



تقدم لجنة EiCoM الاكاديمية

تلخيص لمادة:

مختبر تحكم آلي



$$T(s) = \frac{s^2 + 3s + 2}{s^2 + 2s + 4}$$

transfer fn.
relation bet. output and input
with initial value = 0

$P = 5;$

المطلوب
Result
Command
window
ولكن نضيف

$$n = [1 \ 3 \ 2];$$

$$d = [1 \ 2 \ 4];$$

① $r = \text{roots}(n)$ → roots

$r = \text{roots}(d)$

roots
Complex

second order
under damped

② roots in left → Stable

①

CLS → clear command window

clear delete data

②

$$\text{Poly}([-1 \ -2])$$

roots

النتيجة
النتيجة

$$(x+1)(x+2)$$

$$x^2 + 2x + x + 2$$

$$x^2 + 3x + 2$$

$$[1 \ 3 \ 2]$$

③

polyval(n, # or [])

Ex polyval(n, 1) = n(1)

⇒ help polyval

result of Pol x Pol

$$n \cdot d \quad X$$

$$n * d \quad X$$

$$n \cdot * d \quad [1 \ 6 \ 8]$$

element

① by element

④

$$t = \text{conv}(n, d)$$

$$t = 1 \ 5 \ 12 \ 16 \ 8$$

$$s^4 + 5s^3 + 12s^2 + 16s + 8$$

2

$$T = tf(n, d)$$

transfer function

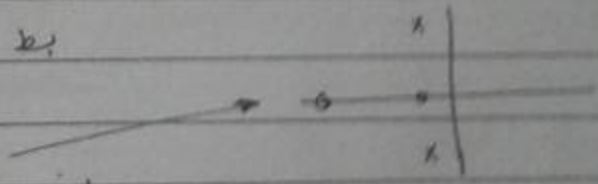
$$f = tf([1 \ 0 \ 1], [1 \ 0 \ 2 \ 1])$$

$$f = \frac{s^2 + 1}{s^3 + 2s + 1}$$

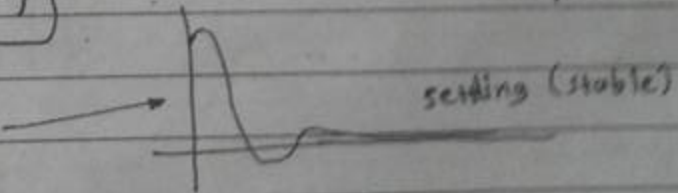
Pole (T) \rightarrow p_1

zero (T) \rightarrow z_1

Pz map (T)



step (T)



damp(T) \rightarrow damping ratio nature frequency

stepinfo (T) Rise time

$$T(s) = \frac{s^2 + 3s + 2}{s^3 + 2s + 4}$$

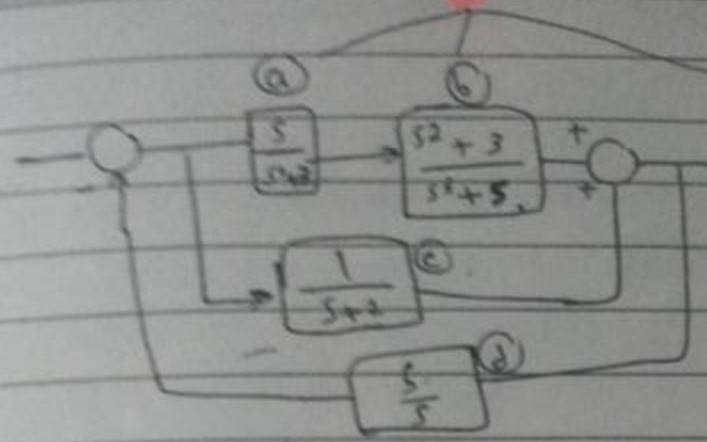
dc gain (T) \rightarrow $\frac{0.5 \text{ out}}{1 \text{ input}} = 0.5$

at time ∞ (steady state) $s=0$

substitute $s=0$ in numerator & denominator

step(5sT) $\frac{2.5 \text{ out}}{5 \text{ input}} = 0.5$

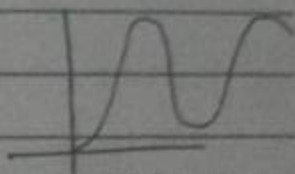
gain input (rise) $\frac{2.5}{5}$ output



fifth order behave
but behave as second

$$\frac{s}{s^2+3} \times \frac{s^2+3}{s^2+5}$$

$$\frac{1}{s^2+5}$$



critically

Parallel damped
locality system
feedback

$$a = tf([1, 0], [1, 0, 3]);$$

$$b = \vdots$$

$$e = series(a, b);$$

$$f = parallel(e, c);$$

$$F = feedback(f, d)$$

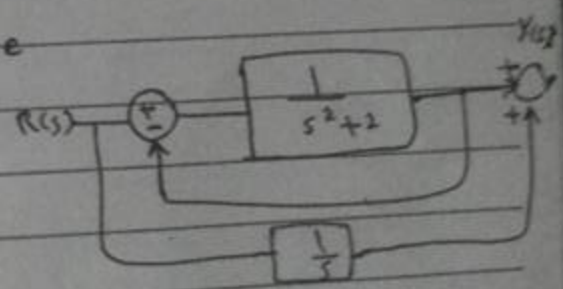
feedback (f, d, -) negative feedback

feedback (f, d, +) +ve

feedback (f, d, 1)

(1) $\frac{1}{s^2+5}$ unstable 0.5

negative \rightarrow Stable
+ve \rightarrow unstable



$$w = minreal(e)$$

زیر کلاسیک

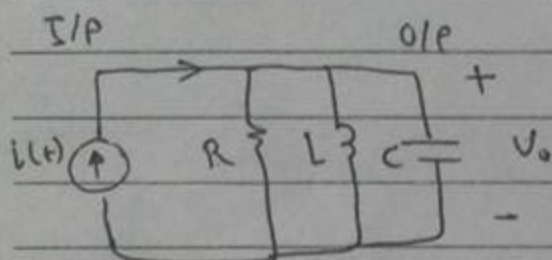
Modeling

1. electrical KVL $\rightarrow \sum \Delta v = \text{zero}$ conservation of energy

KCL $\rightarrow \sum i_{\text{node}} = \text{zero}$ ν of mass

2. mechanical system \rightarrow Newton's 2nd

$$\sum F = ma$$



$$i(t) = i_R + i_L + i_C$$

$$= \frac{v_o}{R} + \frac{1}{L} \int v_o + C \frac{dv_o}{dt}$$

$$\dot{i}(t) = \frac{v_o'}{R} + \frac{1}{L} v_o + C \dot{v}_o'$$

higher

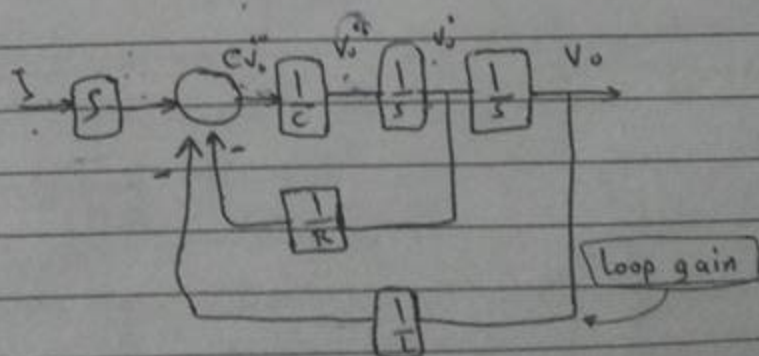
$$C \dot{v}_o' = \dot{i} - \frac{1}{R} v_o - \frac{1}{L} v_o$$

$$C s^2 V = s I - \frac{1}{R} s V - \frac{1}{L} V$$

TF

it must single input and single output

SISO



Simulink

input from [source] (E) step

continout du/dt

math operation (t)

$$\frac{V}{I} = \frac{S}{S^2 + \frac{1}{RC}S + \frac{1}{LC}}$$

Simout → output on matlab workspace

L = 10mH
R = 1KΩ
C = 4μF

save format Array

← i step input

double click

Plot (tout, vout)

mux



رسم آنگونه
مشکل کار نیست
الویه

① Accuracy

$$e = \text{input} - \text{output}$$

② Disturbance rejection

$$DR = \frac{V_{oi}}{V_{od}}$$

$$V_o = V_{oi} + V_{od}$$

$$③ S_G^T = \frac{\Delta T}{\Delta G} \frac{G}{T} = \frac{\Delta T/T}{\Delta G/G}$$

$$S_G^T = \frac{\delta T}{\delta G} \frac{G}{T}$$

sensitivity for the system
when S is open

Home work
 G_1, G_2

open

$$V_{oi} = G_1 G_2 V_{in}$$

$$V_{od} = G_2 V_d$$

$$V_o = G_1 G_2 V_{in} + G_2 V_d$$

closed

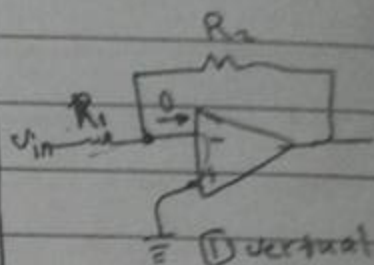
$$V_{oi} = \frac{G_1 G_2}{1 + G_1 G_2} V_{in}$$

$$V_{od} = \frac{G_2}{1 + G_1 G_2} V_d$$

$$DR = \frac{\text{open } G_1 V_{in}}{V_d} \quad DR = \frac{\text{closed } G_1 V_{in}}{V_d}$$

①

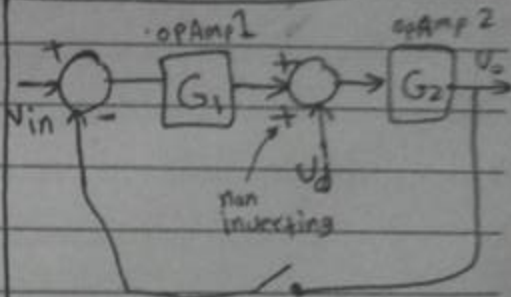
=



① virtual short
 $V_{non} = V_{inver}$

② Input = Zero

③ KCL at each node



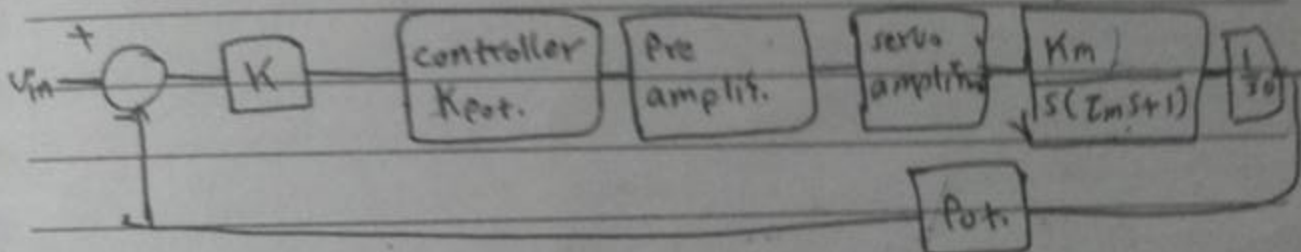
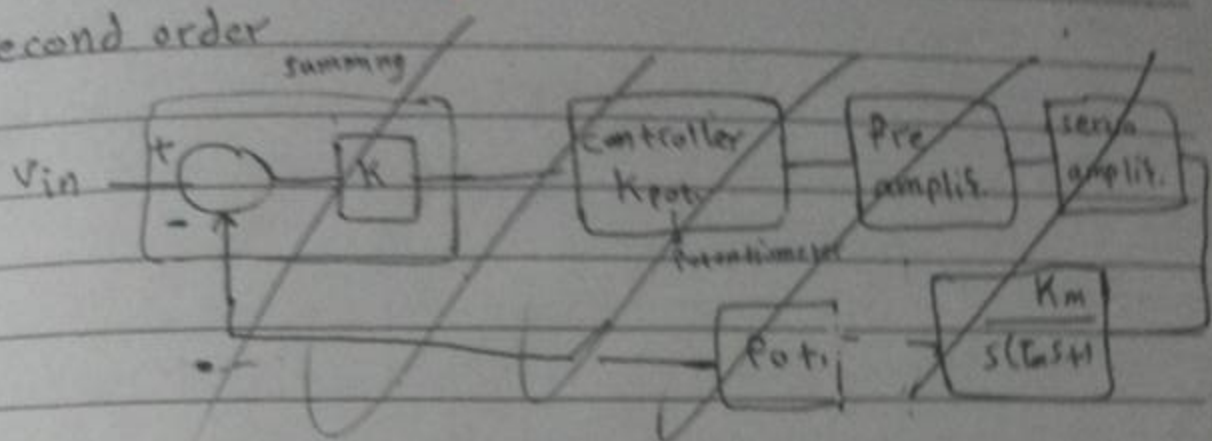
super position
assume $V_d = 0$

$$V_{oi} = \frac{G_1}{1 + G_1} V_{in} \quad ①$$

assume $V_i = \text{zero}$

$$V_{od} = \frac{G_2}{1 + G_2} V_d \quad ②$$

second order



$$\frac{R_1 \parallel R_2}{R_1 + R_2}$$

1) Inverted Pendulum



2) Magnetic Levitation



$$T(s) = \frac{y}{I} = \frac{-a}{s^2 - b}$$

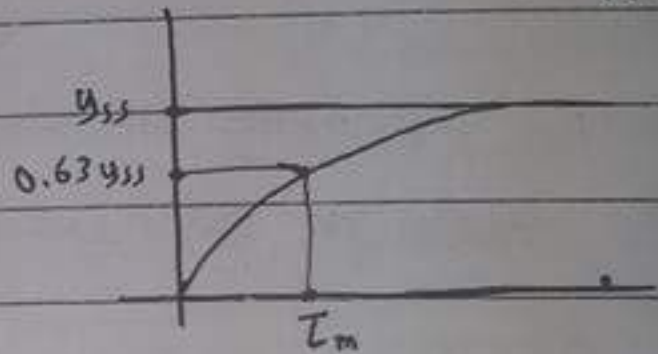
current

1st order

3) DC Motor "speed"

$$T(s) = \frac{K_m}{\tau_m s + 1}$$

$$= \frac{17.2}{66s + 1}$$



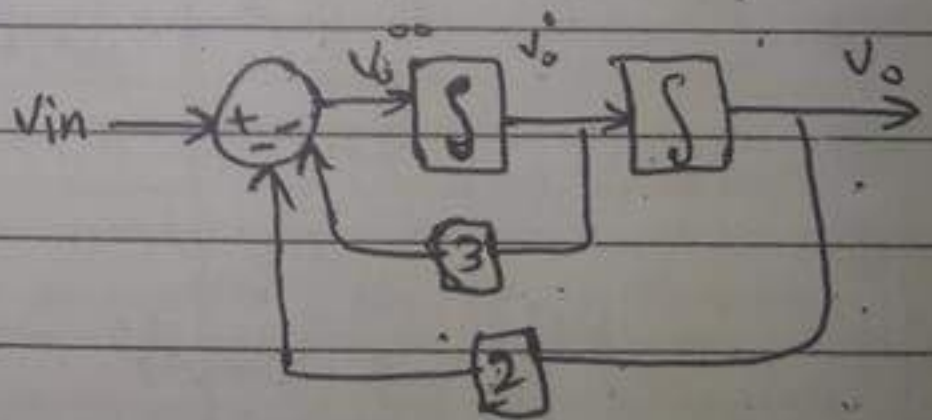
$$K_m = \frac{y_{ss}}{I/P}$$

$$\tau_m \rightarrow 0.634 s$$

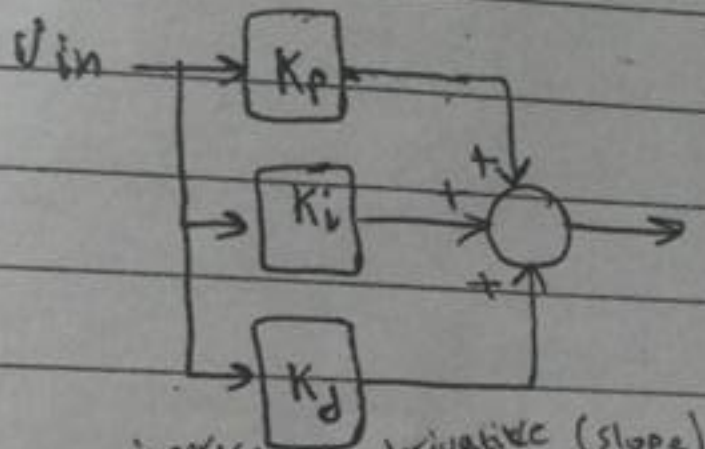
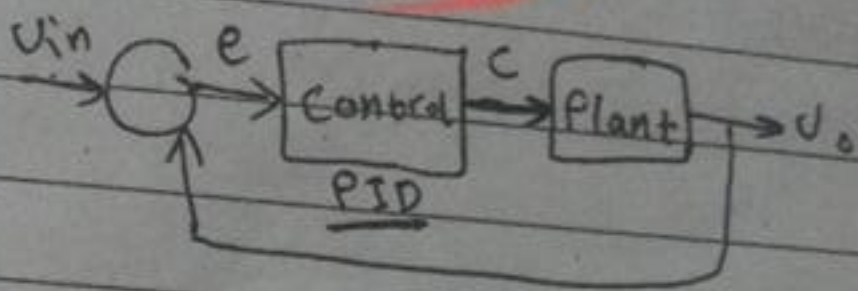
$$\frac{V_o}{V_{in}} = \frac{1}{s^2 + 3s + 2}$$

$$V_o'' + 3V_o' + 2V_o = V_{in}$$

$$V_o'' = V_{in} - 3V_o' - 2V_o$$



PIDc:



K_p : without time
 K_i : $\int e \cdot dt$ (Area)
 K_d : derivative (slope)

$$\frac{v_o}{v_{in}} = \left(K_p + \frac{K_i}{s} + K_d s \right)$$

without time

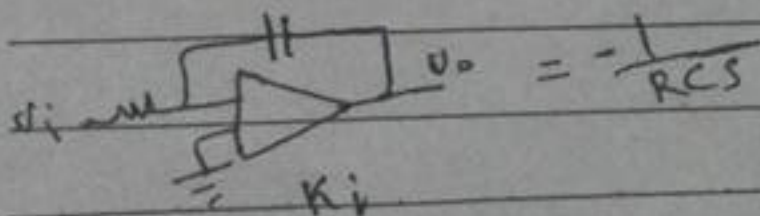
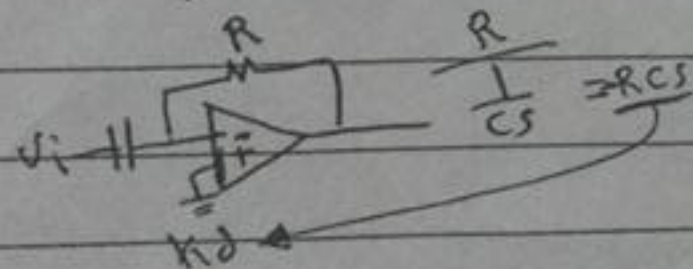
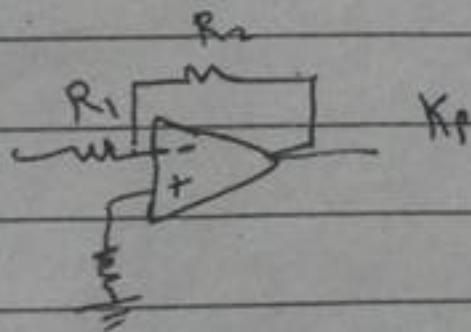
Part time

future time

(eliminate steady state error)

(If the gain increase error increase)

$$e_{ss} = 0$$



PID Controller and Tuning

prepared by Eng. Sarah AL-Bargothi

Tuning the PID Controller

Tuning the PID controller can be like learning to roller blade, ski or maybe riding a bull. Until you've done it a few times, the literature you've read really doesn't hit home. But after few attempts (and falls), you find it wasn't so bad after all - in fact it was kind of fun!

Although you'll find many methods and theories on tuning a PID, here's a straight forward approach to get you up and soloing quickly.

1. SET KP. Starting with $KP=0$, $KI=0$ and $KD=0$, increase KP until the output starts overshooting and ringing significantly.
2. SET KD. Increase KD until the overshoot is reduced to an acceptable level.
3. SET KI. Increase KI until the final error is equal to zero.

the other two. For this reason, the table should only be used as a reference when you are determining the values for K_i , K_p and K_d .

Implementing the PID Controller Using Op-Amp

Figure 1 shows how to separately implement a P, D and an I controllers.

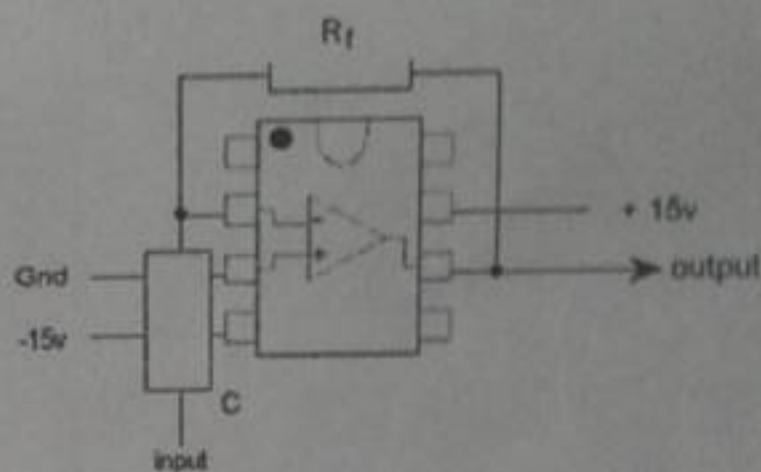
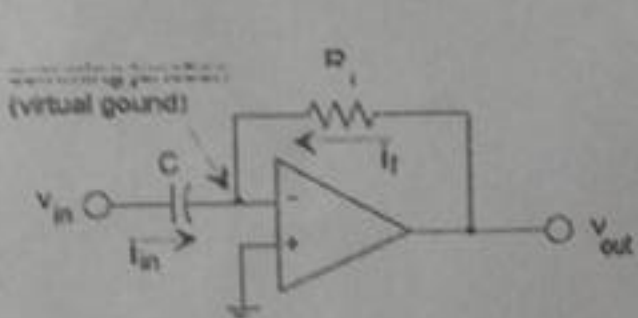


Figure 1.a

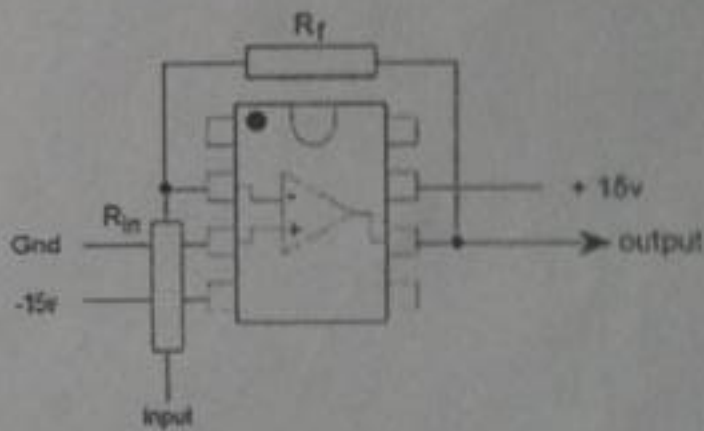
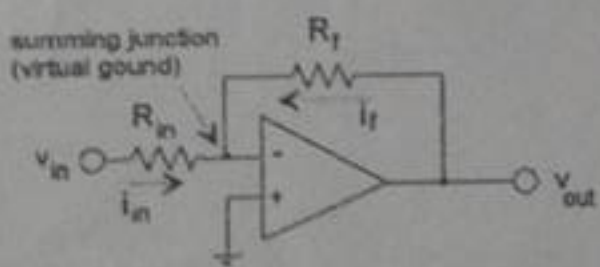


Figure 1.b

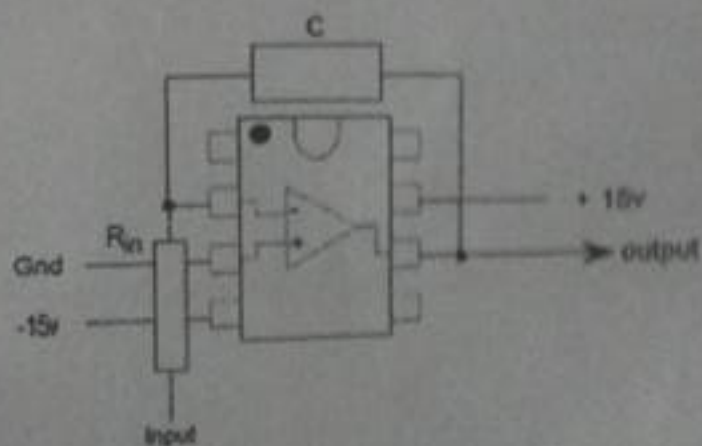
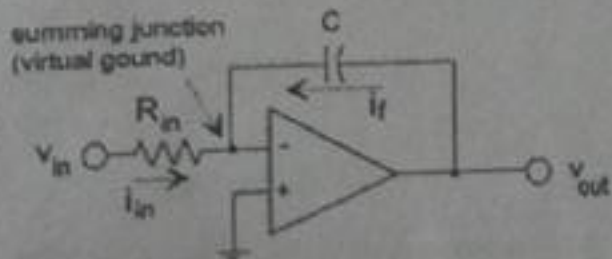


Figure 1.c

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