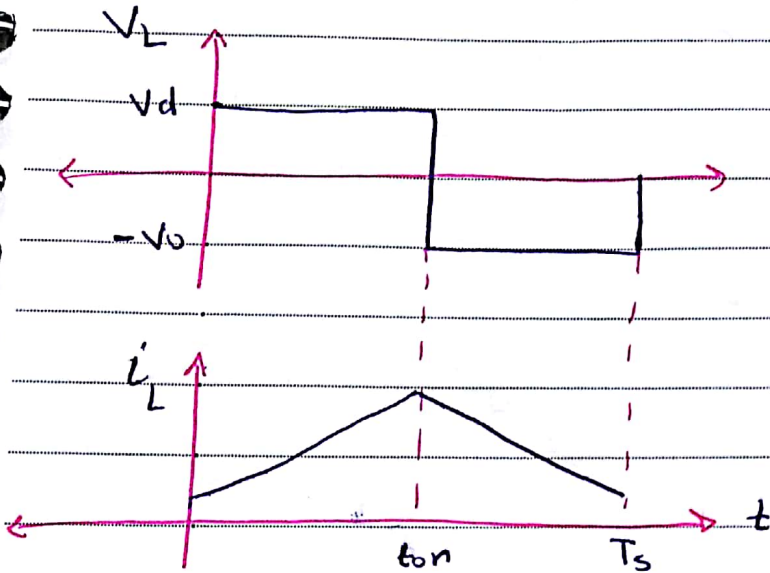
$$V_d = V_L$$

* "off" the switch



$$-V_L - V_O = 0$$

$$V_L = -V_O$$



$$V_L = 0 = \int_0^{t_{on}} V_d dt + \int_{t_{on}}^{T_s} -V_o dt.$$

$$V_d t_{on} = V_o (T_s - t_{on}) = 0$$

$$V_d t_{on} = V_o T_s - V_o t_{on}$$

$$\frac{V_o}{V_d} = \frac{t_{on}}{T_s - t_{on}} = \frac{D T_s}{T_s - D T_s} = \frac{D}{1-D}$$

Step down $0 \rightarrow 0.5$

Step up $0.5 \rightarrow 1$

$$\frac{I_o}{I_d} = \frac{1-D}{D}$$



* Full Bridge dc-dc converter 8-

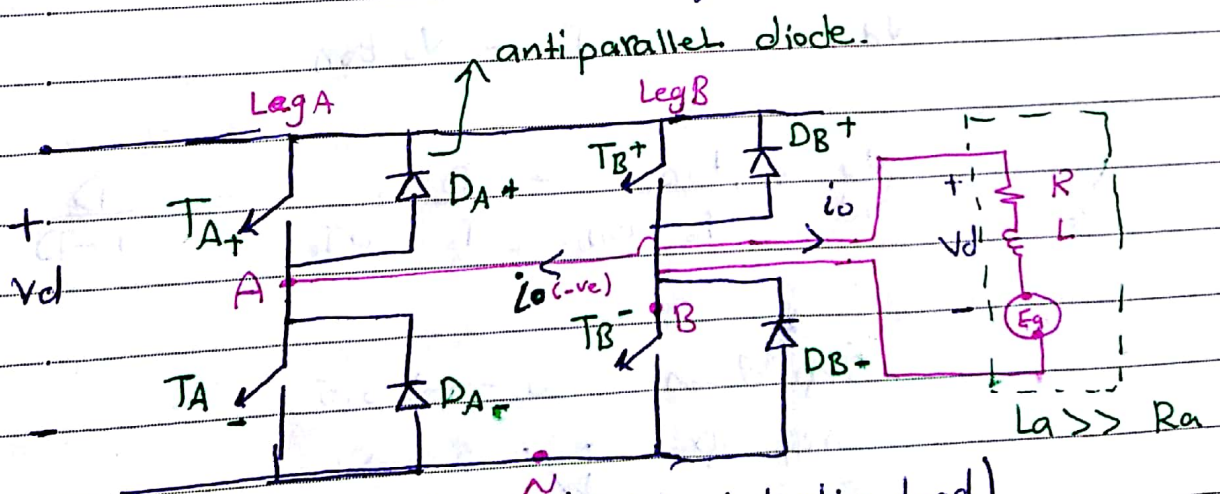
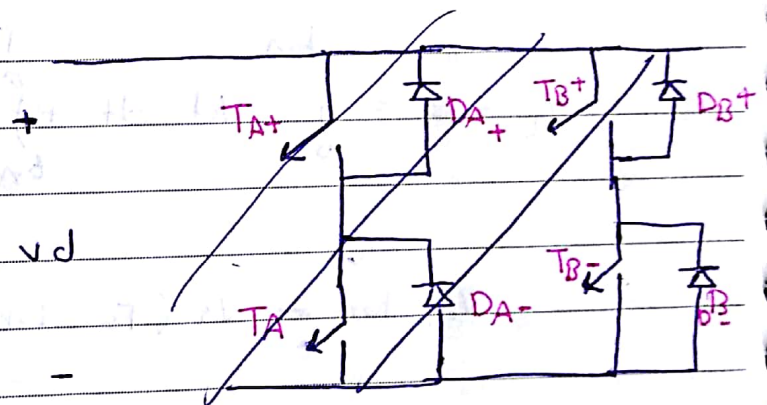
* Applications.

1- dc motor drives.

2- dc to ac conversion.

3- Renewable energy system.

4- Ups (uninterr)



Dc motor (Load) (highly inductive Load).

i_o :- +ve direction of the current.

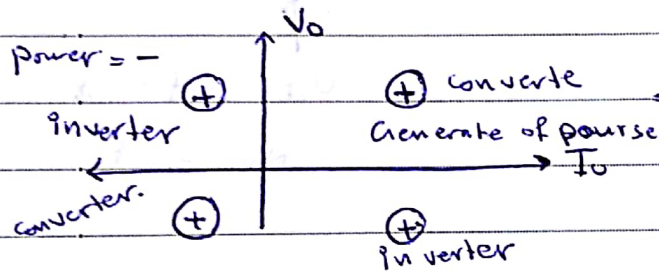
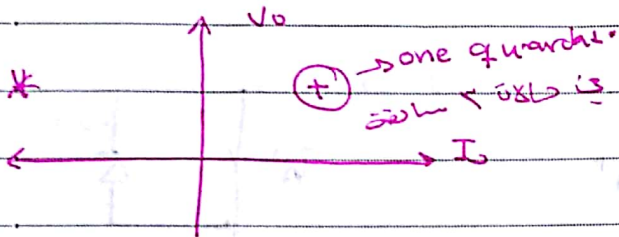
* Switch

i_o :- -ve direction of the current.

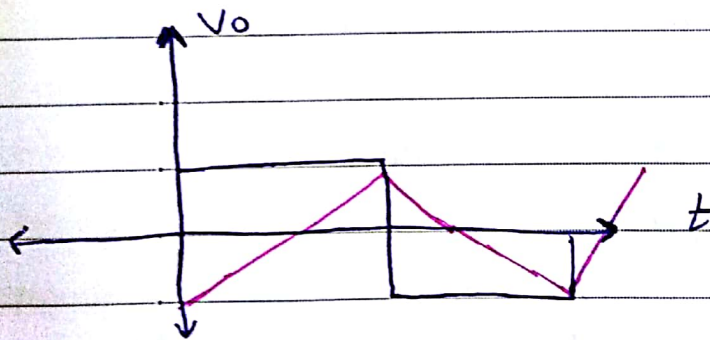
كل تفتح

يكون اسوي on.

Diode. -ve direction of the current. * Switch



بهاي الطاقة تغير اشارة
في ارباع



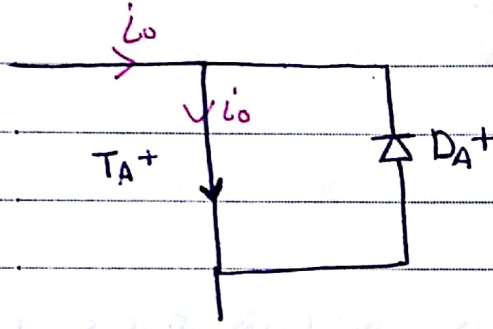
* on State of the Switch :-

the switch is on and may or may not conduct the current.

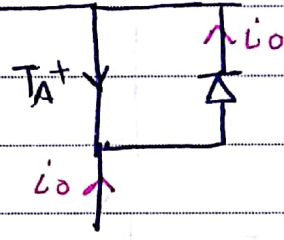
* conducting state of the Switch B-

The Switch on and the current flows through the Switch.

* cct. is same as of negative half cycle



conducting state.



on state of the Switch.

$$T_B^- \rightarrow \text{on} \Rightarrow V_{BN} = 0.$$

* All the case

$$V_o = V_{AN} - V_{BN}$$

$$1. T_B^+ \text{ on } \quad T_A^- \text{ on} \quad \begin{matrix} V_{AN} = 0 \\ V_{BN} = V_d \end{matrix} \quad V_o = -V_{BN}$$

$$2. T_B^+ \text{ on } \quad T_A^+ \quad \begin{matrix} V_{AN} = V_d \\ V_{BN} = V_d \end{matrix} \quad V_o = 0.$$

1- when T_A^+ is on, i_o flows through T_A^+ if i_o is +ve

2- when T_A^+ is on, i_o flows through D_A^+ if i_o is -ve.

3- In both case, T_A^+ is on $V_{AN} = V_d$.

(T_A^+ is on & T_A^- is off).

* when T_A^- is on, i_o flows through T_A^- if i_o is -ve.

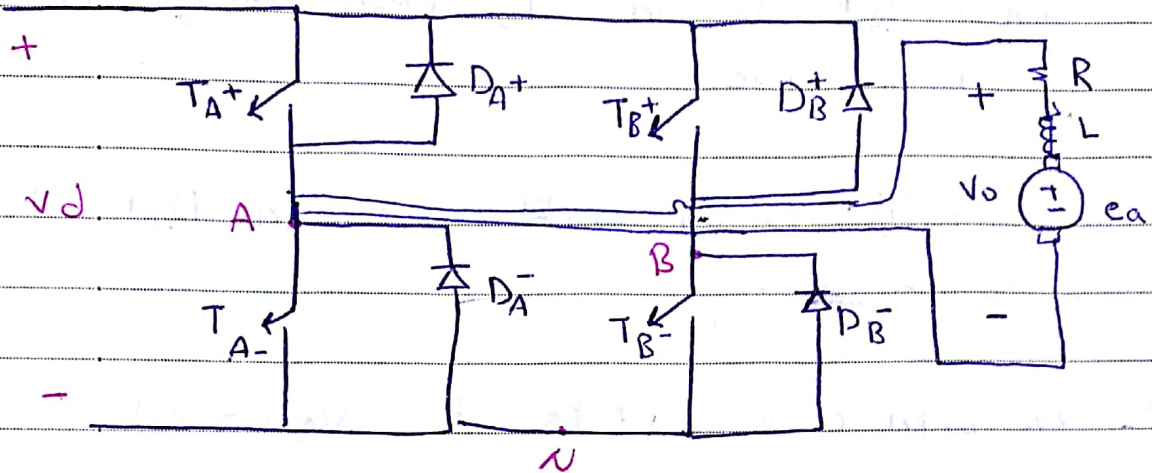
* when T_A^- is on, i_o flows through D_A^- if i_o is +ve.

In both case, T_A^- is on, $V_{AN} = 0$.

* on saw T_A^+ , T_A^- is zero

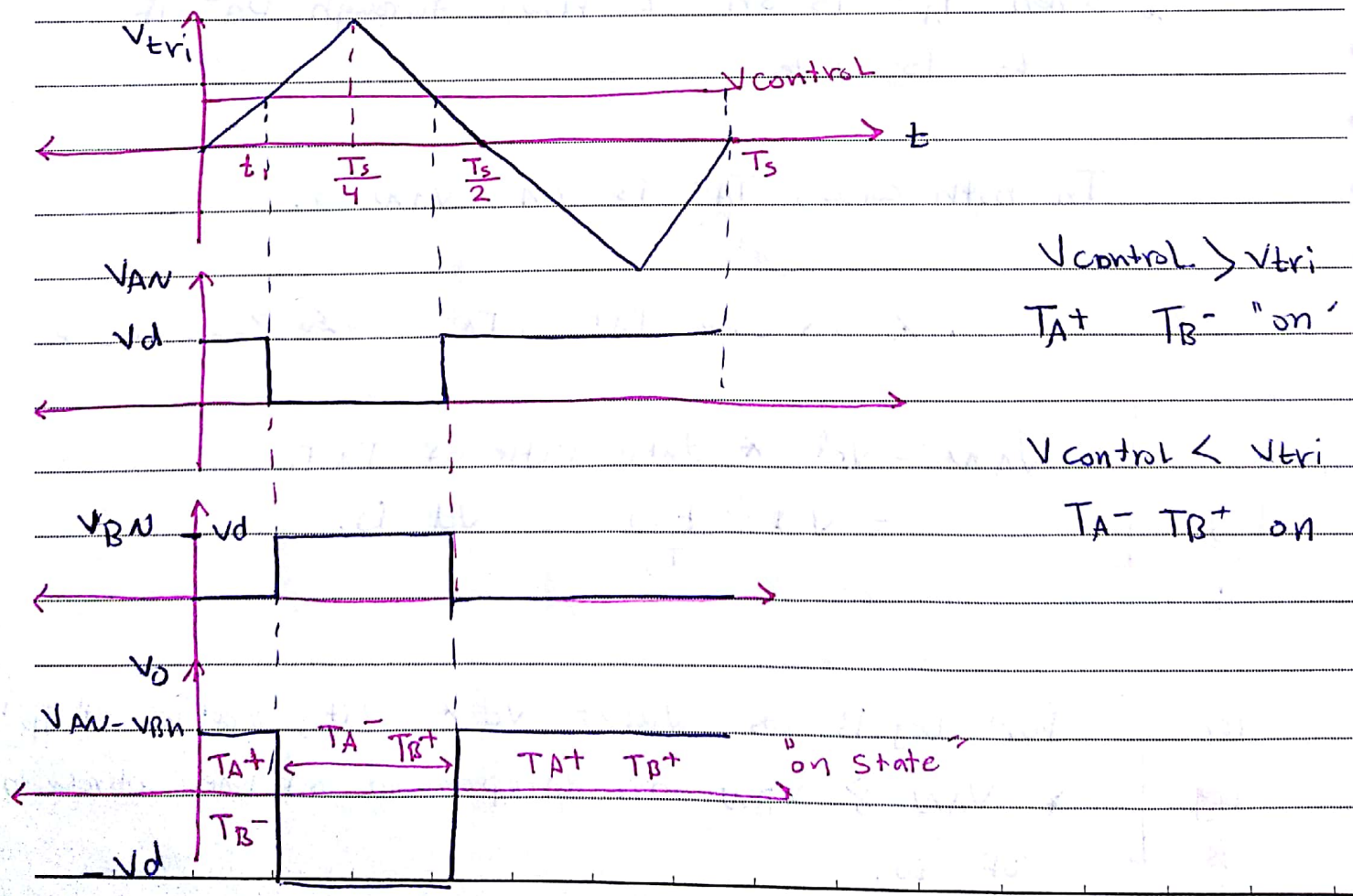
For Leg A $\left[\begin{array}{l} * V_{AN} = V_d * \text{duty ratio of } T_A^+ \\ = V_d \frac{t_{on}}{T_s} = V_d D. \end{array} \right.$

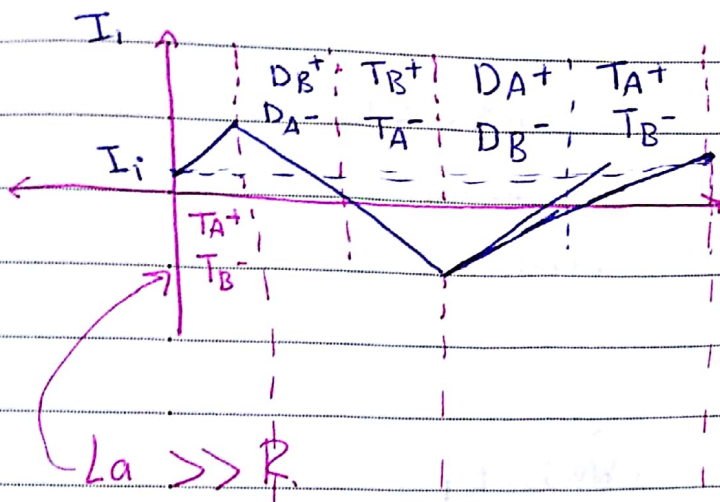
For Leg B $\left[\begin{array}{l} \text{For Leg B } \Rightarrow V_{BN} = V_d * \text{duty ratio of } T_B^+ \\ * V_{AN} \text{ \& } V_{BN} \text{ are independent of the direction of } i_o. \end{array} \right.$



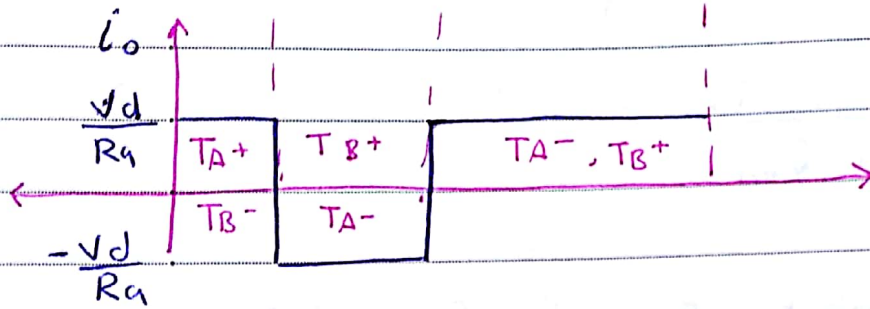
① PWM with bipolar voltage switch

(T_{A+}, T_{B-}) & (T_{B+}, T_{A-}) are turned on and off simulta (inverter).

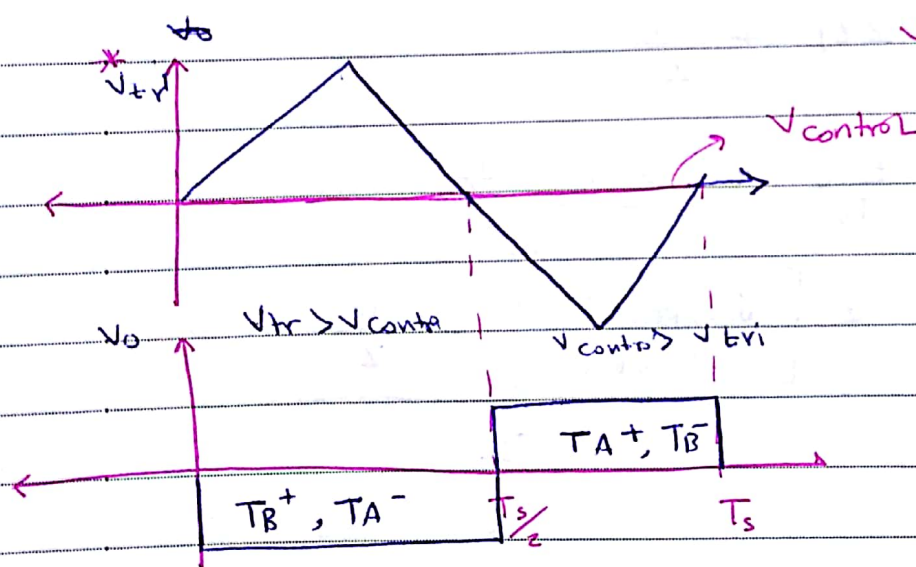




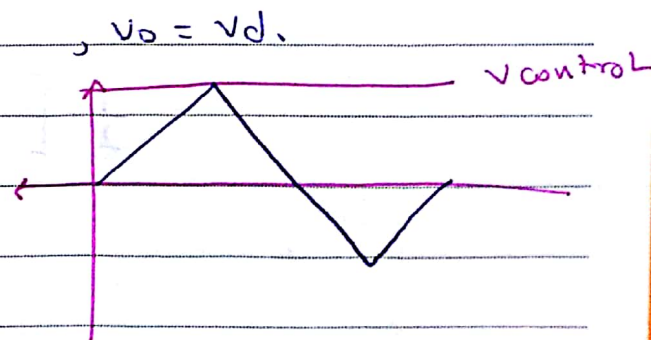
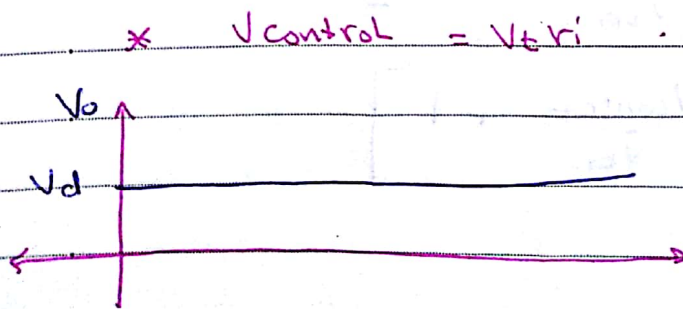
"Conductive state"



(pure R)



$v_{control} = \text{Zero}$



$$* v_{tri} = \frac{\hat{v}_{tri}}{\frac{T_s}{4}} t, \quad 0 < t < t_1$$

Triangle

$$= \frac{4 \hat{v}_{tri}}{T_s} t$$

tan

when $t = t_1$

$$v_{control} = v_{tri} = \frac{4 \hat{v}_{tri}}{T_s} t_1$$

$$t_1 = \frac{v_{control} T_s}{4 \hat{v}_{tri}}$$

The one duration t_{on} of T_A^+ T_B^- is:-

$$t_{on} = 2 t_1 + \frac{T_s}{2}$$

$$D_1 = \frac{t_{on}}{T_s} = \frac{2 t_1 + \frac{T_s}{2}}{T_s}$$

$$D_1 = \frac{2 \left[\frac{v_{control} T_s}{4 \hat{v}_{tri}} \right] + \frac{T_s}{2}}{T_s}$$

$$D_1 = \frac{1}{2} \frac{v_{control}}{\hat{v}_{tri}} + \frac{1}{2}$$

$$= \frac{1}{2} \left[\frac{v_{control}}{\hat{v}_{tri}} + 1 \right]$$

* The on duration of T_{B^+} , T_{A^-} is.

$$D_2 = 1 - D_1$$

$$V_o = V_{AN} - V_{BN}$$

$$= D_1 v_d - D_2 v_d$$

$$= D_1 v_d - (1 - D_1) v_d$$

$$= D_1 v_d - 1 + D_1 v_d$$

$$V_o = (2D_1 - 1) v_d$$

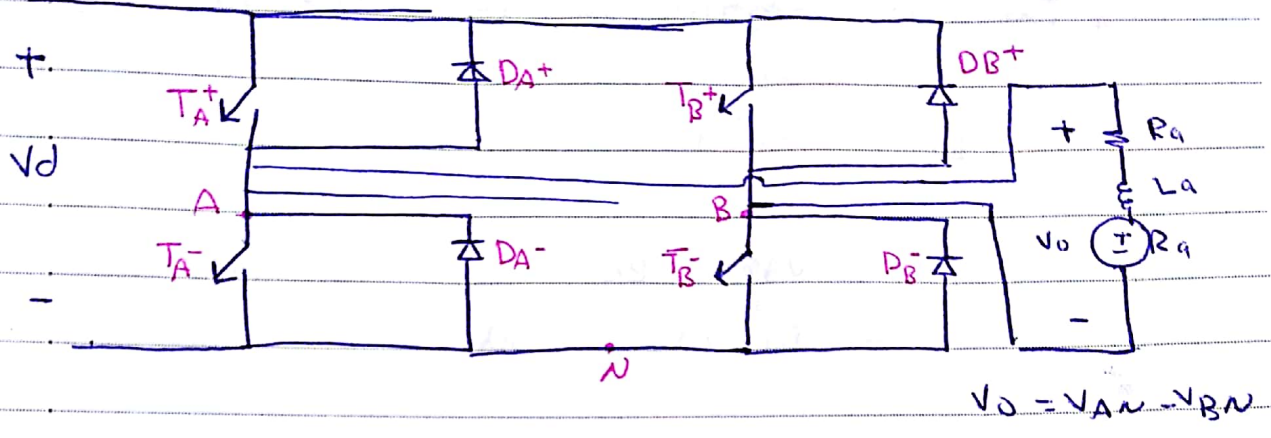
$$V_o = \frac{V_{control}}{\hat{v}_{tri}} v_d$$

$$V_o = K v_d$$

, $V_{control} = 0$, $avg V_o = zero$.

*

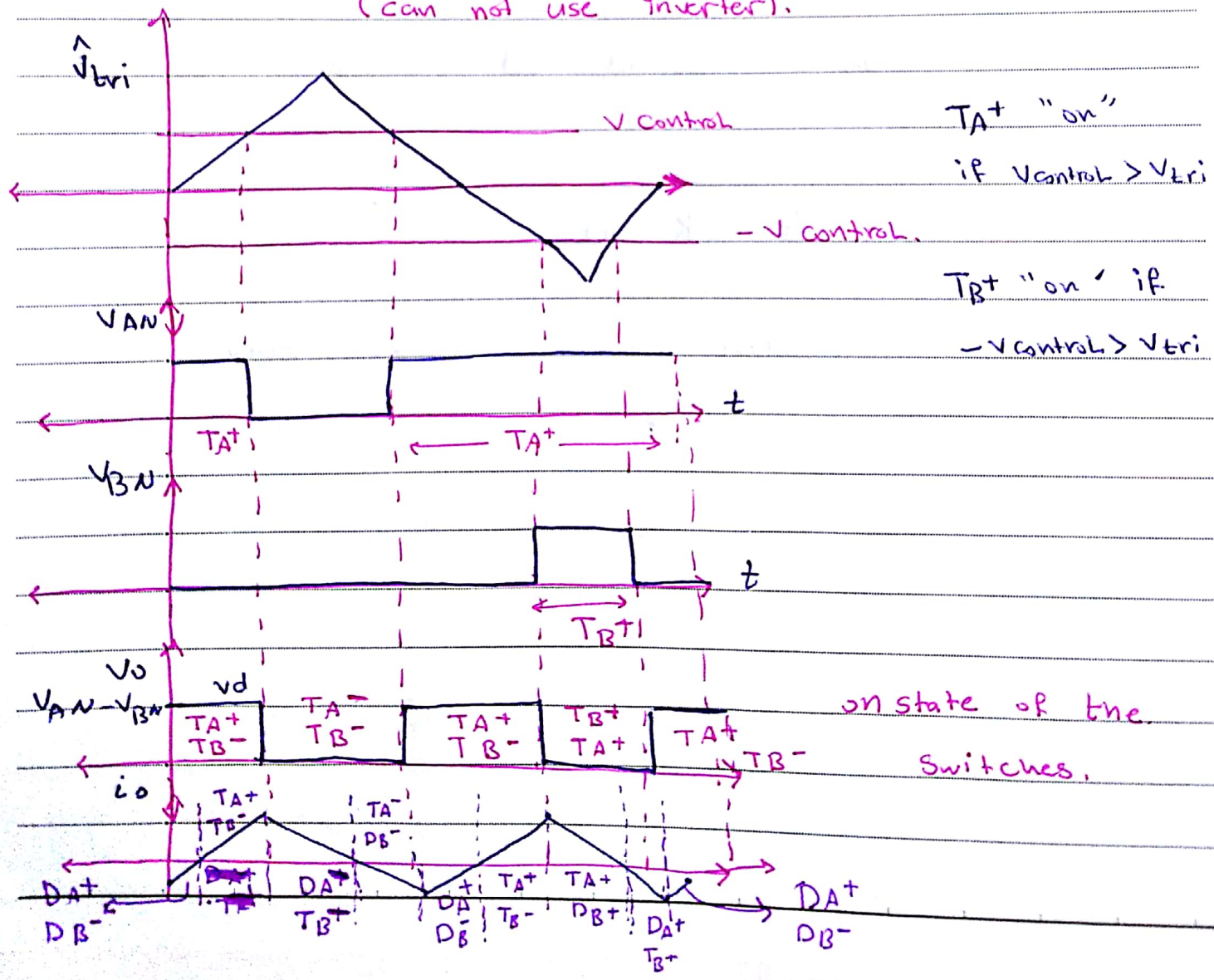
Ux x



* PWM with unipolar voltage switching. 8-

The switches in each unipolar leg are controlled independently of the other leg.

(can not use inverter).



TA+ "on" if $V_{control} > V_{tri}$
 TB+ "on" if $-V_{control} > V_{tri}$

on state of the switches.

~~transmission~~

$$V_o = \frac{V_{control}}{\hat{V}_{tri}} v_d$$

\hat{V}_{tri}

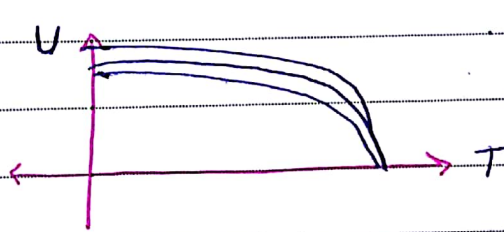
on T_{A+} T_{P+} at T_{A+} T_{P+} T_{A+} T_{P+}

switches T_{A+} T_{P+} T_{A+} T_{P+}

steady state cycle T_{A+} T_{P+}

transim. cycle T_{A+} T_{P+}

prod CH 7 : 1, 2, [(19, 18, 1) 22]

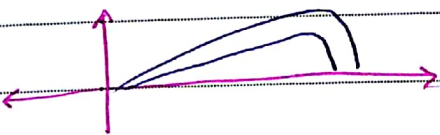


\bar{P}_{avg}

Load \bar{I}

using Dc - Dc converter. to set (constant voltage).

on PV-generator.



CH7 * Switch mode dc → ac Inverters.

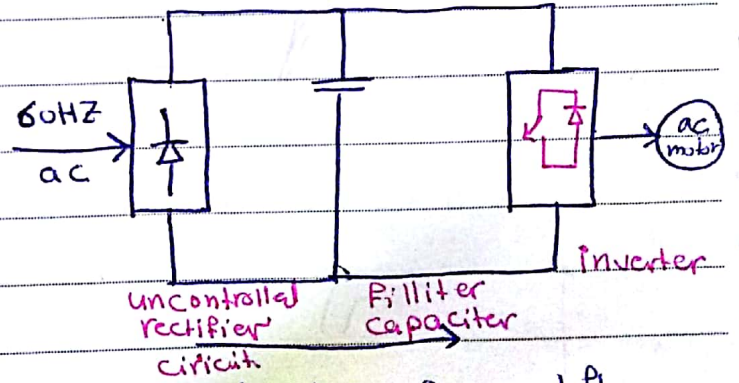
dc → Sinusoidal ac.

* Application :-

- 1 - ac motor drives.
- 2 - UPS
- 3 - PV system.
- 4 - wind energy systems.

Renewable energy system.

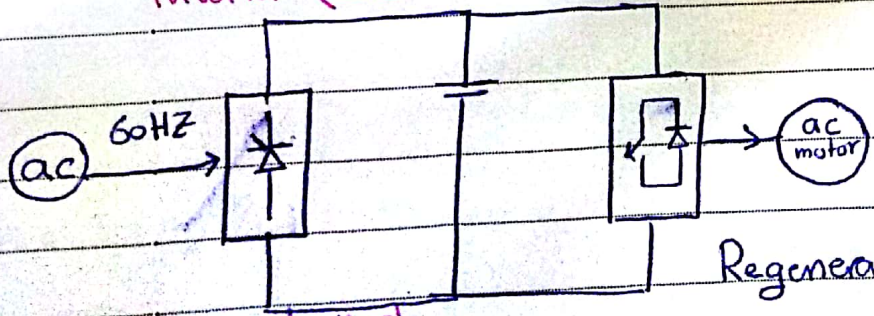
* Objective :- To produce a sinusoidal ac output voltage (current) with controlled frequency and magnitude.



direction of power flow.

(Switch-mode inverter in ac motor drive system)

inverter ← → rectifier

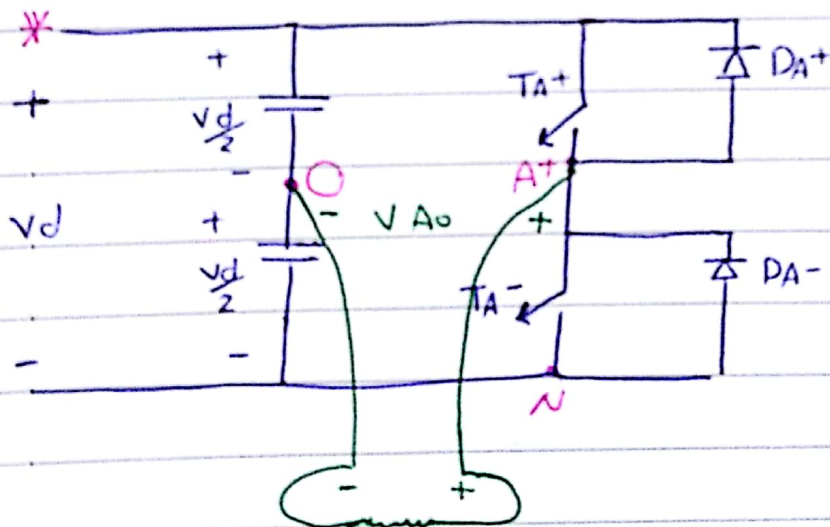
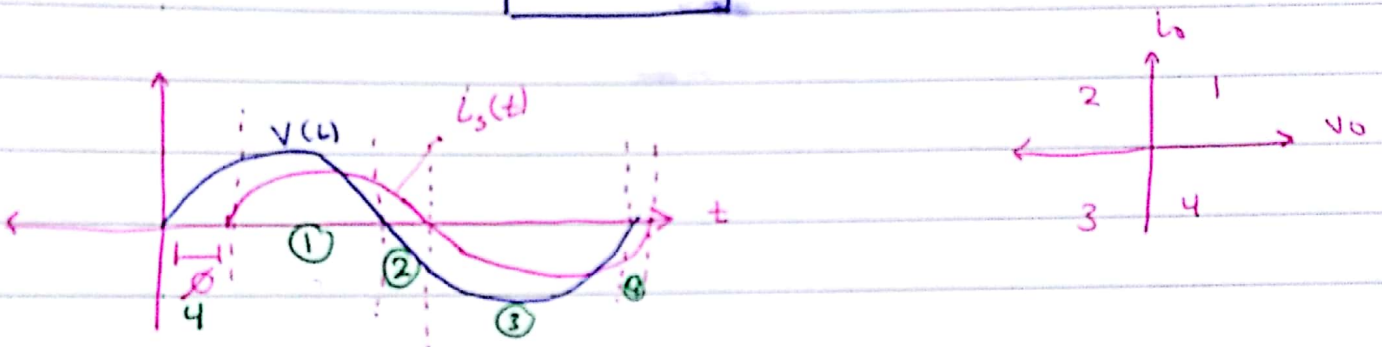
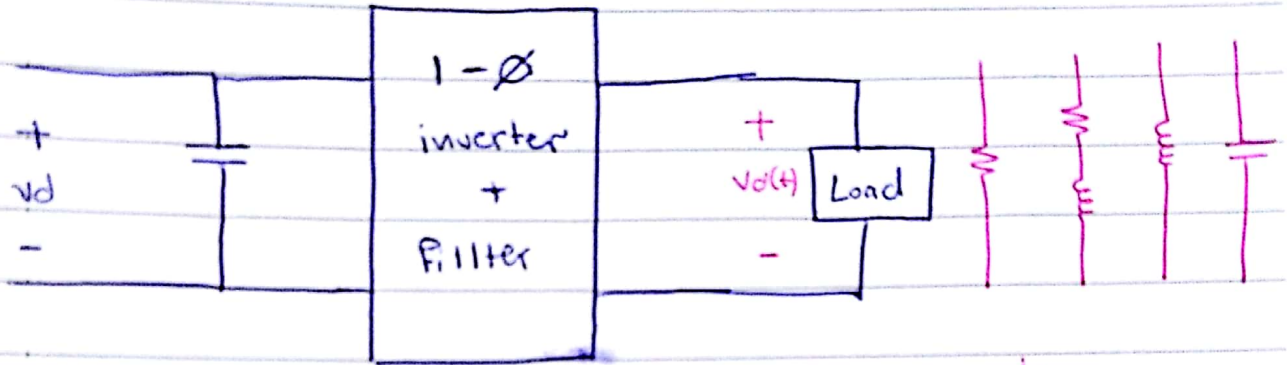


Regenerative braking principle.

controlled rectifier circuit.

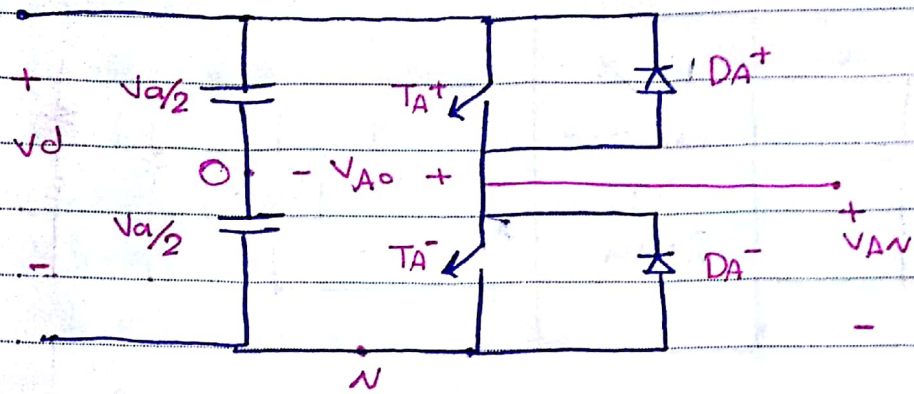
4 1 5 23

* Basic concept of switch-mode Inverter.

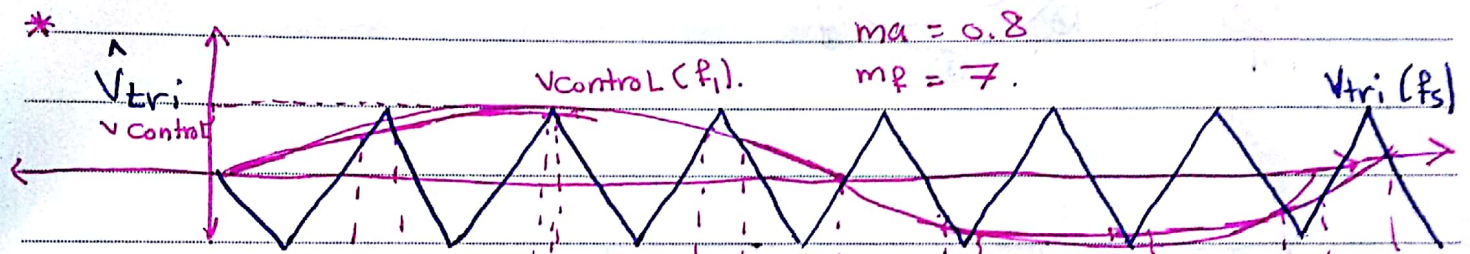


one-leg switch mode inverter.

* on leg inverter. (single phase)

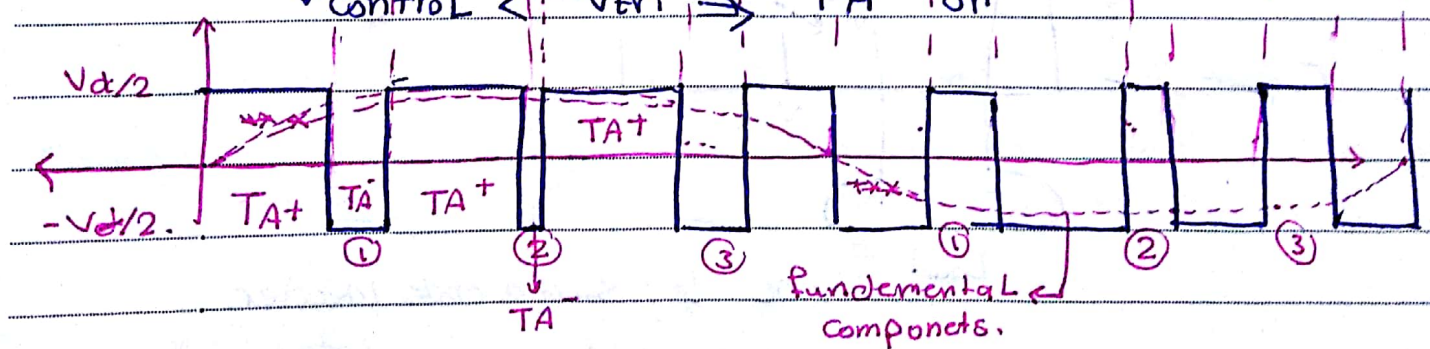


* Pulse width Modulate Switching Schem:-

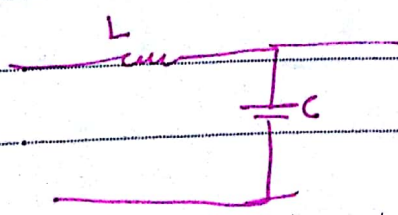


$V_{control} > V_{tri} \Rightarrow TA^+$ "on"

$V_{control} < V_{tri} \Rightarrow TA^-$ "on"



(Filter) LPF سے pure sin wave



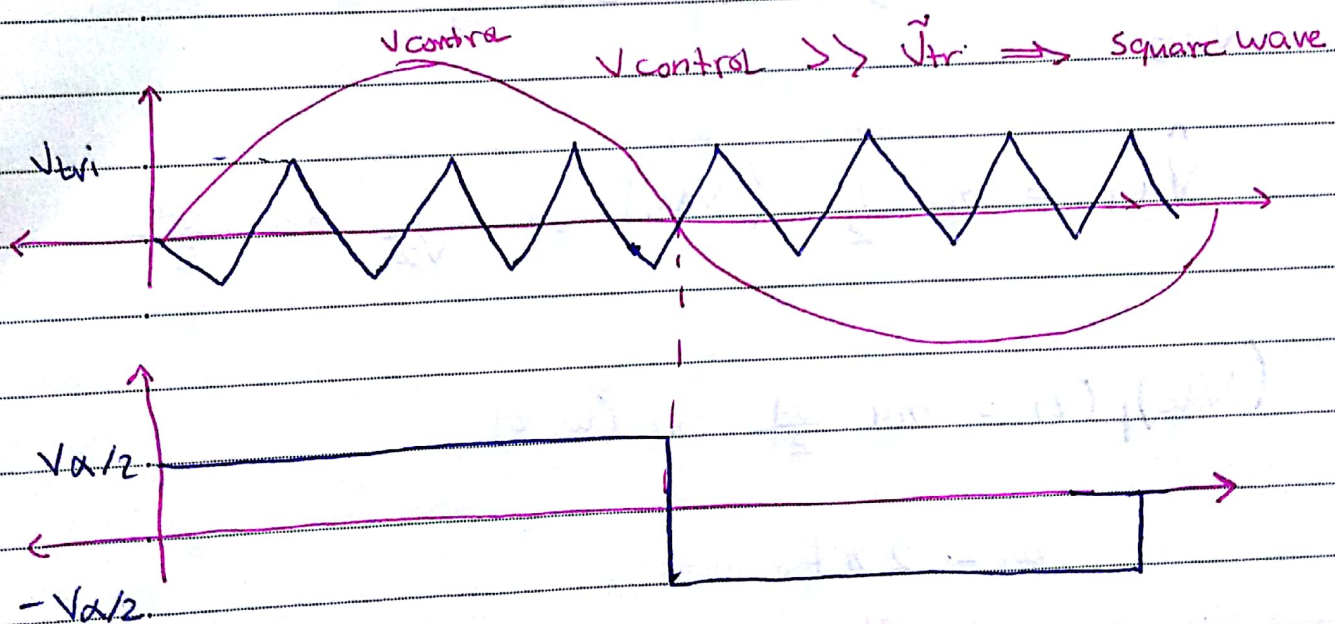
Low Freq sine wave
L, C comp. of

* f_s :- the frequency of which the inverter switches are switched (carrier frequency) \Rightarrow Switching frequency

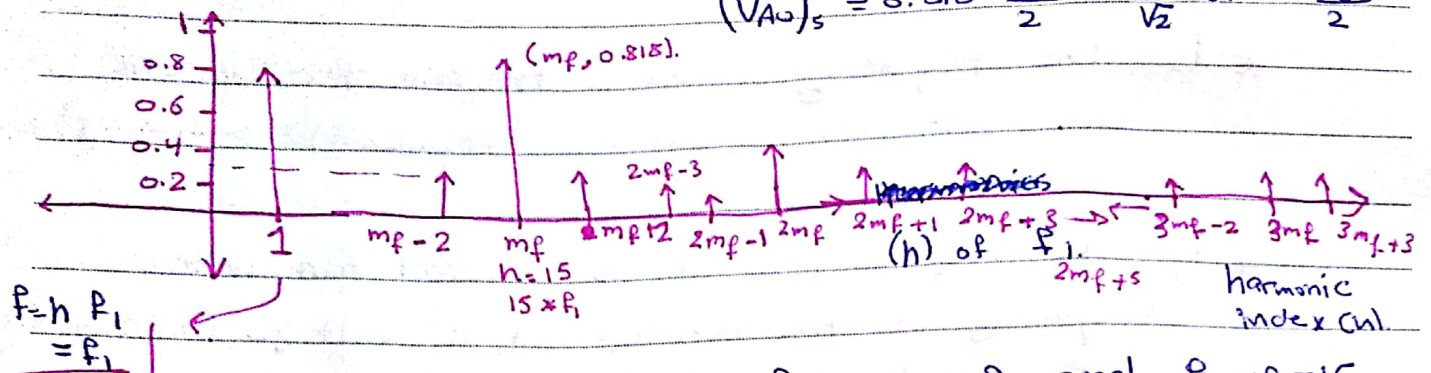
* f_1 the frequency which is desired fundamental frequency of the inverter output voltage (modulating frequency).

$$m_a = \frac{\hat{V}_{control}}{\hat{V}_{tri}} \Rightarrow \text{amplitude modulation index (ratio)}$$

$$m_f = \frac{f_s}{f_1} \Rightarrow \text{frequency modulation index (ratio)}$$



$$\hat{(V_{Ao})}_s = 0.818 \frac{V_d}{2} = \frac{1}{\sqrt{2}} 0.818 \frac{V_d}{2}$$



Fundamental Frequency.

Harmonic spectrum of A_{vo} for $m_a = 0.8$ and $\beta_{mp} = 15$.
For one-leg switch mode DC-AC inverter.

* Note one leg DC-AC inverter :-

At $f_1 \Rightarrow 50 \text{ Hz}, 60 \text{ Hz}, 100 \text{ Hz}, 25 \text{ Hz}.$

$$\frac{\hat{V}_{Ao1}}{V_d/2} = 0.8 \Rightarrow \hat{V}_{Ao1} = 0.8 \frac{V_d}{2}$$

$$\hat{V}_{Ao1} = m_a \frac{V_d}{2} \quad (V_{Ao1})_{\text{rms}} = \frac{1}{\sqrt{2}} m_a \frac{V_d}{2}$$

$$(V_{Ao})_1(t) = m_a \frac{V_d}{2} \sin(\omega_1 t)$$

$$\omega_1 = 2\pi f_1$$

لقد نرى ان m_p لا يتجاوز 15 فالتالي Design for filter
(LPF \Rightarrow (L, C) series). كسرة

* $m_a < 1 \Rightarrow$

* The harmonics in the inverter output voltage wave form are side band centered around the switching frequency and its multiples ($mp, 2mp, 3mp$)

2- the number of harmonic is infinite.

3- the amplitude of the harmonics are independent of m_f .

3- their frequencies is correlated \Rightarrow ~~related~~

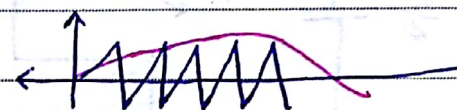
$$f_h = (j m_f \pm k) f_1 = h f_1$$

j odd \Rightarrow k even

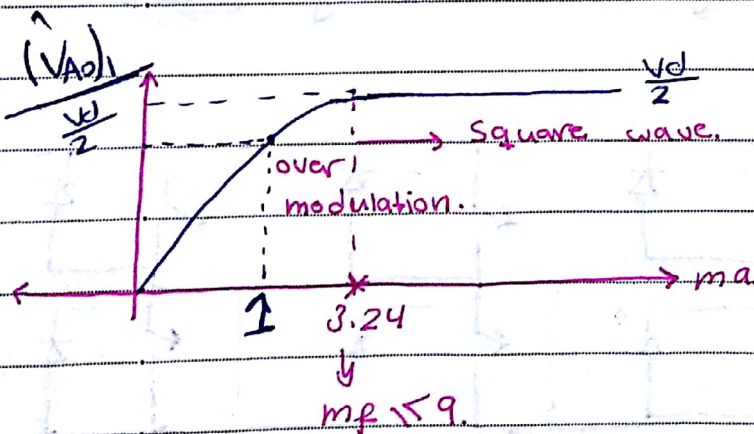
j even \Rightarrow k odd

is.

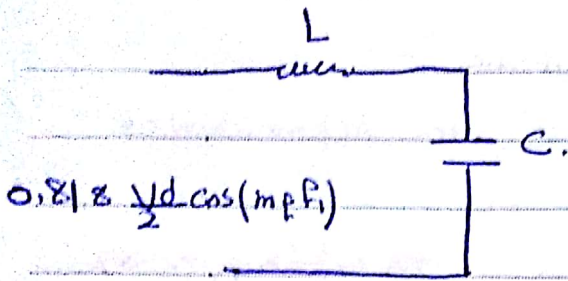
4- For odd value of j the value of k is even
for even " " " " " " " " odd.

* for $m_a > 1 \Rightarrow$ 

1. $m_a \gg 1 \Rightarrow$ \cdot ~~two parts~~



* The square wave out voltage is obtain condition if m_a much greater one ($m_a \gg 1$). the general condition if the control signal does not intersect with \hat{u}_{tri} .

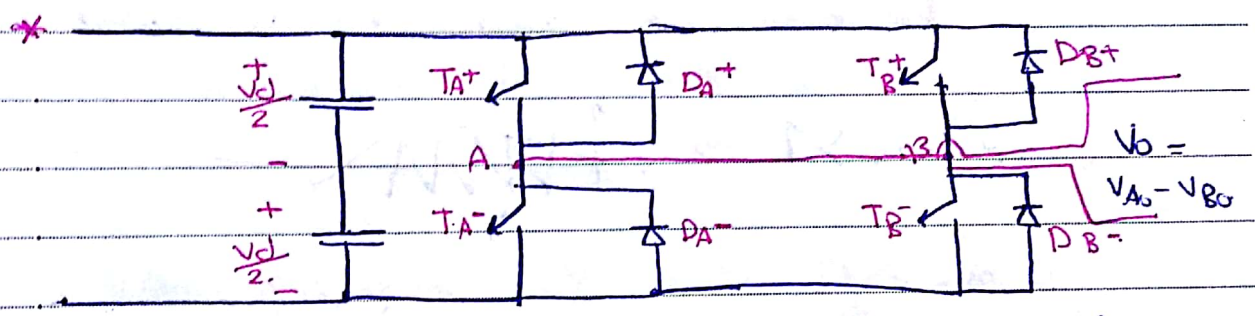


* Design Lpf :-

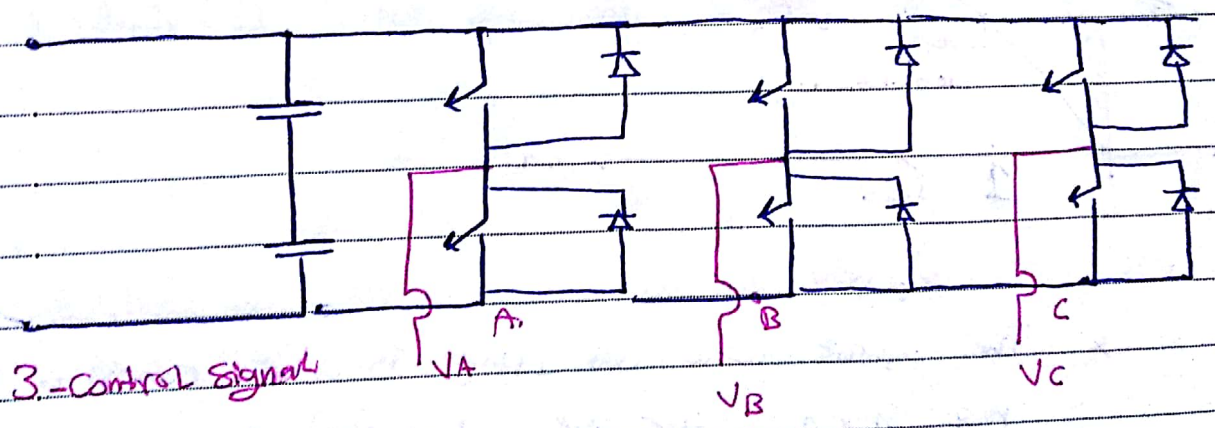
$$0.818 \frac{V_d}{2} \cos(1 F_s) = 15 * 50 = 750$$

$$\omega L = (2\pi) (750) L = \dots \Omega$$

$$\frac{1}{\omega C} = \frac{1}{2\pi (750) C}$$



2 - Control Signal Full - Bridge Inverter (Single-phase)



3 - Control Signal

3-Ø Full Bridge Inverter.

