



تقدم لجنة EiCoM الاكاديمية

ريبورتات لمختبر :

الفيزياء العامة
العملية



EXPERIMENT 2: Measurement and Uncertainties

Analysis

A. Measurement of π

Since $C = \pi d$ (C is circumference, d is the diameter), you determine the value of π , report each measurement five times,

Trial No.	d(cm)	$(d - \bar{d})^2$	c (cm)	$(c - \bar{c})^2$
1	3.75	0.000081	11.7	0
2	3.72	0.000441	11.8	0.01
3	3.735	0.000036	11.7	0
4	3.77	0.000841	11.7	0
5	3.73	0.000121	11.6	0.01
Average	$\bar{d} = 3.741 \text{ cm}$		$\bar{c} = 11.7 \text{ cm}$	
	$\Delta\bar{d} = \pm 0.00871 \text{ cm}$		$\Delta\bar{c} = \pm 0.03162 \text{ cm}$	

- Using your average measured values of \bar{d} and \bar{c} , calculate $\bar{\pi}$.

$$\bar{c} = \bar{d} \bar{\pi}$$

$$\bar{\pi} = \frac{\bar{c}}{\bar{d}} = \frac{11.7 \text{ cm}}{3.741 \text{ cm}} = 3.1275$$

- Calculate $\Delta\bar{\pi}$ ($\Delta\pi = \bar{\pi} \sqrt{(\frac{\Delta\bar{d}}{\bar{d}})^2 + (\frac{\Delta\bar{c}}{\bar{c}})^2}$)

$$\Delta\pi = (3.1275) \sqrt{\left(\frac{0.00871}{3.741}\right)^2 + \left(\frac{0.03162}{11.7}\right)^2} = 0.011$$

3. Calculate the error $\Delta\bar{d}$, in measuring the diameter of the disk, and $\Delta\bar{c}$ in measuring the circumference and enter the values calculated in the table above.

To calculate (\bar{d}) :

$$\bar{d} = \frac{\Sigma d}{n} = \frac{(3.75+3.72+3.735+3.77+3.73)}{5} = 3.741 \text{ (cm)}$$

To calculate (\bar{c}) :

$$\bar{c} = \frac{\Sigma c}{n} = \frac{((11.7 \times 3) + 11.8 + 11.6)}{5} = 11.7 \text{ (cm)}$$

To calculate ($\Delta\bar{d}$) :

$$\Delta\bar{d} = \sqrt{\frac{\Sigma_1^5 (d - \bar{d})^2}{5(5-1)}} = \sqrt{\frac{(0.000081 + 0.000441 + 0.000036 + 0.000841 + 0.000121)}{5 \times 4}} = 0.00871 \text{ (cm)}$$

To calculate ($\Delta\bar{c}$) :

$$\Delta\bar{c} = \sqrt{\frac{\Sigma_1^5 (c - \bar{c})^2}{5(5-1)}} = \sqrt{\frac{((0 \times 3) + (0.01 \times 2))}{5 \times 4}} = 0.03162 \text{ (cm)}$$

4. Which quantity contributes more to the error in the $\bar{\pi}$? ($\Delta\bar{d}/\bar{d}$, $\Delta\bar{c}/\bar{c}$)

The ratio of ($\frac{\Delta\bar{c}}{\bar{c}}$) is greater than the ratio of ($\frac{\Delta\bar{d}}{\bar{d}}$), so it is ($\frac{\Delta\bar{c}}{\bar{c}}$) that contributes the most to the error of $\bar{\pi}$.

$$\frac{\Delta\bar{c}}{\bar{c}} = \frac{0.03162}{11.7} = 0.0027$$

$$\frac{\Delta\bar{c}}{\bar{c}} > \frac{\Delta\bar{d}}{\bar{d}}$$

$$\frac{\Delta\bar{d}}{\bar{d}} = \frac{0.00871}{3.741} = 0.0023$$

5. Does the measured average value of $\bar{\pi}$ agree with the accepted value of $\pi(3.14159)$ (percent error)

$$P.E = \frac{|3.14159 - 3.1275|}{3.14159} \times 100\% = 0.44\%$$

- B. Determination of the density:
Record your data in the following table

Trial No.	h(cm)	$(h - \bar{h})^2$	d (cm)	$(d - \bar{d})^2$
1	11.315	0.000484	0.603	0.00007056
2	11.37	0.001089	0.605	0.00004096
3	11.325	0.000144	0.616	0.00002116
4	11.325	0.000144	0.622	0.00011236
5	11.35	0.000169	0.611	0.00000016
Average	$\bar{h} = 11.337 \text{ cm}$		$\bar{d} = 0.6114 \text{ cm}$	
Error	$\Delta\bar{h} = \pm 0.0100747 \text{ cm}$		$\Delta\bar{d} = \pm 0.035 \text{ cm}$	
Mass	$m = 45.63 \text{ g}$		$\Delta m = \pm 0.01 \text{ g}$	

1. Find the **average value** of the calculated densities and compare it with the standard value of this material density ($\rho = 8.65 \text{ g/cm}^3$)? [find the percent error]

$$\bar{\rho} = \frac{4m}{\pi\bar{d}^2\bar{h}} = \frac{4 \times 45.63}{(3.1275) \times (0.6114)^2 \times 11.337} = 13.77 \text{ (g/cm}^3\text{)}$$

$$P.E = \frac{|13.77 - 8.65|}{8.65} \times 100\% = 59.19\%$$

2. Calculate the error in the density ($\Delta\rho$) ($\Delta\bar{\rho} =$

$$\bar{\rho} \sqrt{\left(\frac{\Delta m}{m}\right)^2 + \left(\frac{\Delta \bar{h}}{\bar{h}}\right)^2 + \left(\frac{2\Delta \bar{d}}{\bar{d}}\right)^2 + \left(\frac{\Delta \bar{\pi}}{\bar{\pi}}\right)^2}$$

$$\begin{aligned} \Delta\bar{\rho} &= (13.77) \sqrt{\left(\frac{0.01}{45.63}\right)^2 + \left(\frac{0.0100747}{11.337}\right)^2 + \left(\frac{2(0.035)}{0.6114}\right)^2 + \left(\frac{0.011}{3.1275}\right)^2} \\ &= 1.57721 \end{aligned}$$

3. Which quantity contributes more to the error in the density; the mass, the diameter or the height? Why? (see part A 4) $\left(\frac{\Delta m}{m}, \frac{\Delta \bar{h}}{\bar{h}}, \frac{2\Delta \bar{d}}{\bar{d}}, \frac{\Delta \bar{\pi}}{\bar{\pi}}\right)$

$$\frac{\Delta m}{m} = \frac{0.01}{45.63} = 0.000219$$

$$\frac{\Delta \bar{h}}{\bar{h}} = \frac{0.0100747}{11.337} = 0.0008865$$

$$\frac{2\Delta \bar{d}}{\bar{d}} = \frac{2(0.035)}{0.6114} = 0.1144$$

$$\frac{\Delta \bar{\pi}}{\bar{\pi}} = \frac{0.011}{3.1275} = 0.00351$$

$\frac{2\Delta \bar{d}}{\bar{d}}$ is more contributes to uncertainty in density ($\bar{\rho}$) because ($\frac{2\Delta \bar{d}}{\bar{d}}$ is the largest one) .

Mohammed Abadi ♥